

A Modern Perspective on Fault Tree Analysis

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Roadmap of This Tutorial

Part 1. What are Dynamic Fault Trees?

- DFT Elements, Benchmarks, Intricacies, DFTs as Stochastic Petri Nets

Part 2. From DFTs to Markov Models, Compositionally

- Compositional State-Space Minimisation, Non-Determinacy

Part 3. From DFTs to Markov Models, Monolithically

- Symmetry Reduction, Don't Care Propagation

Part 4. DFT Analysis by Model Checking

- Reliability Measures, Core Algorithms, Storm Tool

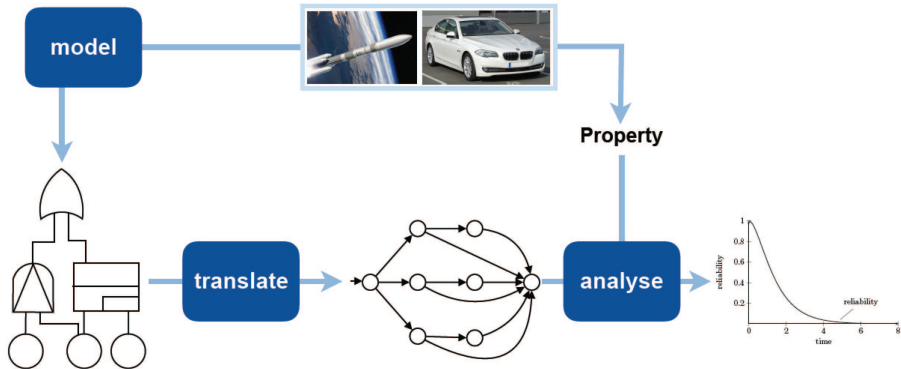
Part 5. Advanced Optimisations

- Graph Rewriting, Partial State-Space Generation

Part 6. Industrial Applications and Outlook

Focus is on conveying intuition and experimental results

Graphical Overview



Overview Part 1 and 2

Introduction

Part 1. What are Dynamic Fault Trees?

- Static Fault Trees

- Dynamic Fault Trees

Part 2: From DFTs to Markov Models

- What do DFTs Mean? A Petri Net View

- Semantic Intricacies

- Compositional Model Generation and Minimisation

Overview

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- Static Fault Trees

- Dynamic Fault Trees

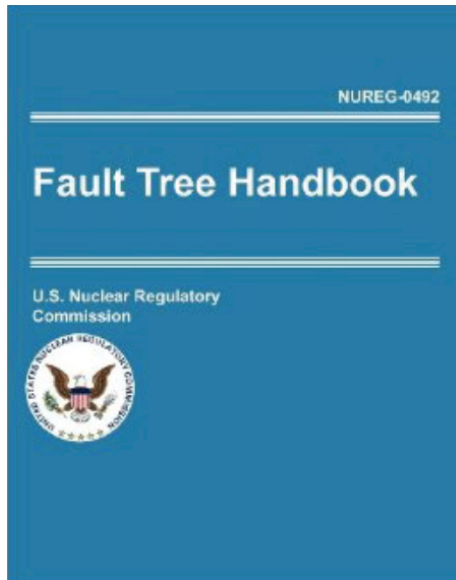
Part 2: From DFTs to Markov Models

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- Semantic Intricacies

- Compositional Model Generation and Minimisation

Reliability Engineering



Reliability Engineering

- ▶ Risk analysis ensures that critical assets, like medical devices and nuclear power plants, operate in a safe and reliable way.
- ▶ Fault tree analysis (FTA) is one of the most prominent techniques.
- ▶ Used by a wide range of industries (aerospace, automotive, nuclear, medical, process engineering)
- ▶ Used by many companies and institutions: FAA, NASA, ESA, Airbus, Honeywell, etc.
- ▶ Industrial standards by the IEC and by ISO for automotive applications

The SpaceX Falcon-9 Explosion



Elon Musk ✓ @elonmusk · 28 Jun 2015

There was an overpressure event in the upper stage liquid oxygen tank. Data suggests counterintuitive cause.



471



4.1K



3.3K



Elon Musk ✓

@elonmusk

Follow

That's all we can say with confidence right now. Will have more to say following a thorough fault tree analysis.

A launch failure in 2015 resulted in a loss of a quarter billion dollars.

Overview

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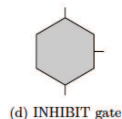
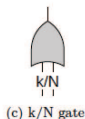
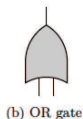
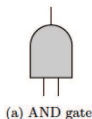
Fault Trees

- ▶ Fault trees (FTs) are a **graphical** method that model how failures propagate through the system
- ▶ They model how do component failures lead to system failures?
- ▶ Not all component failures lead to a system failure due to redundancy, spare management, etcetera.

Reliability: Static Fault Trees

[Watson, 1961–62]

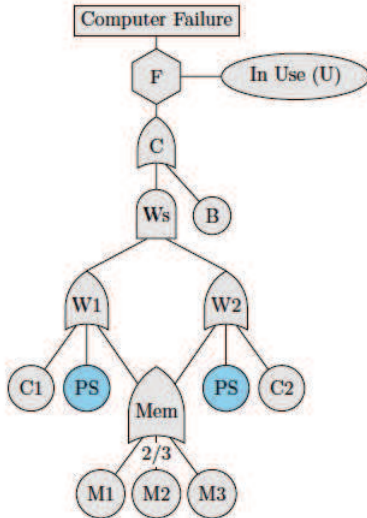
- ▶ Fault tree is a **directed acyclic graph** consisting of two types of nodes: **events** (depicted as circles) and **gates**:



- ▶ An **event** is an occurrence within the system, typically the failure of a component or sub-system.
- ▶ Events can be divided into:
 - ▶ **basic** events (BEs), which occur on their own, and
 - ▶ **intermediate events**, which are caused by other events
- ▶ The root, called the **top level event** (TLE), models a system failure

Static Fault Trees

[Watson, 1961–62]



Legend:

F: Computer failure while in use

C: Computer failure

Ws: Failure of both workstations

B: Bus failure

W1: Failure of workstation 1

W2: Failure of workstation 2

C1: Failure of CPU 1

C2: Failure of CPU 2

PS: Failure of power supply

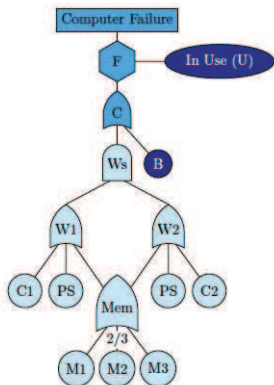
Mem: Failure of memory system

M1: Failure of memory module 1

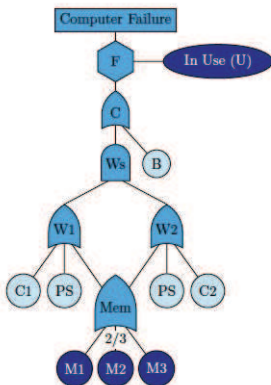
M2: Failure of memory module 2

M3: Failure of memory module 3

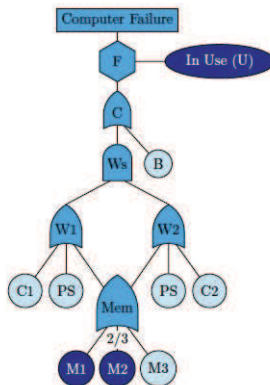
Minimal Cut Sets



minimal



not minimal

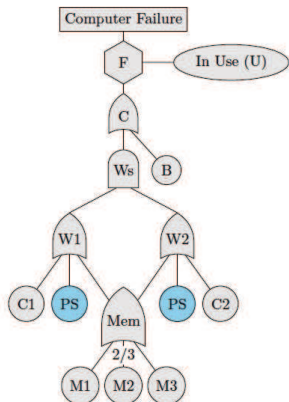


minimal

A **cut set** is a set of components that together can cause the system to fail.

A **minimal** cut set is a cut set without proper subset being a cut set.

Boolean Manipulation



- ▶ Turn SFT into a propositional Boolean formula
- ▶ **Top-down:** $F, F \wedge C, F \wedge (B \vee Ws), (F \wedge B) \vee (F \wedge Ws), \dots$
- ▶ Halt when all gates are eliminated
- ▶ This yields all MCSs
- ▶ **Bottom-up:** $W1 = C1 \vee PS \vee Mem,$
- ▶ $Mem = (M1 \wedge M2) \vee \dots \vee (M2 \wedge M3), \dots$
- ▶ This yields cut sets for all gates

Efficient implementation: using **BDDs**.

Probability calculations are done on top of the analysis using minimal cut sets.

Methods for Minimal Cut Sets

Author	Method	Remarks	Tool
Vesely et al. [VGRH81]	Top-down	Classic boolean method	MOCUS [FHM74]
Vesely et al. [VGRH81]	Bottom-up	Produces MSC for gates	MICSUP [PSC75]
Coudert and Madre [CM93]	BDD	Usually faster than classic methods	MetaPrime [CM94]
Rauzy [Rau93]	BDD	Only for coherent FTs but faster than [CM93]	Aralia [RD97]
Dutuit and Rauzy [DR96]	Modular BDD	Faster for FTs with independent submodules	DIFTree [DVG97]
Remenyte et al. [RA06, RPA08]	BDD	Comparison of BDD construction methods	-
Codetta-Raiteri [CR06]	BDD	Faster when FT has shared subtrees	-
Xiang et al. [XYM ⁺ 11]	Minimal Cut Vote	Reduced complexity with large voting gates	CASSI [XYM ⁺ 11]
Carrasco et al. [Cn99]	CS-Monte Carlo	Less complex for FTs with few MCS	-
Vesely and Narum [VN70]	Monte Carlo	Low memory use, accuracy not guaranteed	PREP [VN70]

Analysing static fault trees is relatively simple as the ordering of failures is irrelevant.
It only matters whether an event has occurred or not.

Deficiencies of Static Fault Trees

Main limitations of static fault trees:

- ▶ Too simple for practical systems
- ▶ They lack common dependability patterns, such as:
 - ▶ spare management
 - ▶ functional dependencies
 - ▶ redundancies
- ▶ Static behaviour:
 - ▶ TLE failure only depends on the set of failed events, not on any temporal ordering of faults

Dynamic Fault Trees

[Dugan *et al.*, 1990]

(a) BE



(b) AND



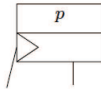
(c) OR



(d) PAND



(e) POR



(f) PDEP

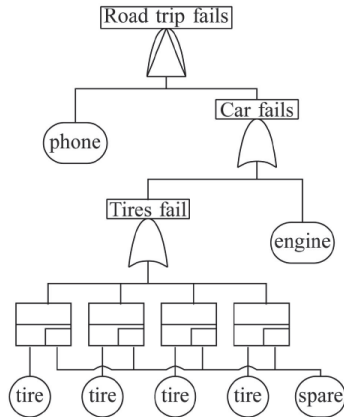


(g) SEQ

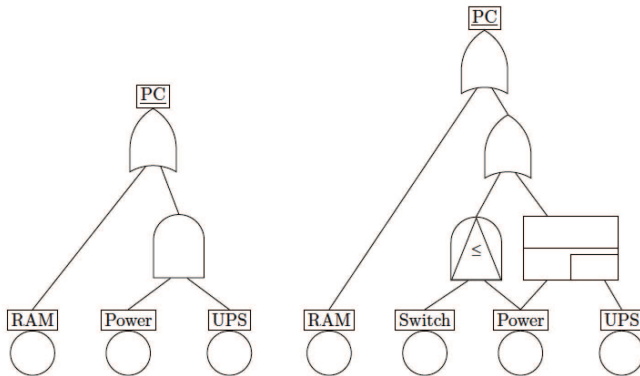


(h) SPARE

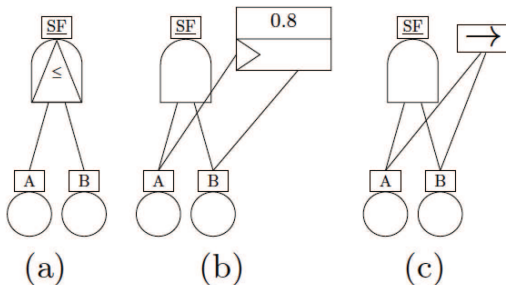
A Simple DFT Example

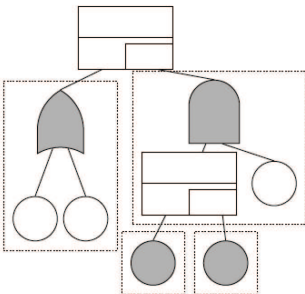


A Simple DFT Example

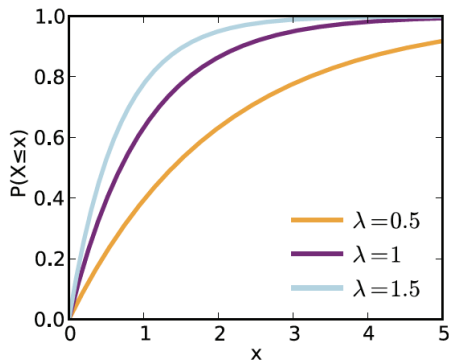
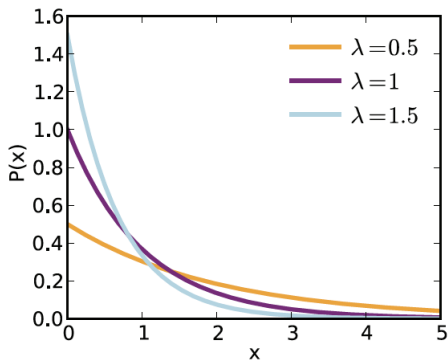


Dynamic Gates: PAND, FDEP, and SEQ



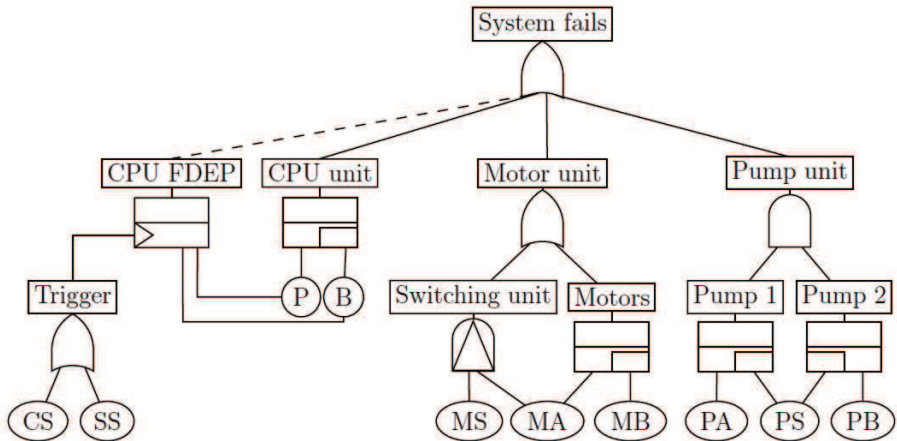


Failures := Exponential Distributions



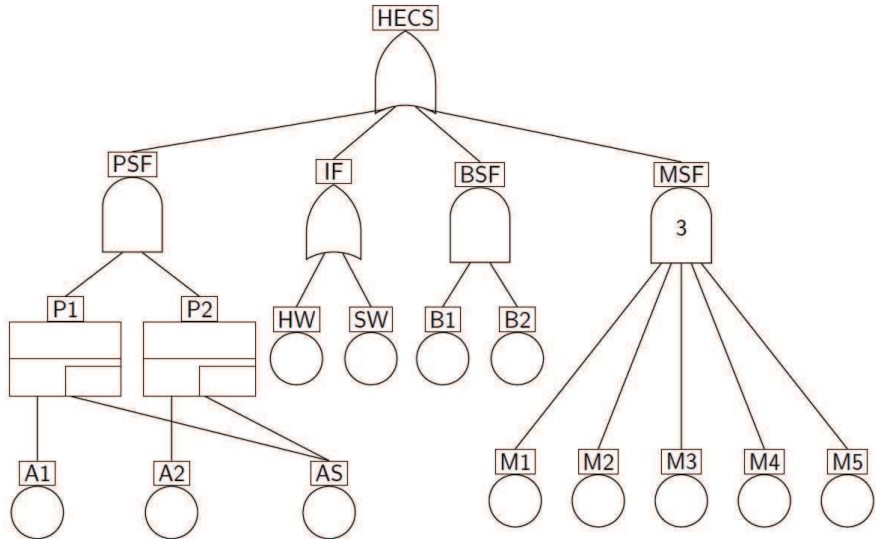
The higher the rate λ , the faster the cdf approaches 1.

Benchmark DFT: Cardiac Assist System [Boudali & Dugan, 2005]

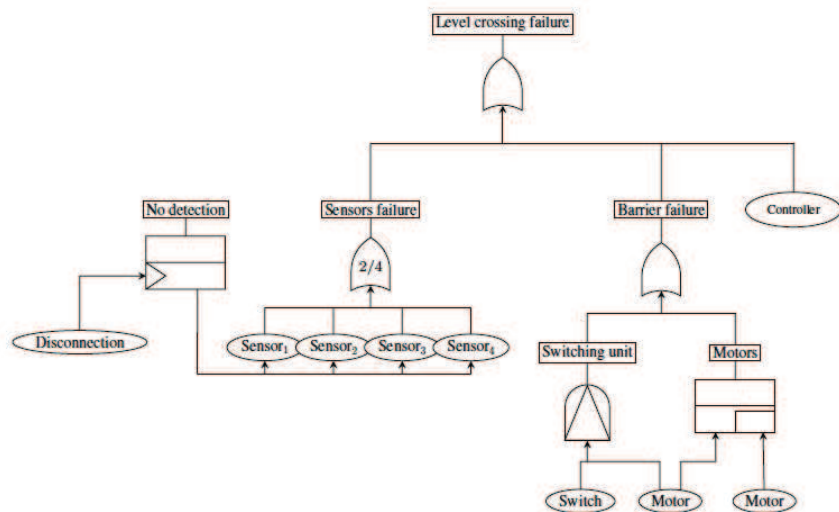


Benchmark DFT: HECS

[NASA Handbook, 1982]

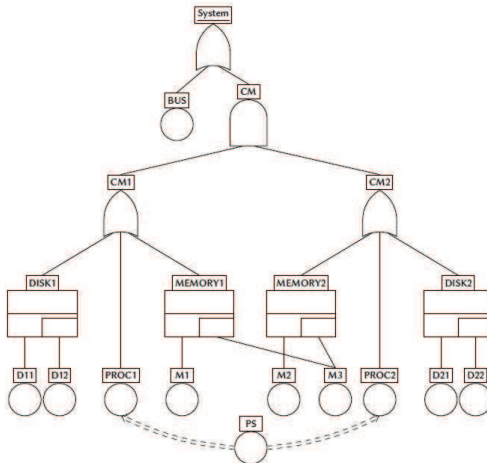


Benchmark DFT: Railway Crossing

[Guck *et al.*, 2014]

Benchmark DFT: MCS

[Malhotra & Trivedi, 1995]



Multiprocessor Computing System

The Price of DFTs

- ▶ Analysis can **no longer** be done using **minimal cut sets**
 - ▶ Generalisations towards cut sequences are insufficient
 - ⇒ The DFT behaviour is **history-dependent**
- ▶ DFT analysis is done by generating a **stochastic (decision) process**¹
 - ▶ Monolithic approach
 - ▶ Compositional approach
 - ▶ Approaches via other models (e.g., Bayes' networks or Petri nets)
- ▶ Use **Markov Chain analysis techniques** to obtain quantitative measures
 - ▶ We use **probabilistic model checking**

¹Continuous-Time Markov Chain.

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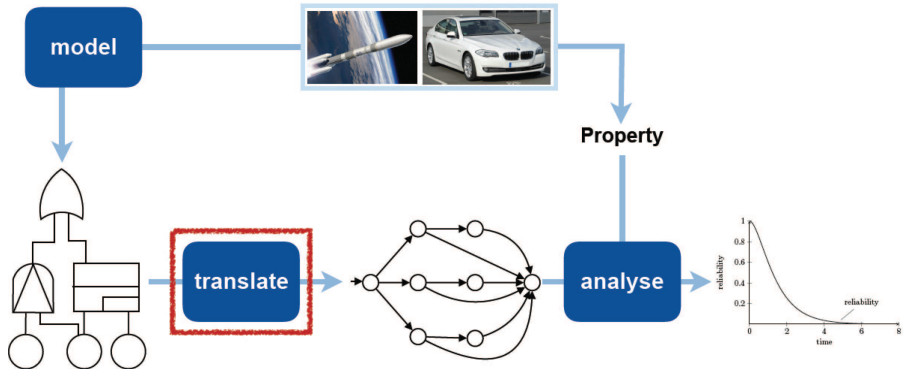
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- What do DFTs Mean? A Petri Net View

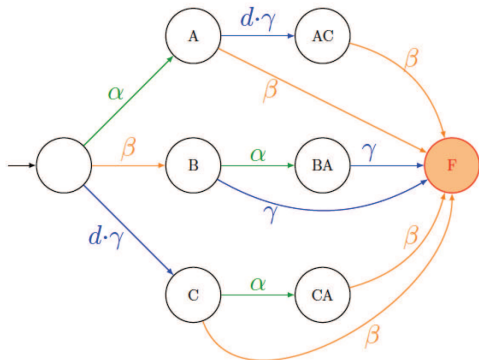
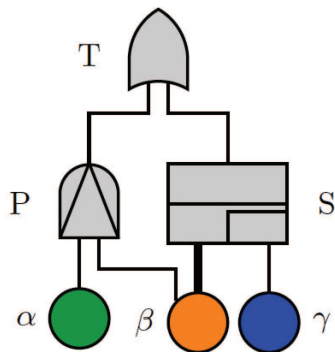
- Semantic Intricacies

- Compositional Model Generation and Minimisation

Graphical Overview



The Markov Model of a DFT



$d :=$ dormancy factor

State-space generation
is a major bottleneck in DFT analysis.

Myths About Dynamic Fault Trees

“Although DFTs are powerful in modeling systems with dynamic failure behaviors, their **quantitative analyses** are pretty much **troublesome**, especially for large scale and complex DFTs.”

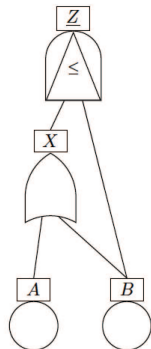
[Ge *et al.*, Rel. Eng. Syst. Safe, 2015]

“Although many **extensions of fault trees** have been proposed, they suffer from a variety of shortcomings. In particular, even where software tool support exists, these **analyses require a lot of manual effort**.”

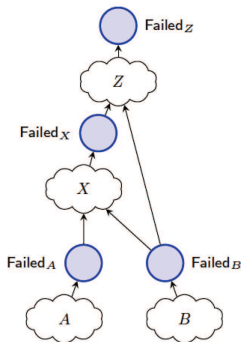
[Kabir, Expert Syst. Appl., 2017]

We will show that these are myths. Scalable DFT analysis is possible.

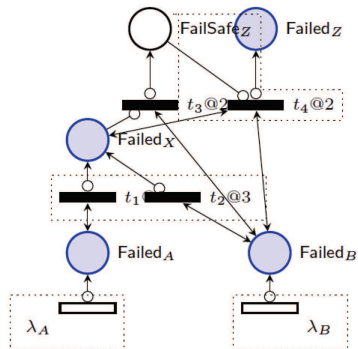
Use Nets to Capture The Meaning of DFTs



(a) DFT



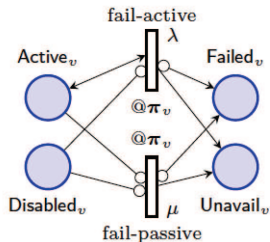
(b) Basic scheme



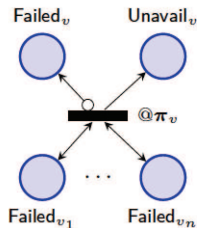
(c) Simplified resulting GSPN

This provides a meaning to DFTs in a **compositional** manner

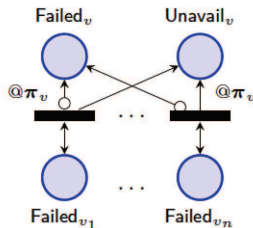
Nets for Static Gates



(a) BE

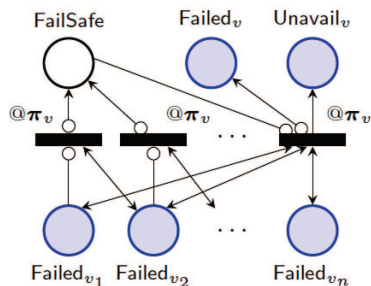


(b) AND

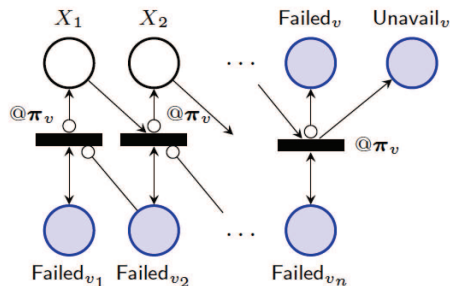


(c) OR

Nets for PANDs

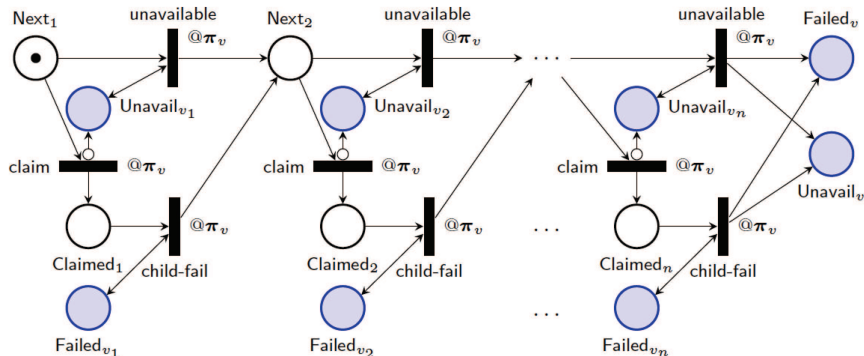


(a) Inclusive PAND_≤



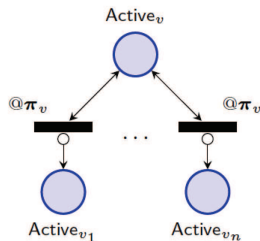
(b) Exclusive PAND_<

A Net for the SPARE Claiming Mechanism

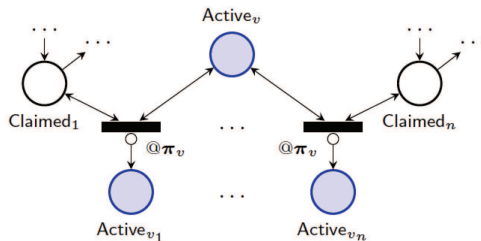


Claiming: a SPARE uses **one** of its children. If this **child fails**, the SPARE tries to **claim another child** (left to right). Only operational children that are not claimed by another SPARE can be claimed. If claiming **fails** – all spare components have failed – **the SPARE fails**.

A Net for the SPARE Activation Mechanism



(a) Gate



(b) SPARE

Activation: Nodes outside spare “modules” are **disabled** by default. For each **active** SPARE and used child v , the nodes in v ’s spare module are **activated**. **Active** BEs fail with their **active** failure rate, **disabled** BEs with their **passive** failure rate.

GSPNs for DFTs

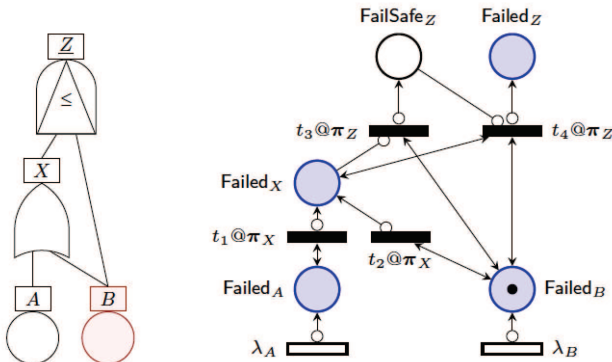
Benchmark	DFT				GSPN		
	#BE	#Dyn.	#Nodes	σ_{\max}	#Places	#Timed Trans.	#Immed. Trans.
HECS 5_5_2_np	61	10	107	16	273	122	181
MCS 3_3_3_dp_x	46	21	80	7	246	92	163
RC 15_15_hc	69	33	103	34	376	138	240

σ_{\max} is the maximal number of children in the DFT

The size of the GSPN is linearly proportional to the DFT size.

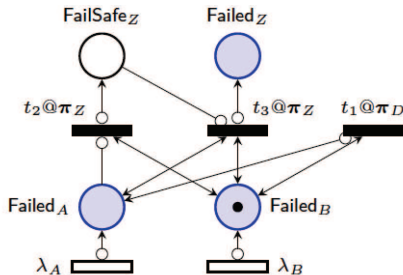
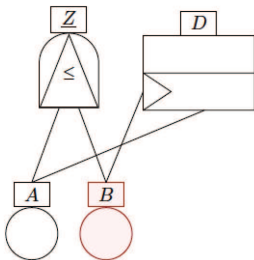
The GSPNs are 2-bounded and have no time traps.

Issue 1: Failure Propagation



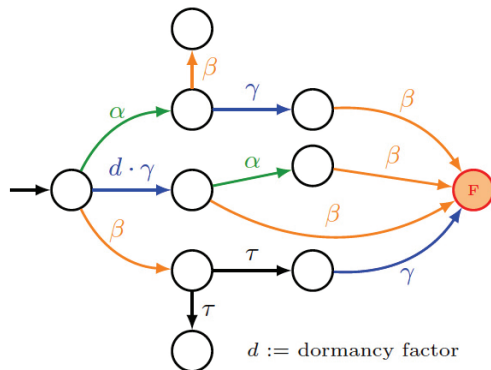
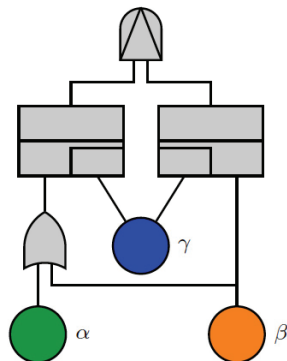
Is B 's failure first propagated to gate X , causing PAND Z to **fail**,
or is B 's failure first propagated to gate Z , turning Z **fail-safe**?

Issue 2: FDEP Failure Forwarding



Is **B**'s failure first propagated via **D**, causing **A** and **Z** to **fail**, or does **B**'s failure first cause **Z** to become **fail-safe** before **A** fails?

Issue 3: Nondeterminism



This phenomenon is called a **spare race**.

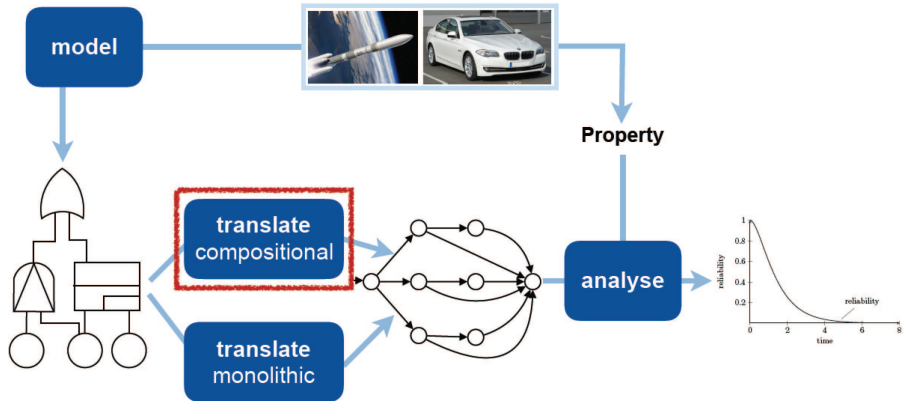
Different Existing DFT Semantics

[Volk *et al.*, 2018]

	Monolithic CTMC [11]	IOIMC [12]	Monolithic MA [13]	Orig. GSPN [7]	New GSPN
Tool support	Galileo [17]	DFTCalc [18]	Storm [19]	—	—
Underlying model	CTMC	IMC [15]	MA [14]	GSPN/CTMC [5, 6]	GSPN/MA [16]
Priority gates	\leq	$<$	\leq	$<$	\leq and $<$
Nested spares	not supported	late claiming	early claiming	not supported	early claiming
Failure propagation	bottom-up	arbitrary	bottom-up	arbitrary	bottom-up
FDEP forwarding	first	interleaved	last	interleaved	first
Non-determinism	uniform	true (everywhere)	true FDEP	uniform	true (PAND, SPARE)

All these different semantics are small twists of the GSPN mapping.
 Only the **priority** mechanism and treatment of **nondeterminacy** differs.

Graphical Overview



Probabilistic Bisimulation

[Larsen & Skou, 1989]

Intuition: transition probabilities for each equivalence class coincide.

Consider a DTMC with state space S and equivalence $R \subseteq S \times S$.
 R is a **probabilistic bisimulation**² on S if for any $(s, t) \in R$:

$$L(s) = L(t) \quad \text{and} \quad \mathbf{P}(s, C) = \mathbf{P}(t, C) \quad \text{for each } C \in S/R$$

where $\mathbf{P}(s, C) = \sum_{s' \in C} \mathbf{P}(s, s')$.

Let \sim denote the largest possible probabilistic bisimulation.

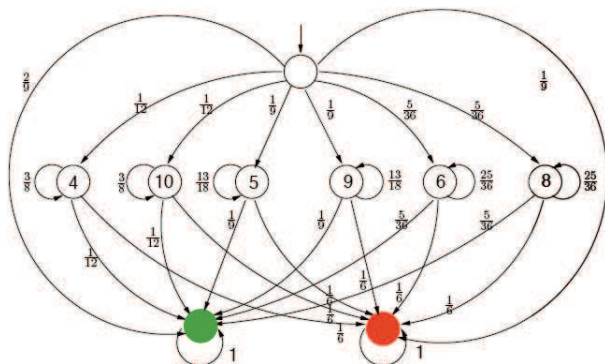
Variants: weak, divergence-sensitive, distribution-based, for CTMC, MDPs, etc.

²**Lumping.**

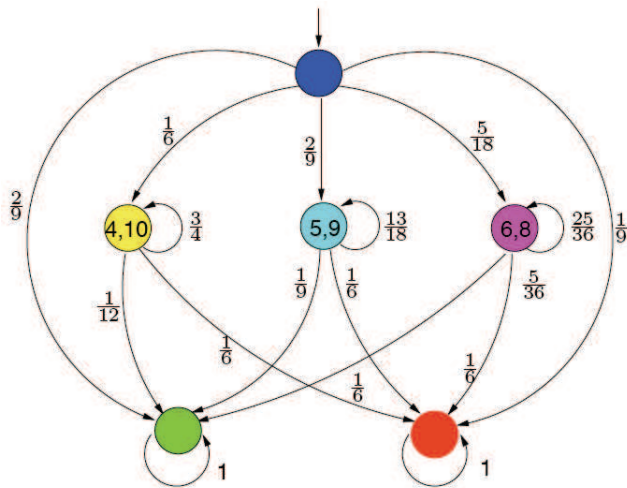
Craps

- ▶ Come-out roll:
 - ▶ 7 or 11: win
 - ▶ 2, 3, or 12: lose
 - ▶ else: roll again

- ▶ Next roll(s):
 - ▶ 7: lose
 - ▶ point: win
 - ▶ else: roll again



Craps's Bisimulation Quotient



Properties

Quotienting: using partition-refinement in $\mathcal{O}(|P| \cdot \log |S|)$

Preservation: all relevant measures-of-interest

Congruence: with respect to parallel composition

$$\mathcal{M} \sim \mathcal{N} \text{ implies } \mathcal{M} \parallel \mathcal{M}' \sim \mathcal{N} \parallel \mathcal{M}'$$

Stuttering: weak variants treat internal transitions in special way

Savings: potentially exponentially in time and space

Compositional Minimisation

[Hermanns and K., 2000]

- Assume system is given by:

$$\mathcal{M}_1 \parallel \dots \parallel \mathcal{M}_i \parallel \dots \parallel \mathcal{M}_k$$

with \mathcal{M}_j a Markov model and parallel composition \parallel

- Recall congruence property:

$$\mathcal{M} \sim \mathcal{N} \text{ implies } \mathcal{M} \parallel \mathcal{M}' \sim \mathcal{N} \parallel \mathcal{M}'$$

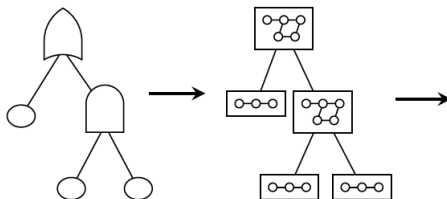
- Component-wise minimisation

- Pick process \mathcal{M}_i and consider its quotient \mathcal{M}_i / \sim under \sim
- Yielding $\mathcal{M}_1 \parallel \dots \parallel \mathcal{M}_i / \sim \parallel \dots \parallel \mathcal{M}_k$; repeat 1. and 2.
- Once all done, minimise pairs $\mathcal{M}_i / \sim \parallel \mathcal{M}_{i+1} / \sim$ etc.

- Finding optimal ordering to minimise is NP-complete

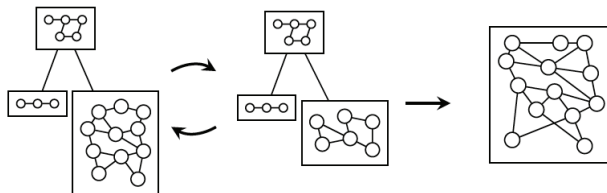
Ordering by heuristics [Crouzen *et al.*, 2008]

Compositional DFT Minimisation

[Crouzen *et al.*, 2010]

(a) DFT

(b) Transformation



(c) Composition

(d) Minimisation

(e) IMC

Compositional DFT Minimisation

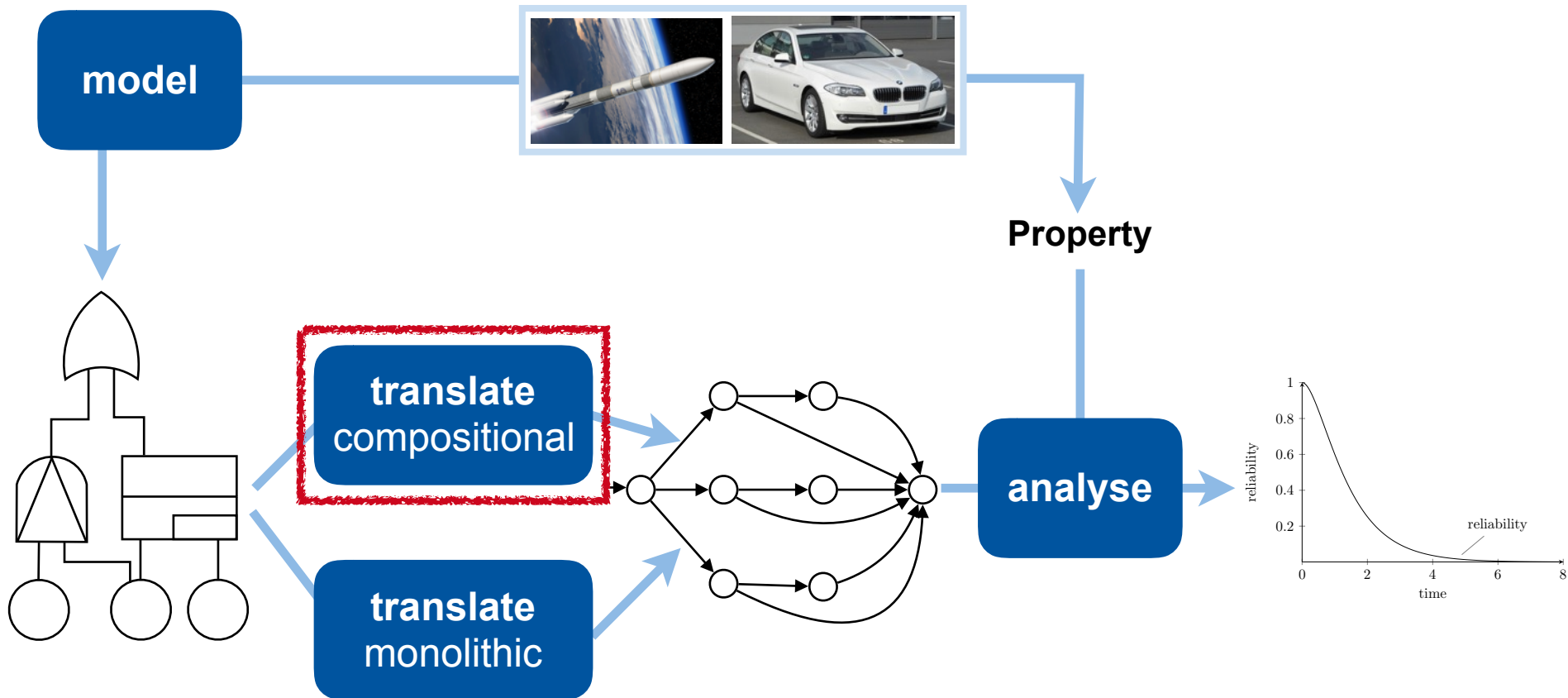
[Crouzen *et al.*, 2010]

case study	peak # states	# transitions	unreliability	time (s)
CPS	4113	24608	.00135	490
CAS	8	10	.65790	1
CAS-PH	x	x	x	x
NDPS	x	x	x	x
FTTP-4	32757	426826	.01922	13111
FTTP-5	MO	MO	MO	MO

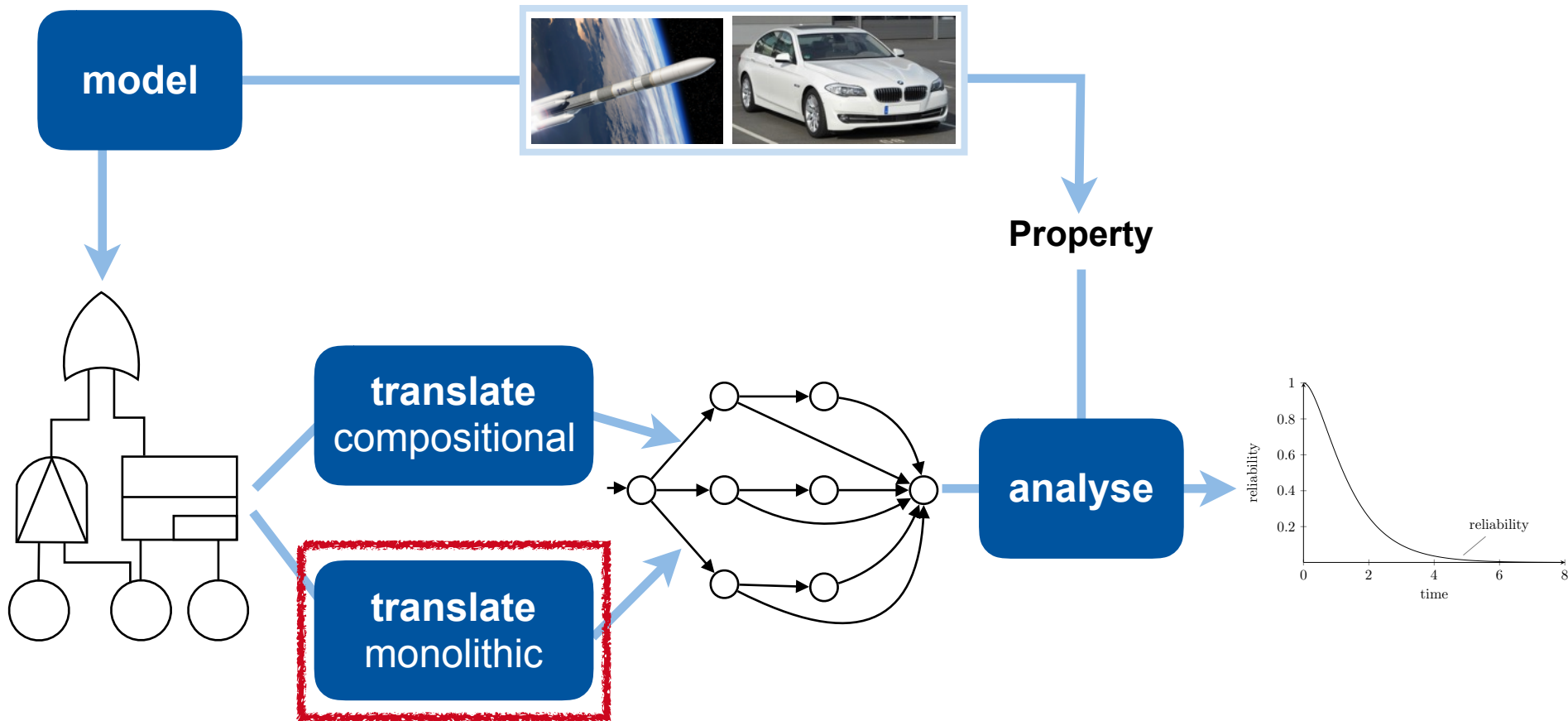
CPS	133	465	.00135	67
CAS	36	119	.65790	94
CAS-PH	40052	265442	.112	231
NDPS	61	169	[.00586, .00598]	266
FTTP-4	1325	13642	.01922	65
FTTP-6	11806565	22147378	.00045	1989

Comparing Galileo DIFTree (1995, top) to DFTCalc (2011, bottom)

Overview



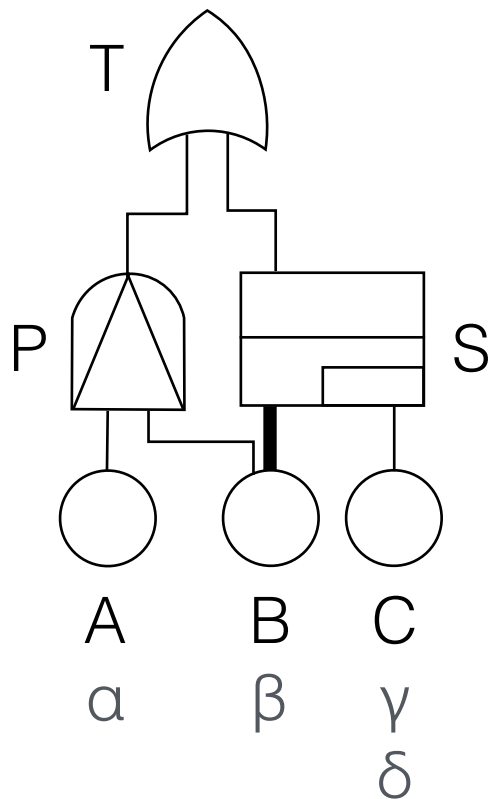
Overview



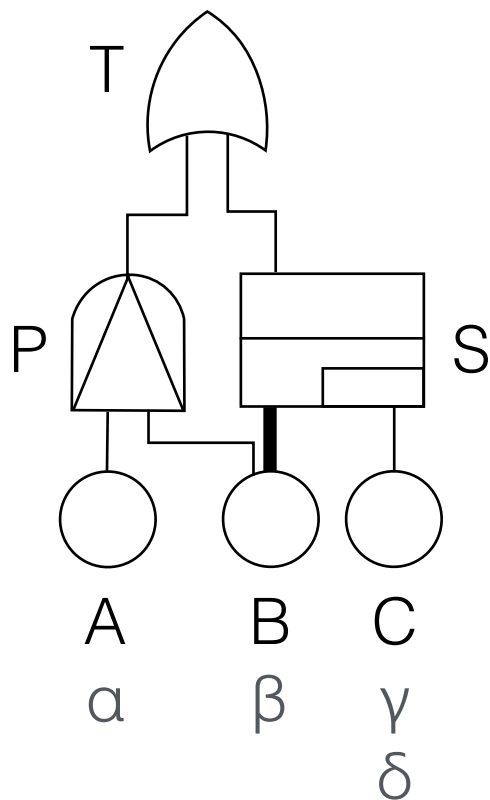
Monolithic idea

- Based on **Galileo** approach
- Generate states of Markov chain **iteratively**:
 1. Let **basic element** in DFT **fail**
 2. **Propagate failure** through the DFT
 3. Resulting failure status of DFT is **new state** in Markov chain

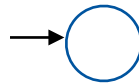
State space exploration



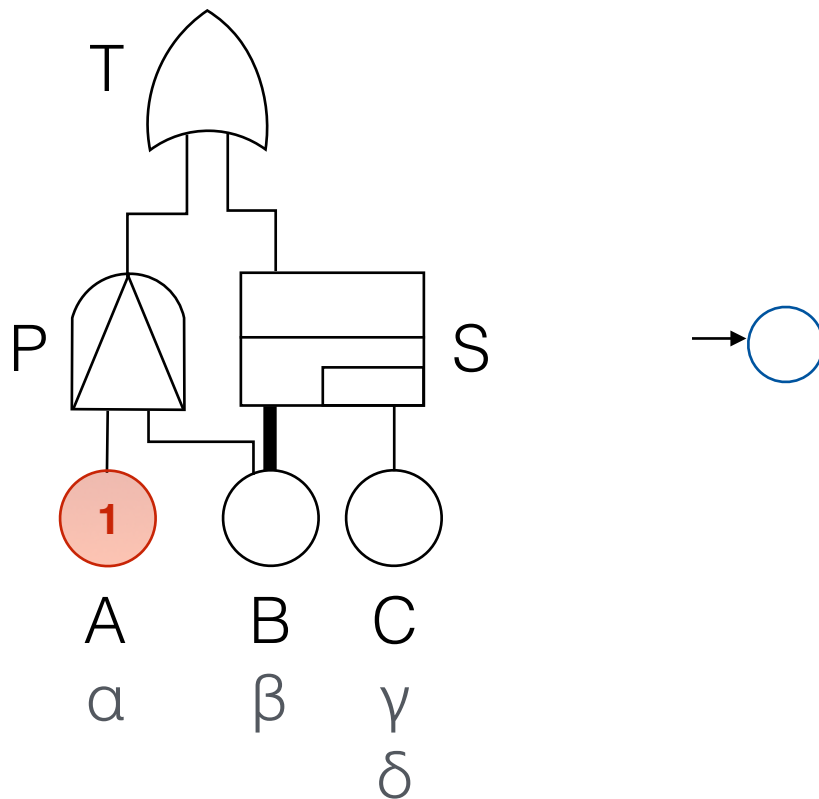
State space exploration



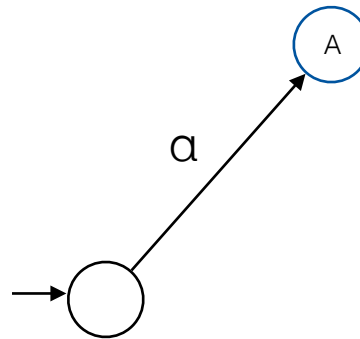
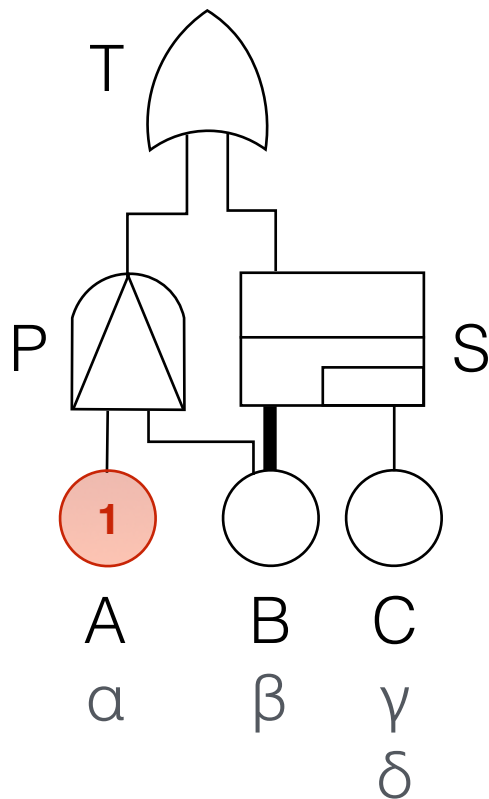
Failure status:
A: Operational
B: Operational
:
S uses B



State space exploration

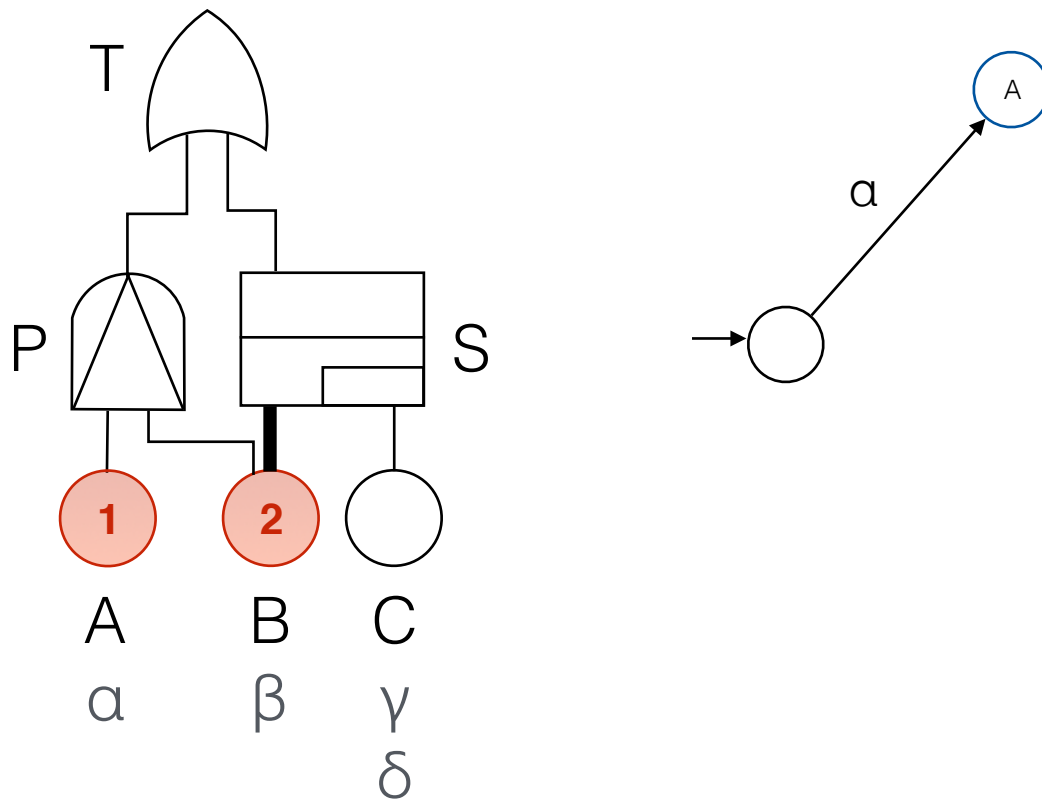


State space exploration

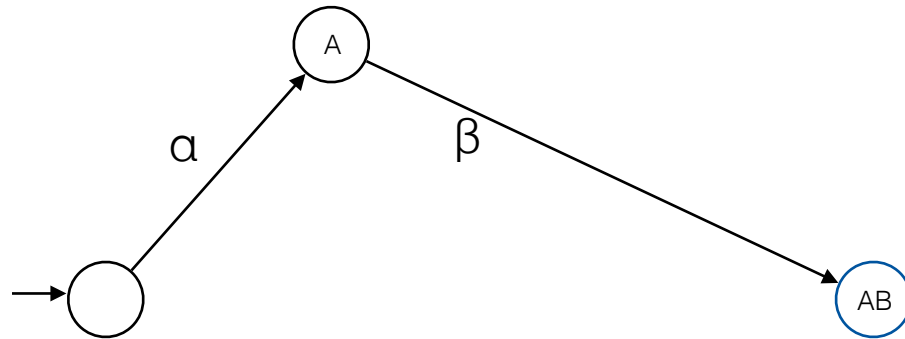
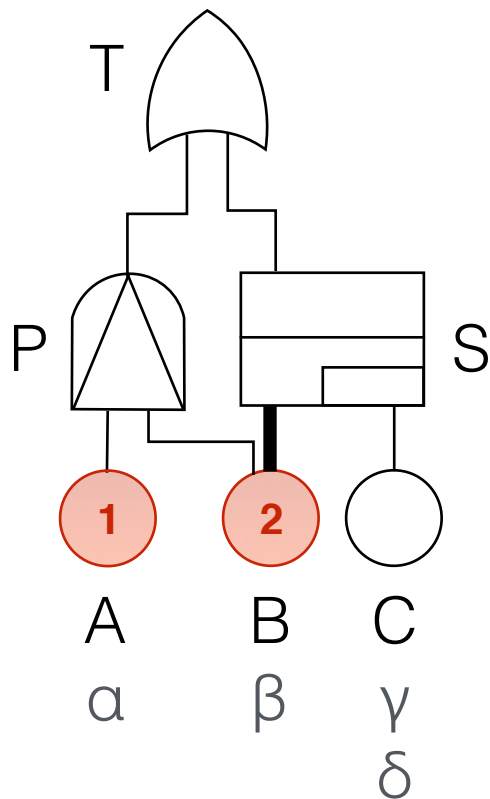


Failure status:
A: Failed
B: Operational
:
S uses B

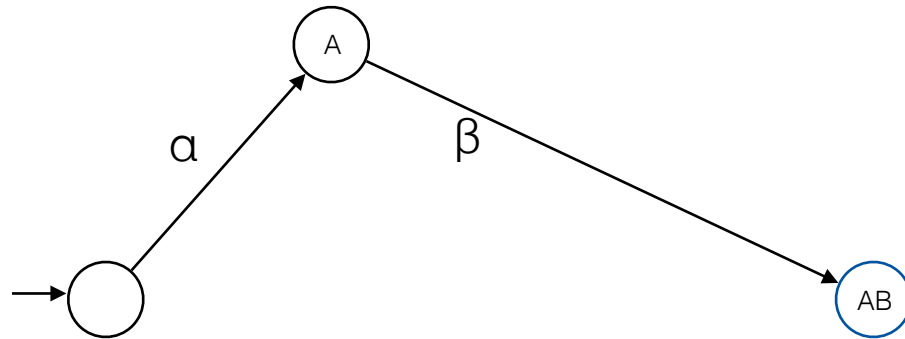
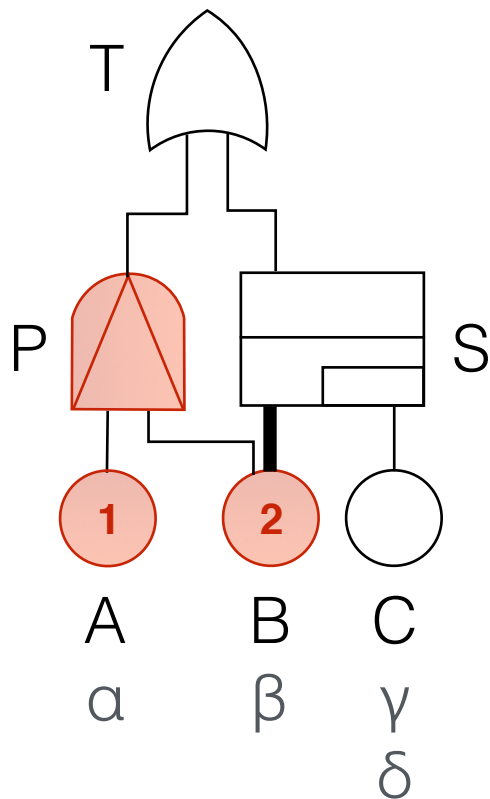
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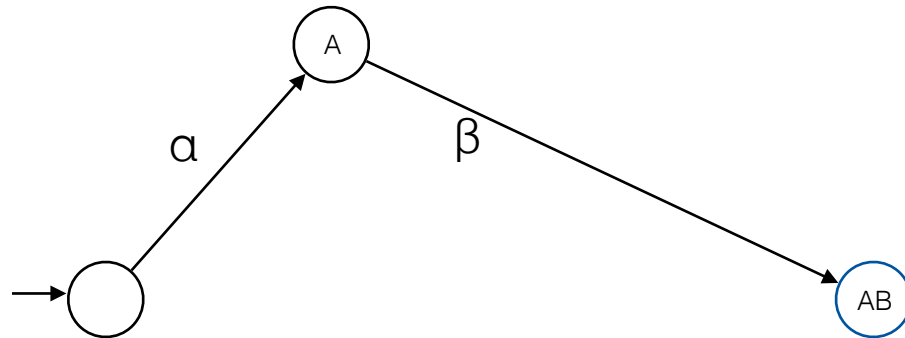
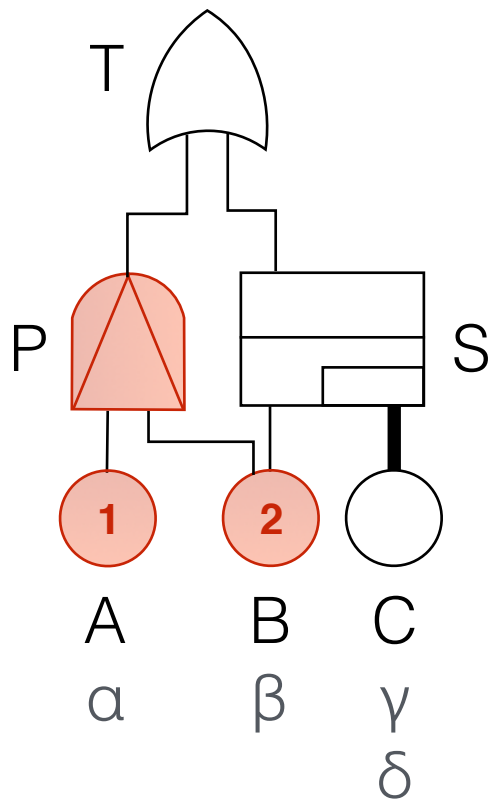
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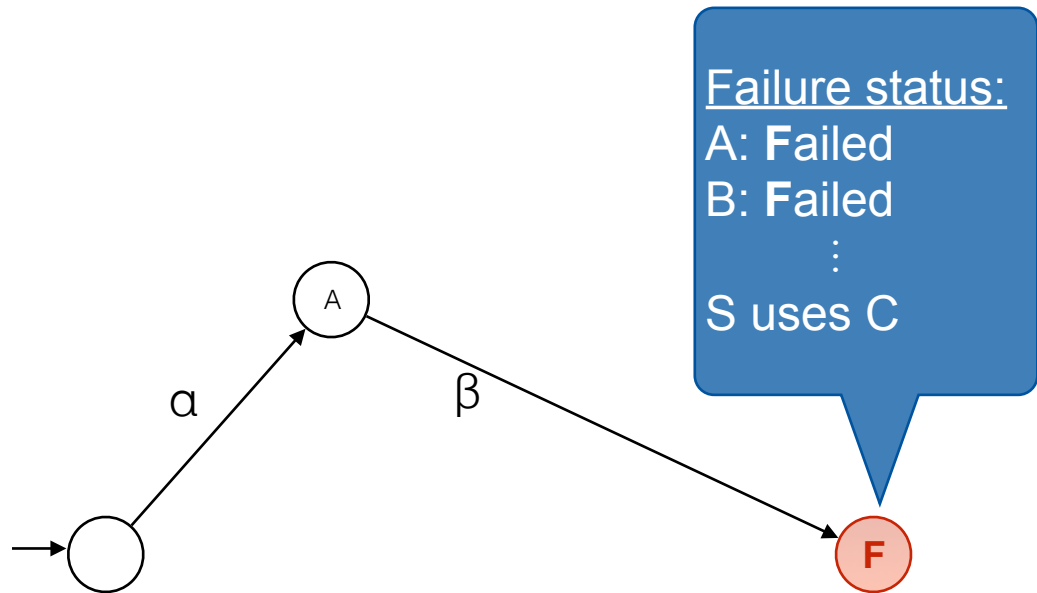
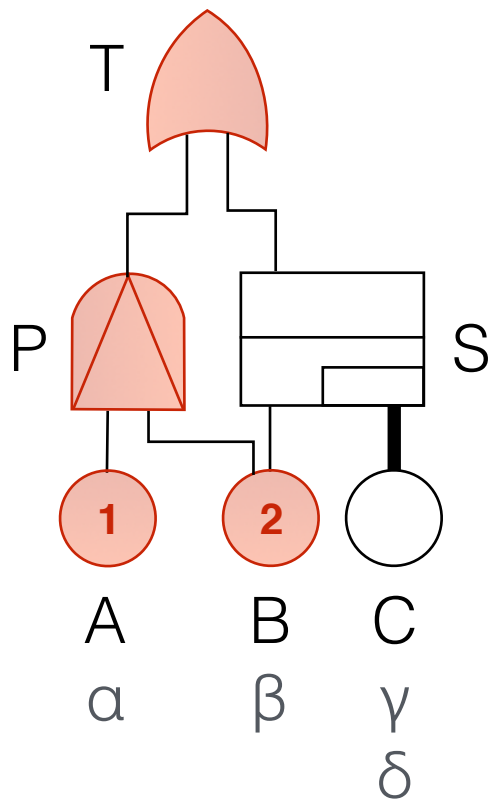
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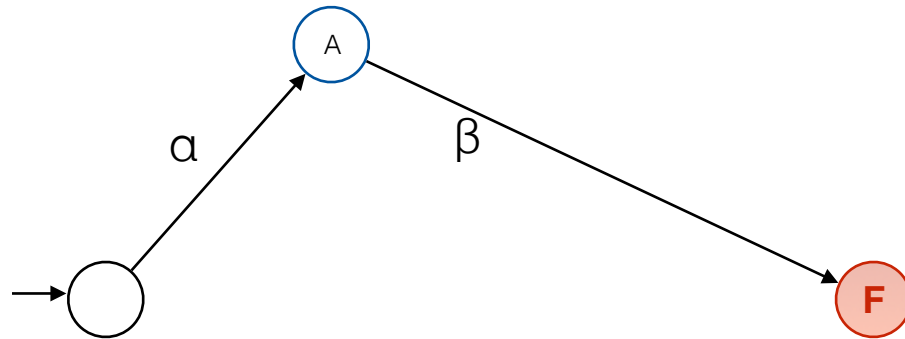
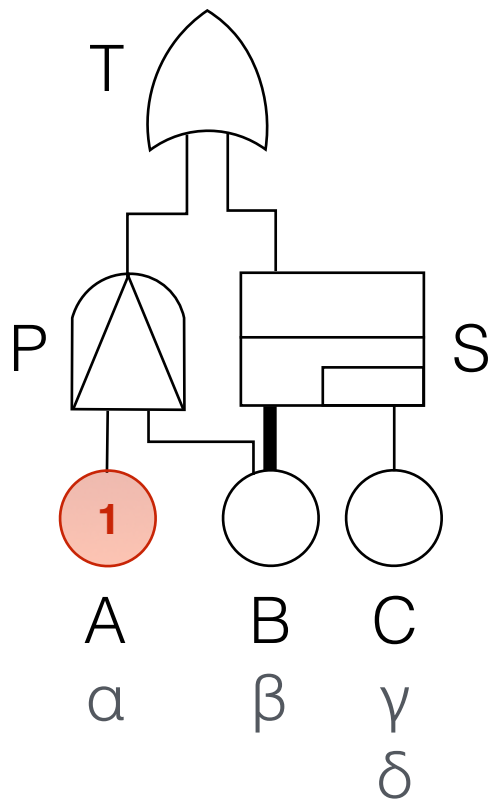
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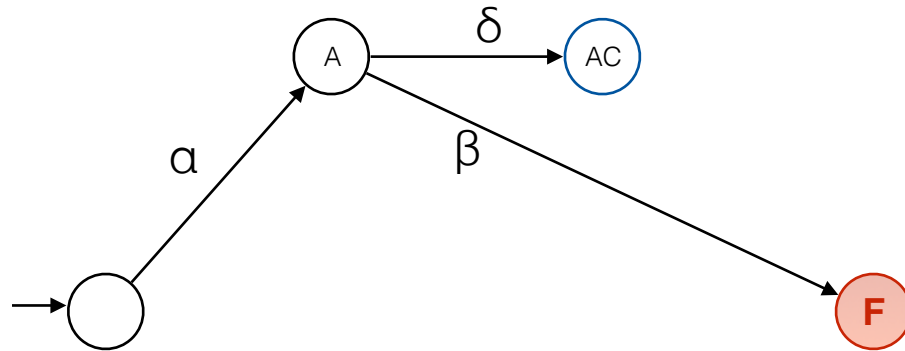
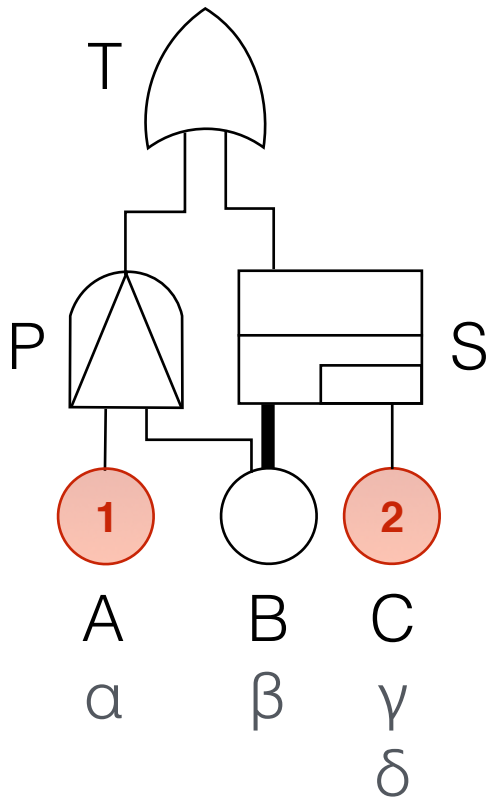
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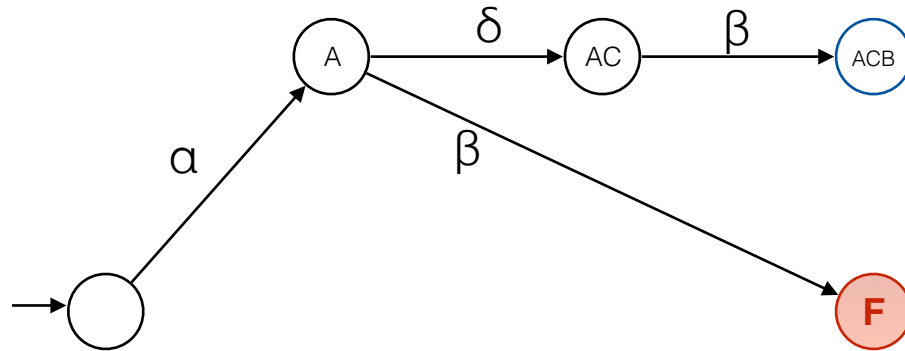
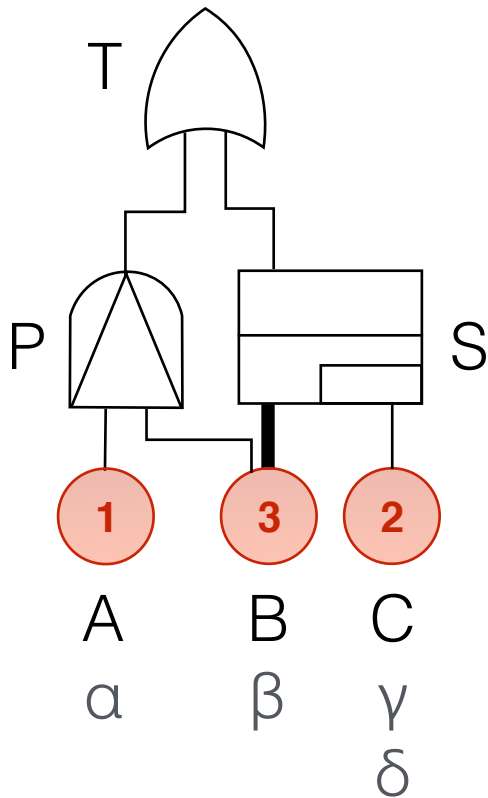
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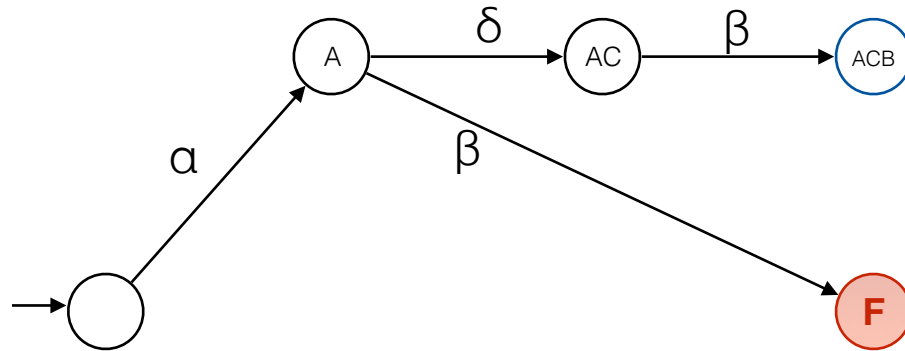
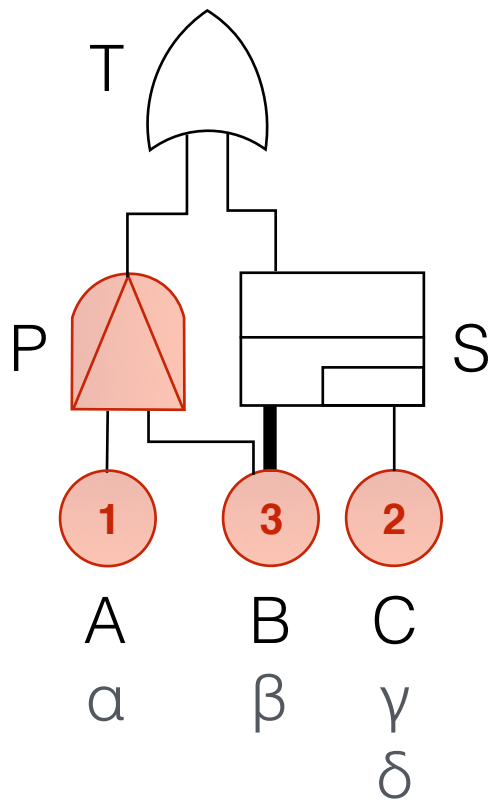
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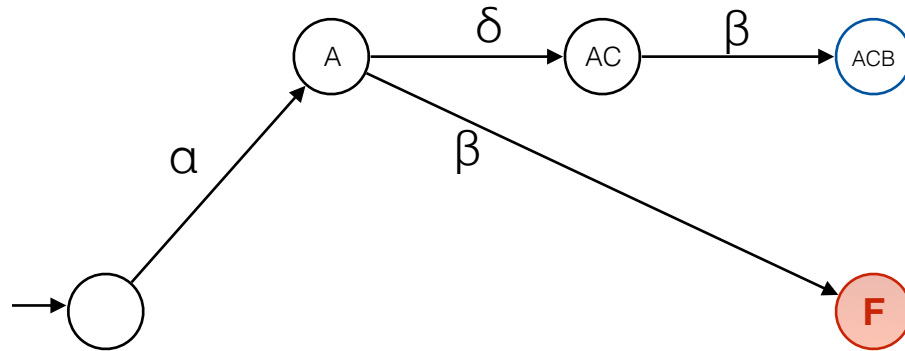
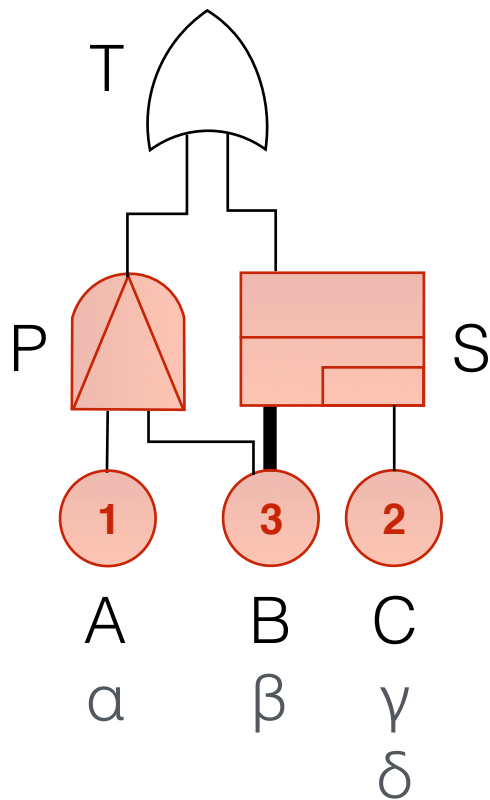
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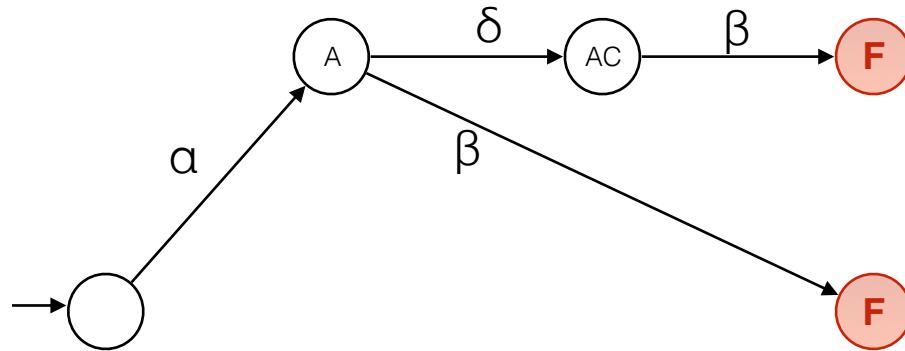
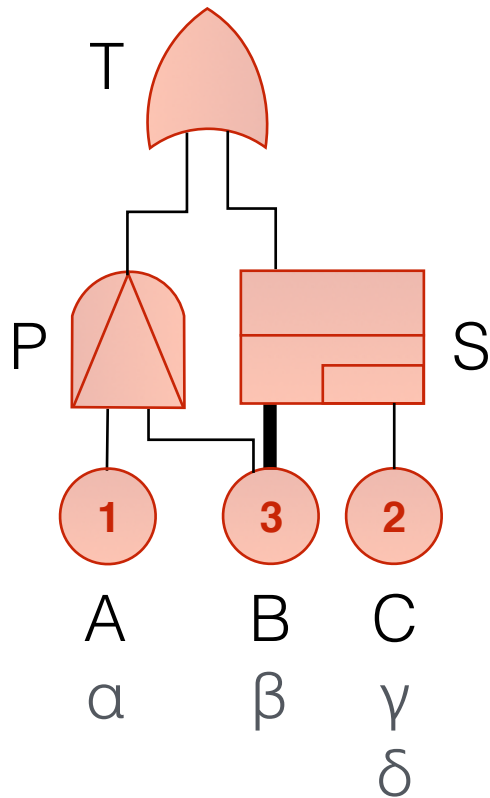
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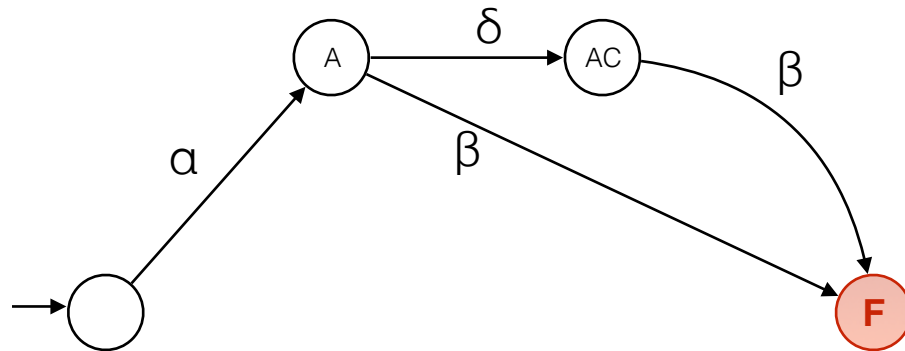
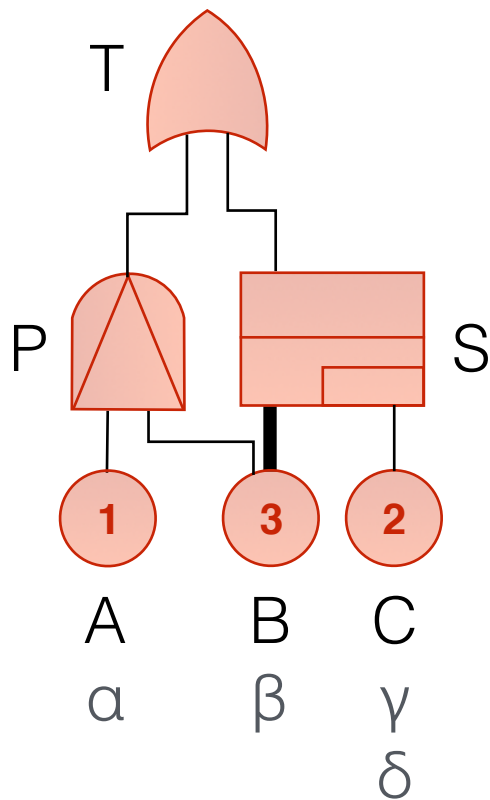
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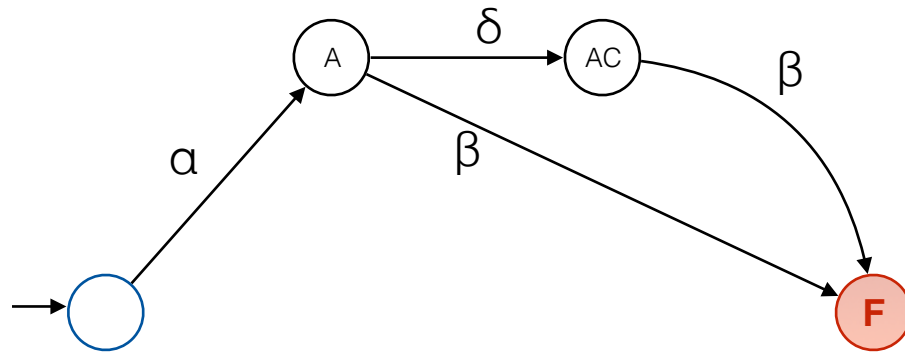
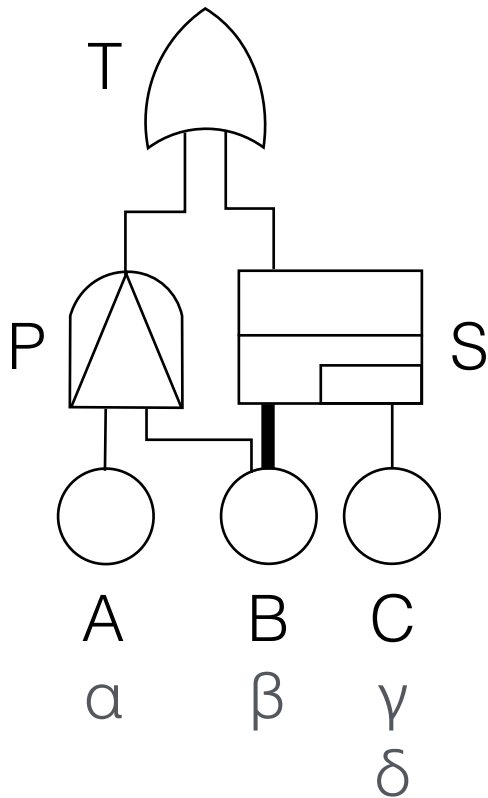
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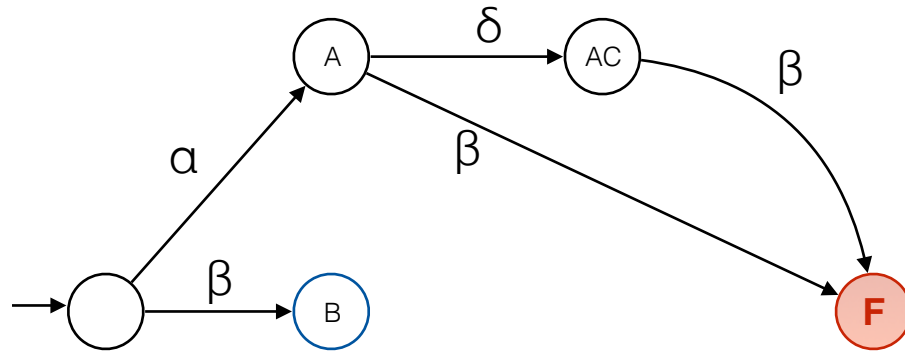
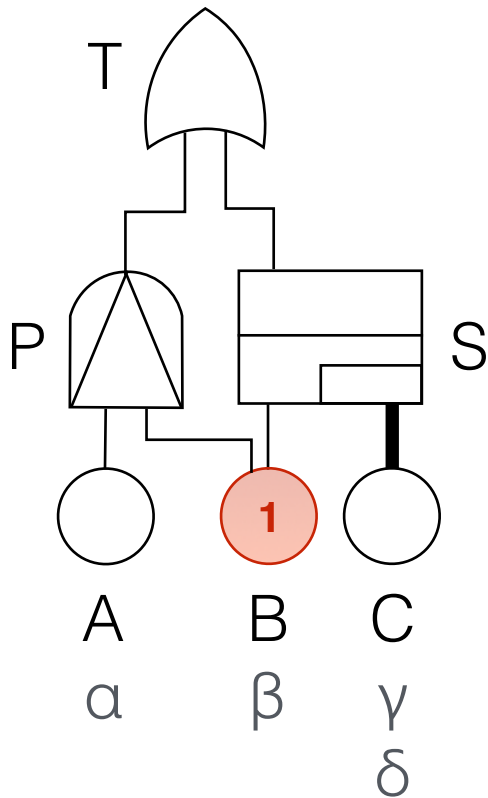
State space exploration



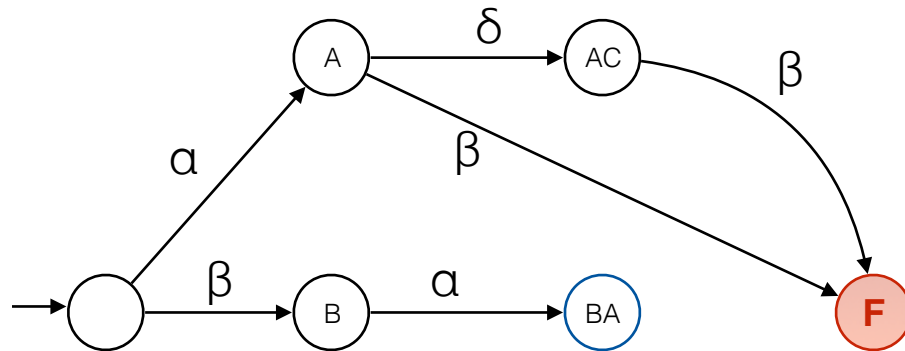
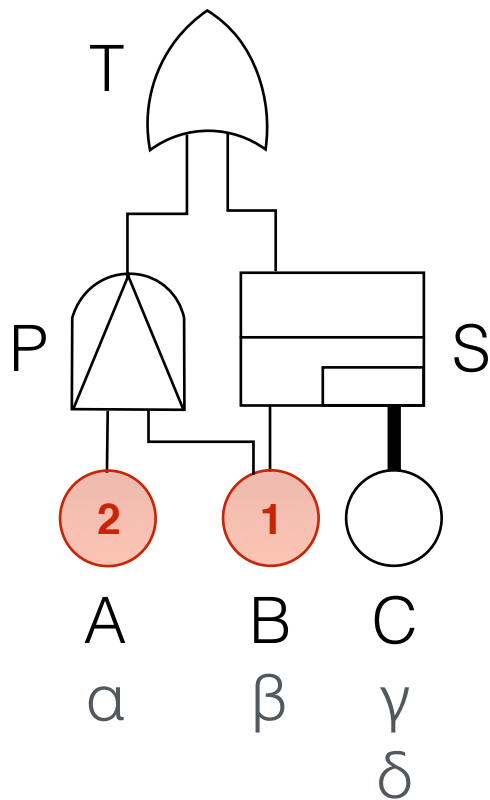
State space exploration



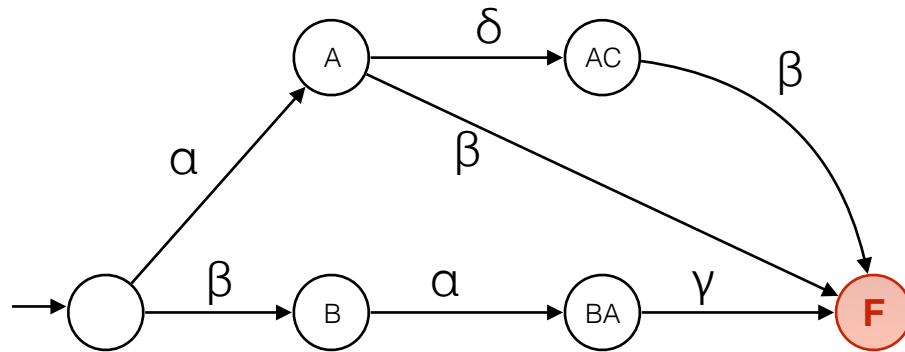
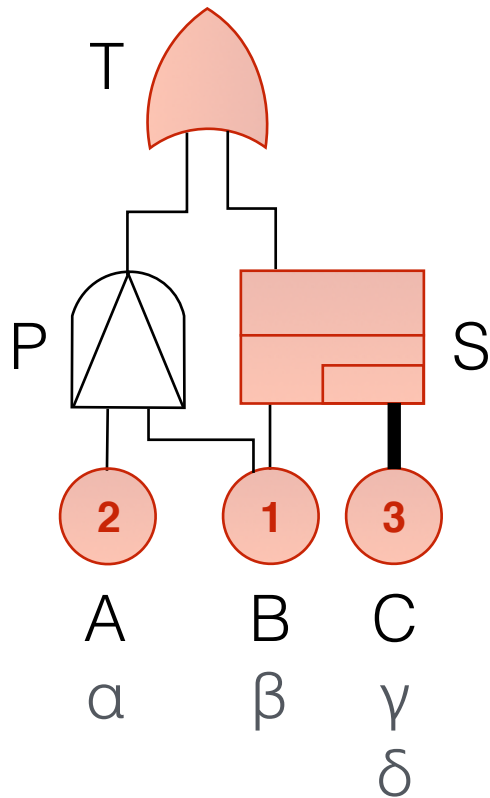
State space exploration



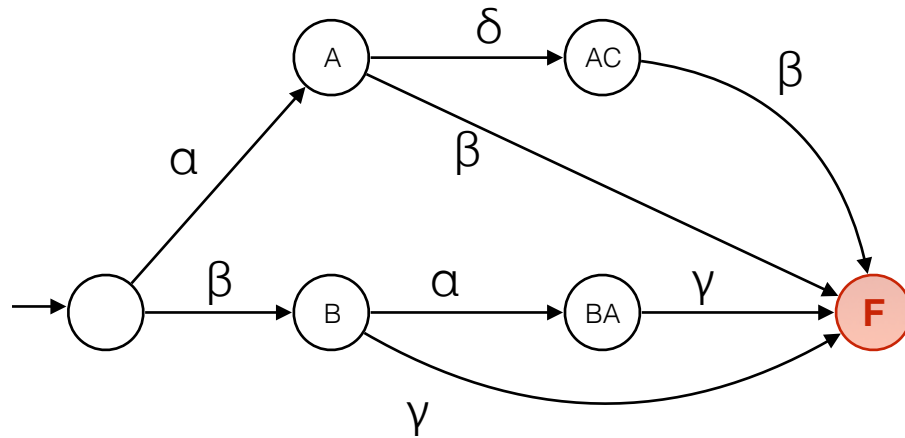
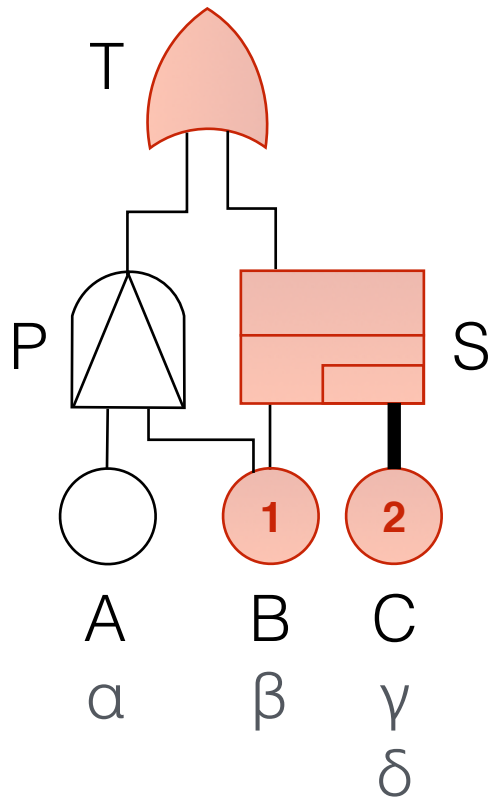
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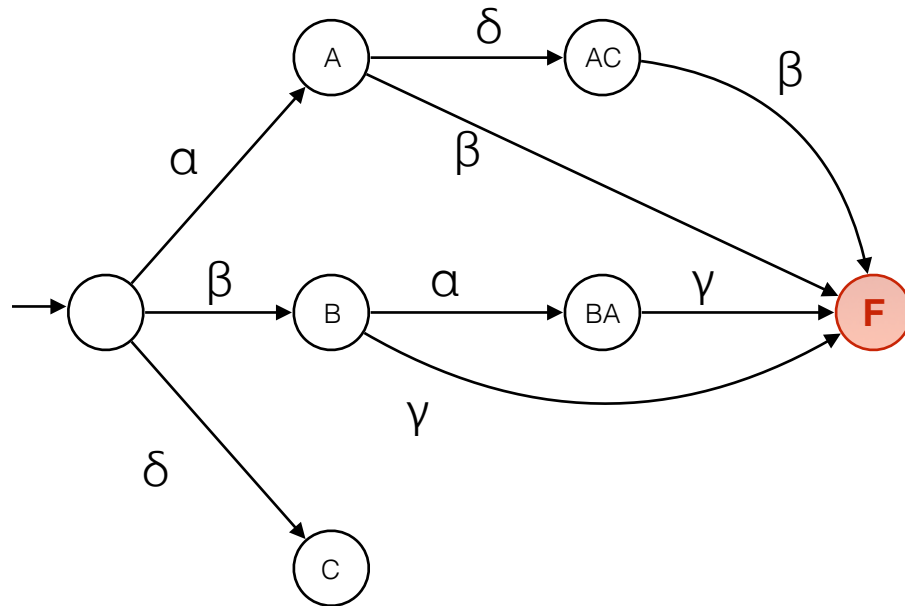
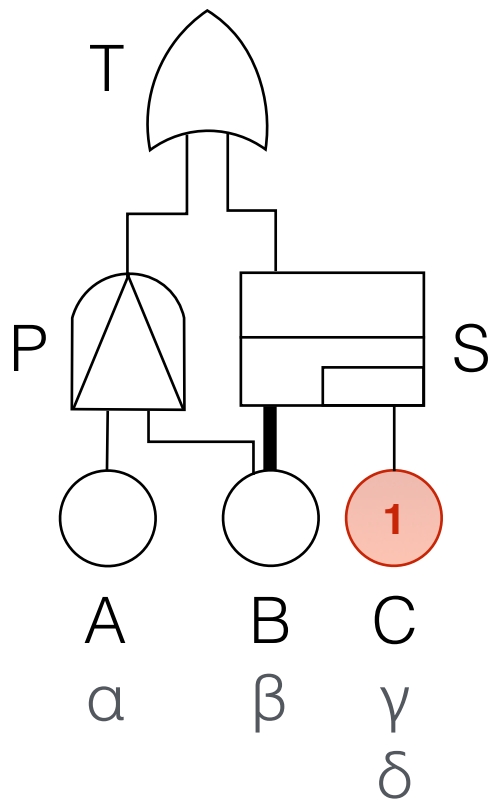
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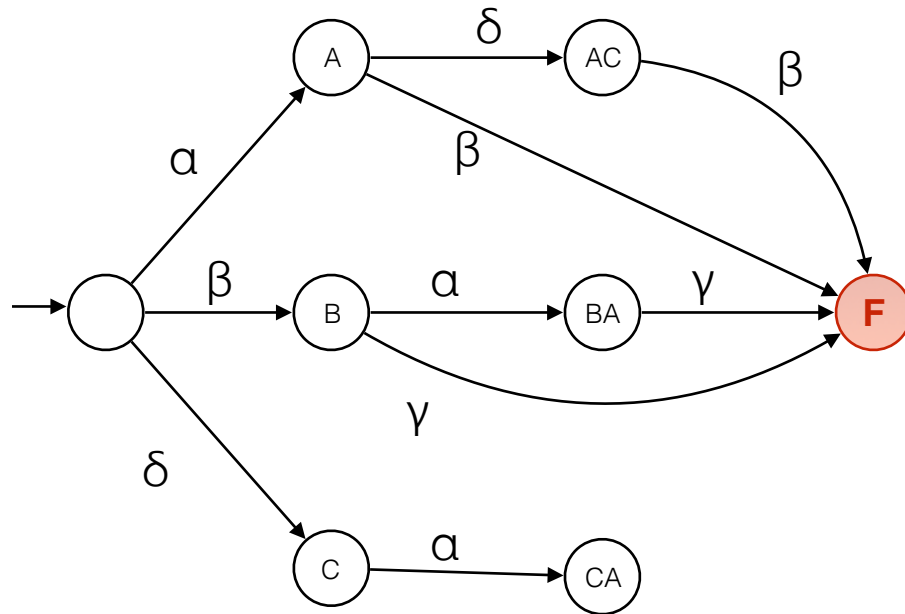
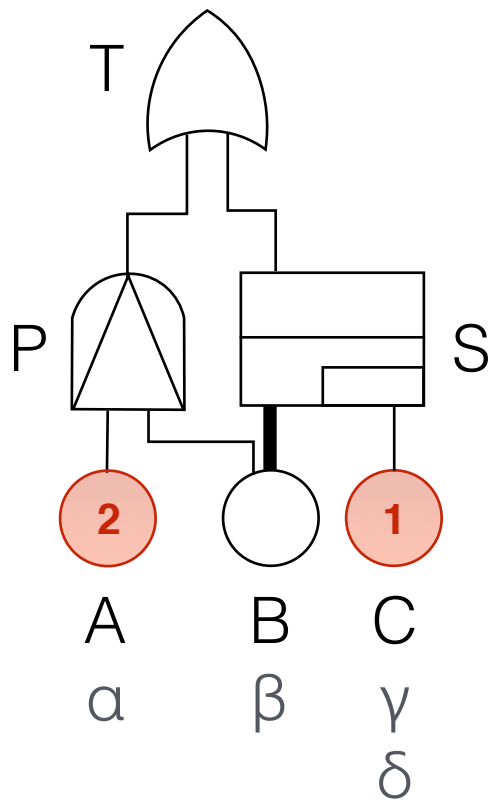
State space exploration



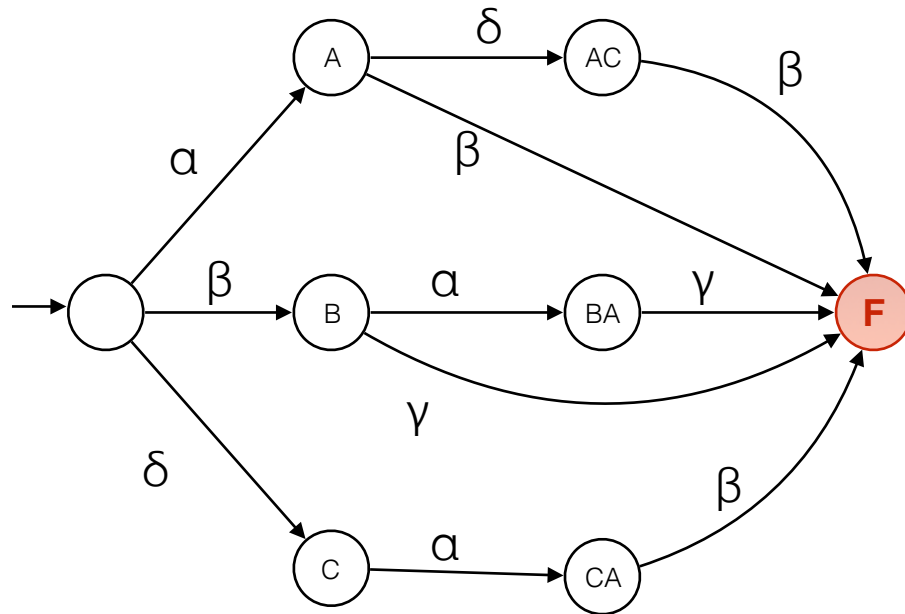
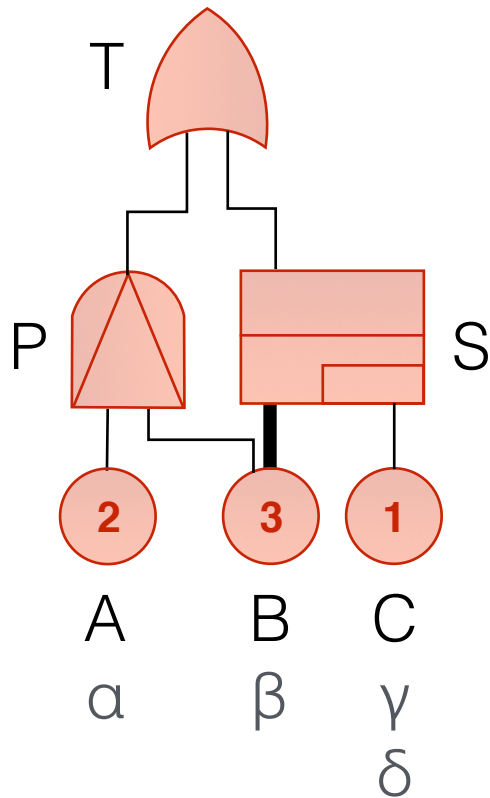
State space exploration



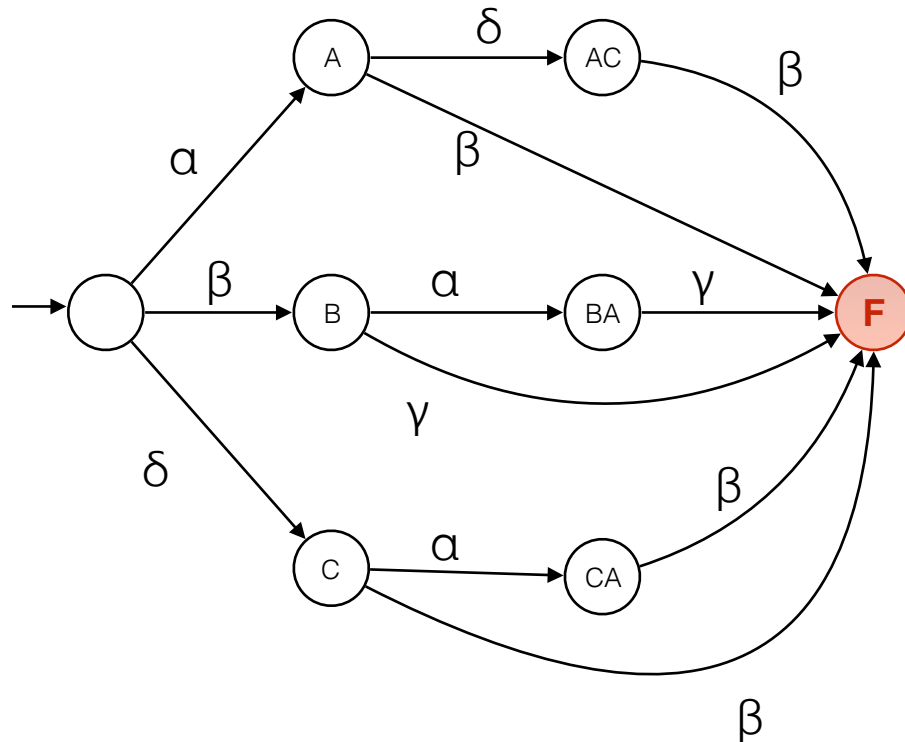
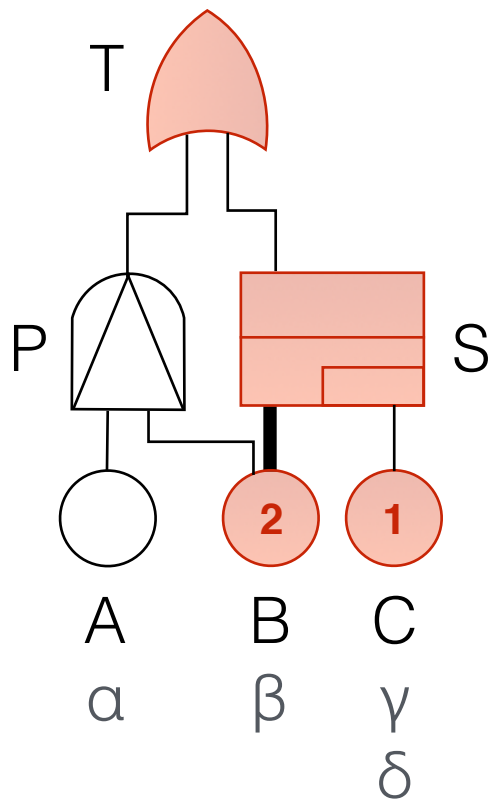
State space exploration



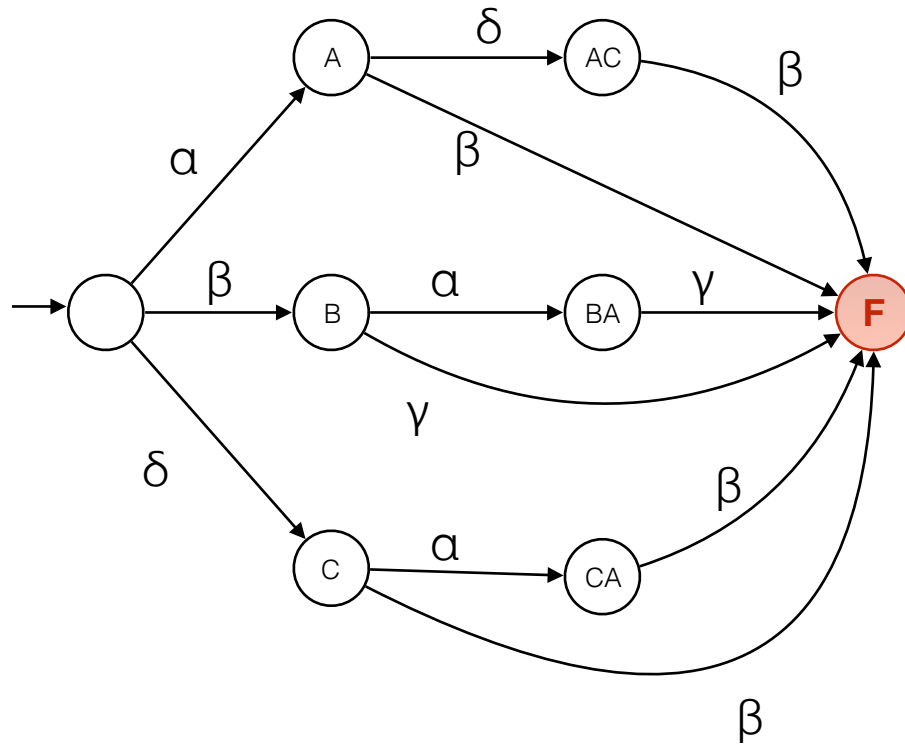
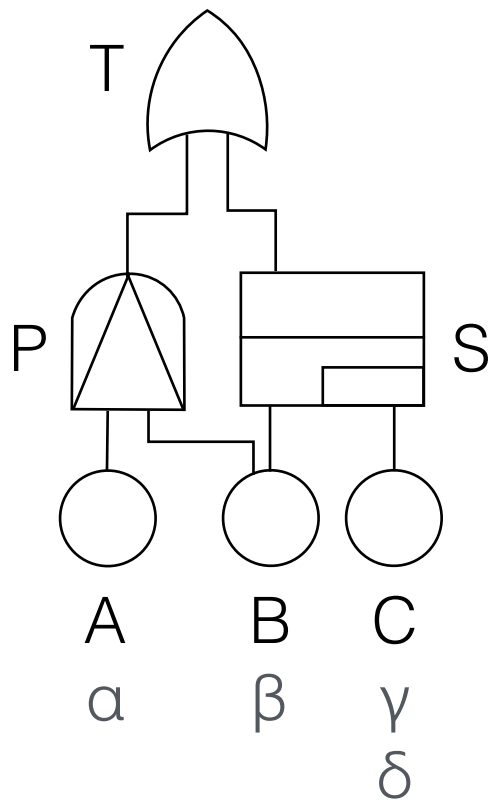
State space exploration



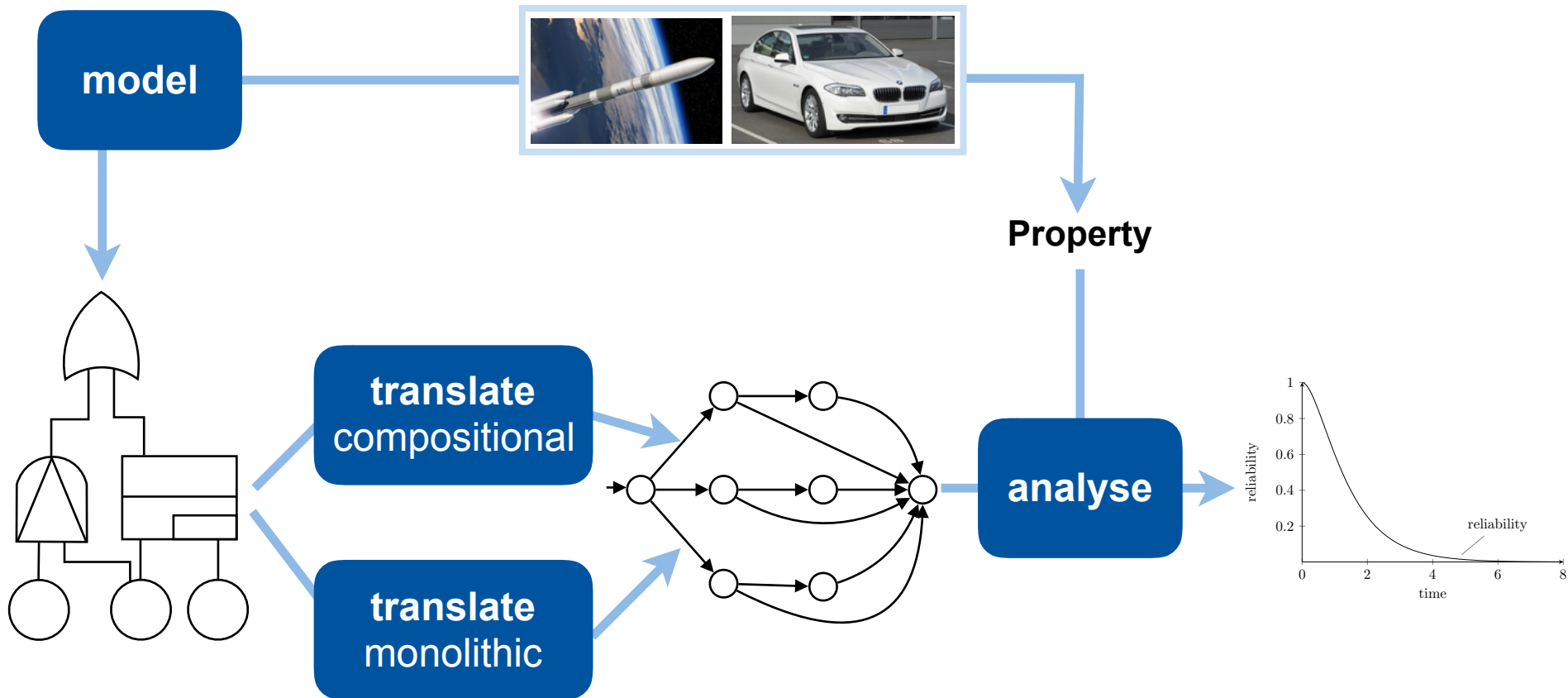
State space exploration



State space exploration



Overview



State space reduction techniques

Problem:
exponential state space size

Solution:
apply reduction techniques

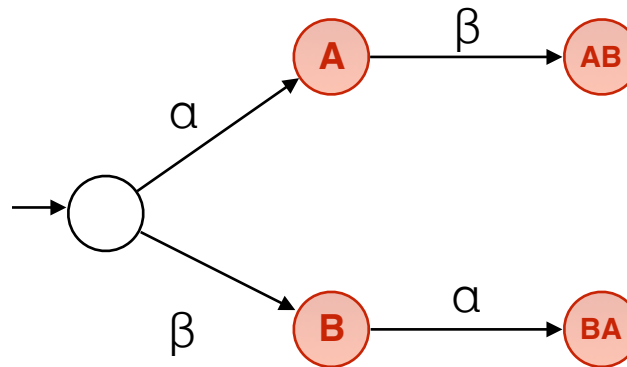
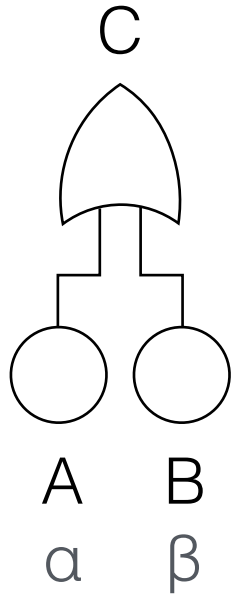
Solution:
apply reduction techniques

Reduction techniques:

- Bisimulation minimisation:
 - existing reduction technique for Markov chains
- Don't care propagation:
 - only consider failures making a difference
- Symmetry reduction:
 - exploit symmetric structures
- Modularisation:
 - compositional analysis for reliability

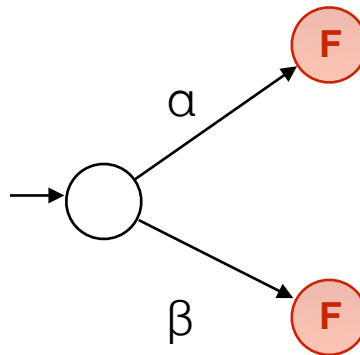
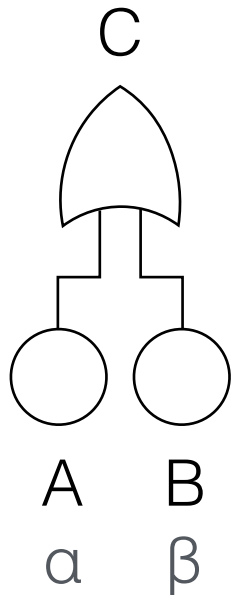
Don't care propagation

only consider failures making a difference



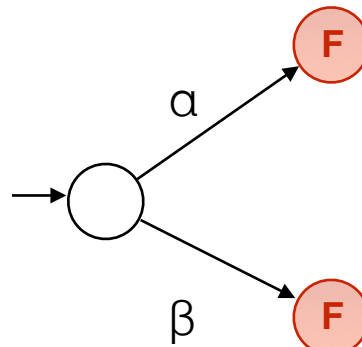
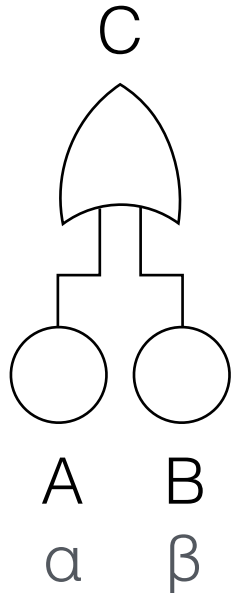
Don't care propagation

only consider failures making a difference



Don't care propagation

only consider failures making a difference

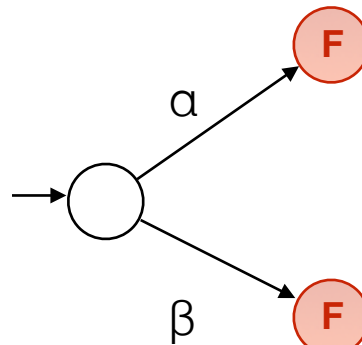
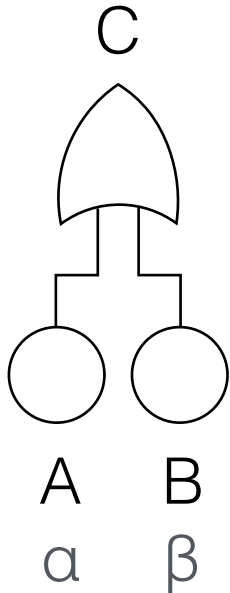


Failure status:
A: Failed
B: Operational
C: Failed

Failure status:
A: Operational
B: Failed
C: Failed

Don't care propagation

only consider failures making a difference



Failure status:

A: X

B: X

C: Failed

Failure status:

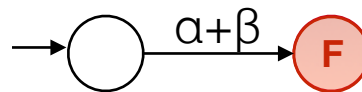
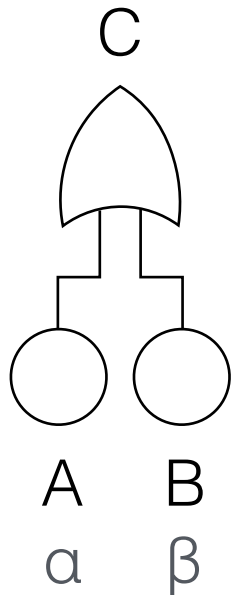
A: X

B: X

C: Failed

Don't care propagation

only consider failures making a difference



Failure status:

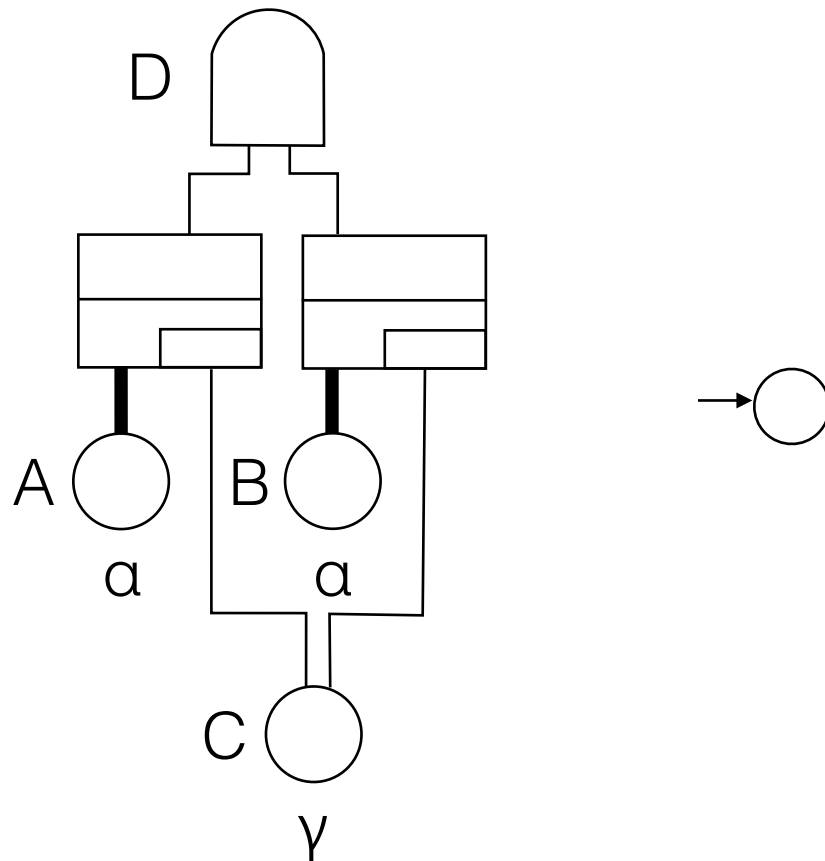
A: X

B: X

C: Failed

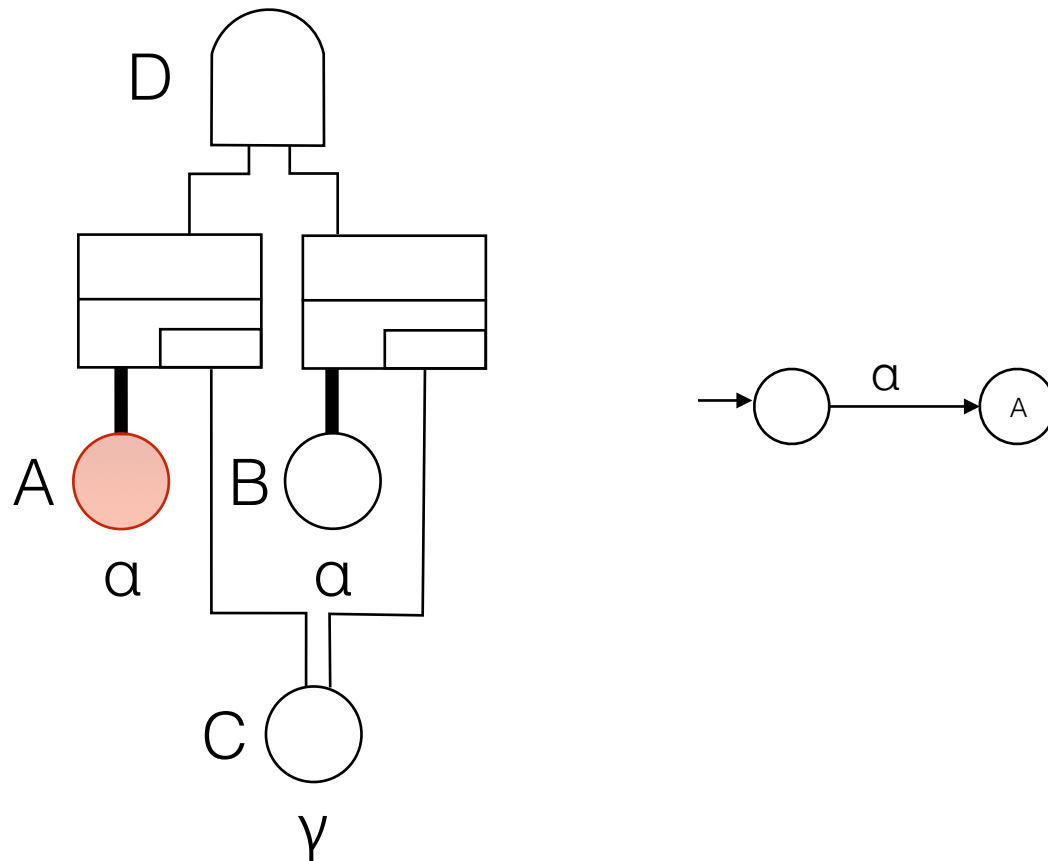
Symmetry reduction

exploit **symmetric structures**



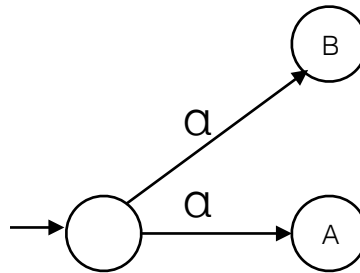
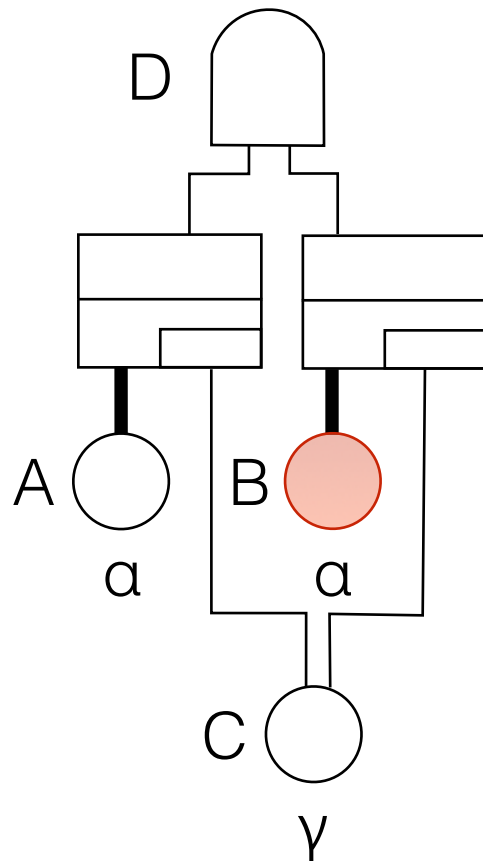
Symmetry reduction

exploit symmetric structures



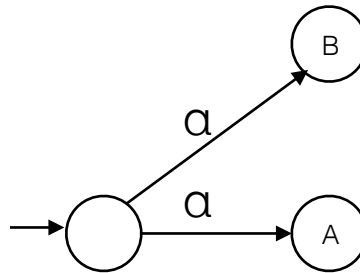
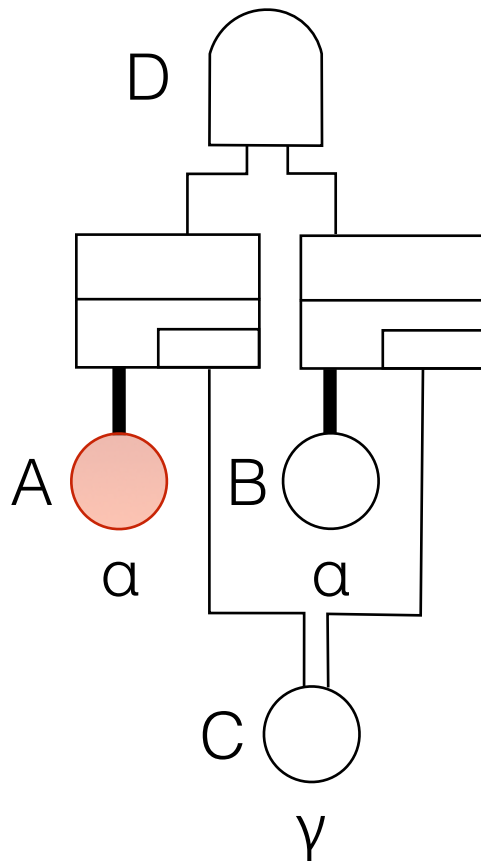
Symmetry reduction

exploit symmetric structures



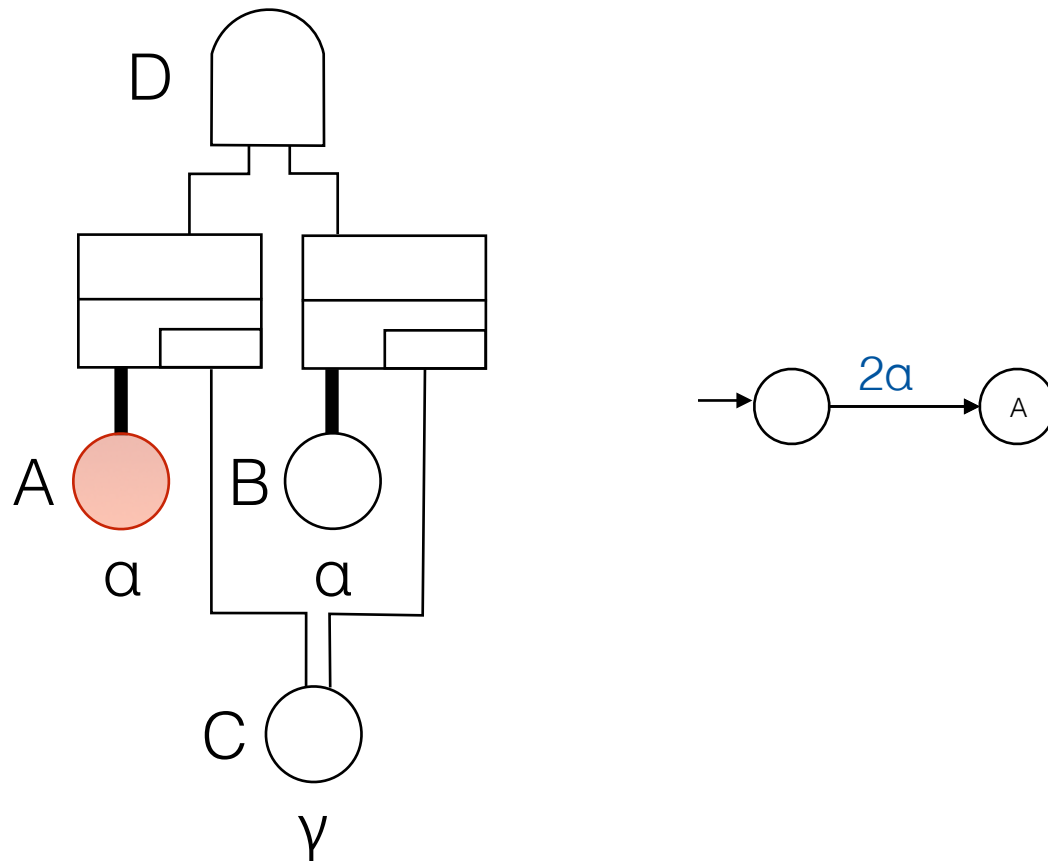
Symmetry reduction

exploit symmetric structures



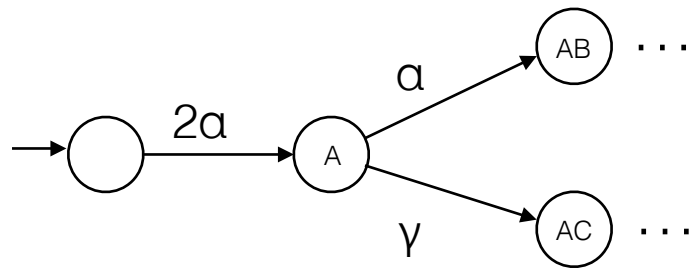
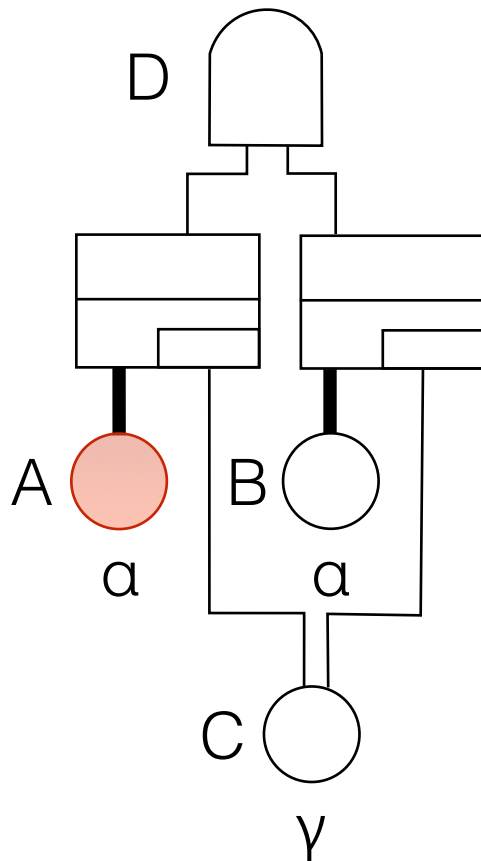
Symmetry reduction

exploit symmetric structures



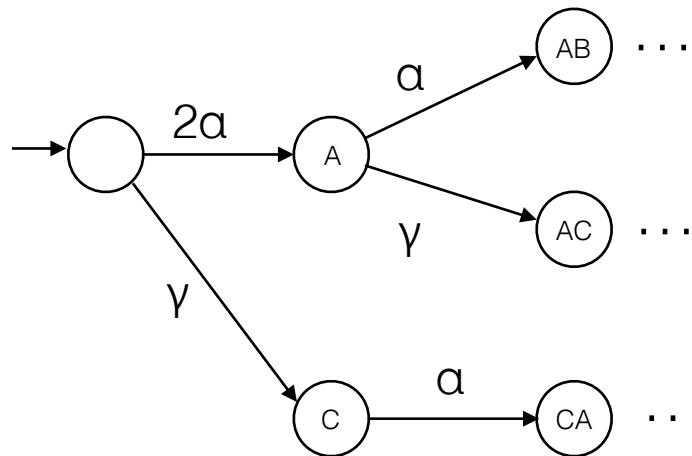
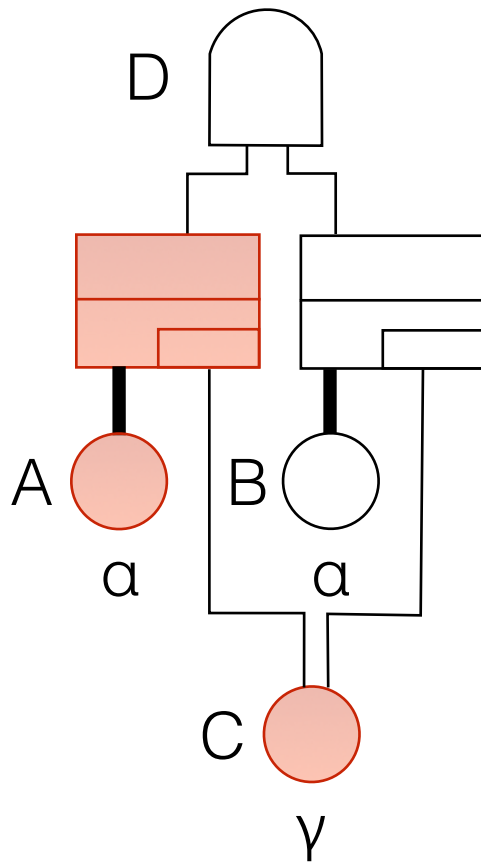
Symmetry reduction

exploit symmetric structures



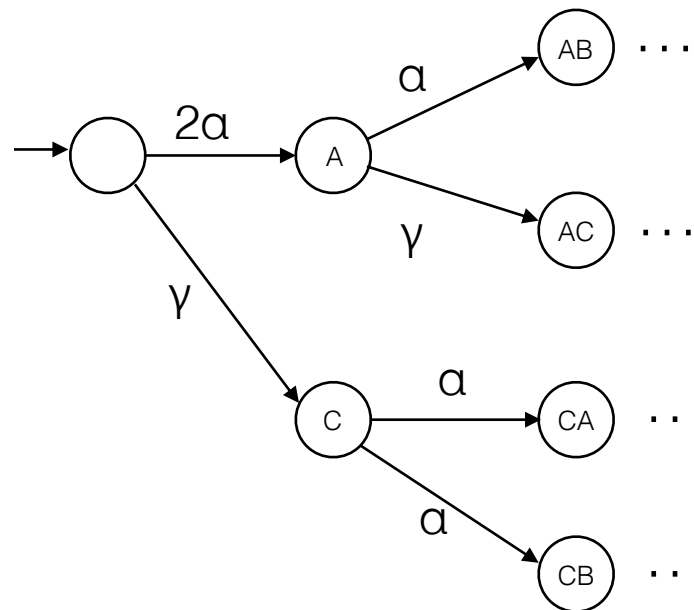
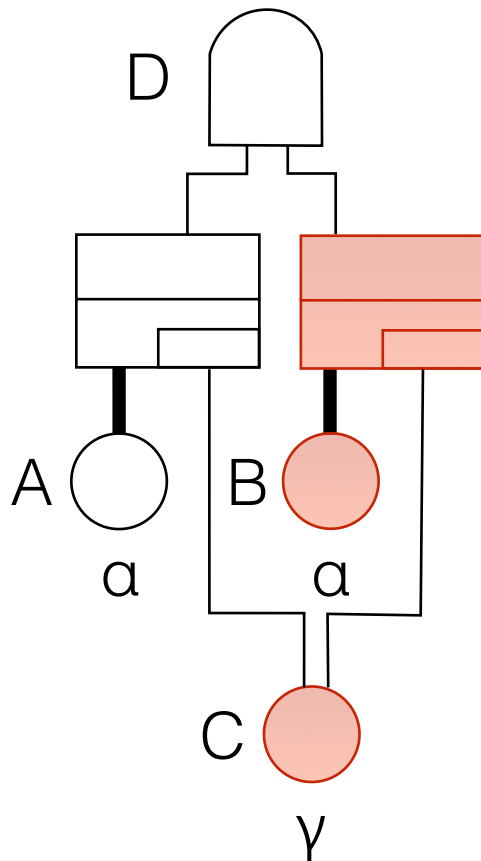
Symmetry reduction

exploit symmetric structures



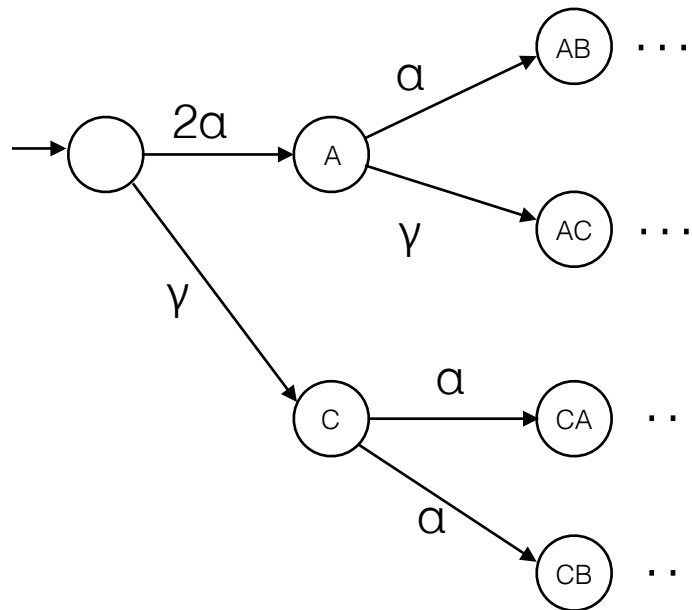
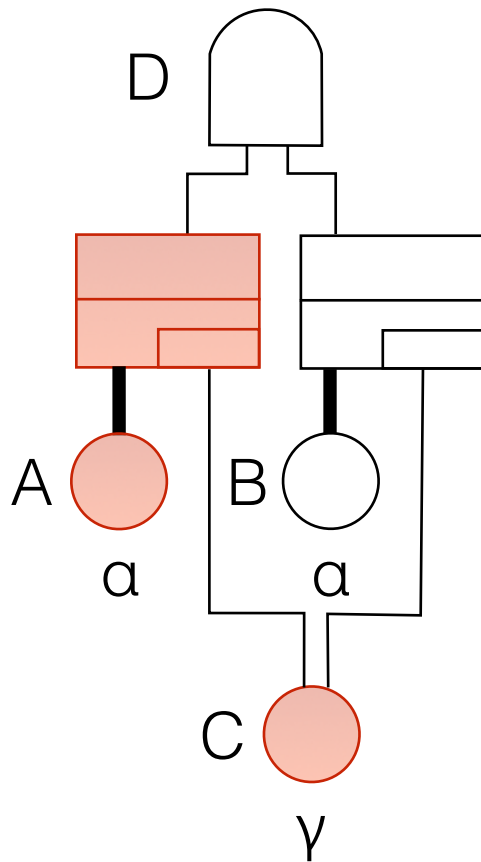
Symmetry reduction

exploit symmetric structures



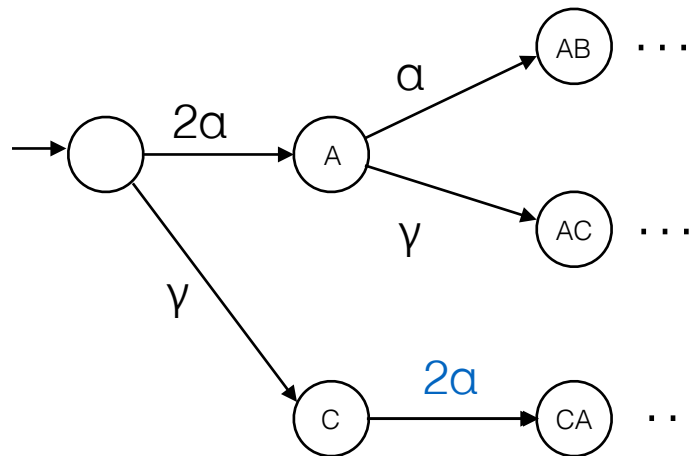
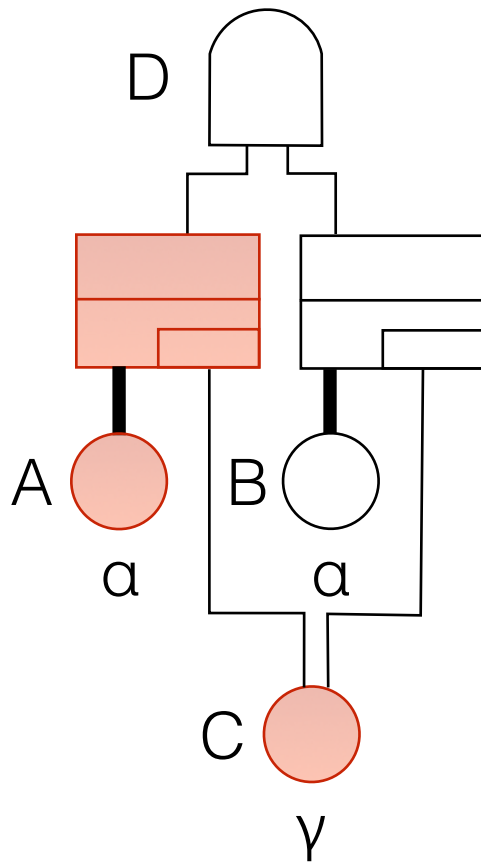
Symmetry reduction

exploit symmetric structures

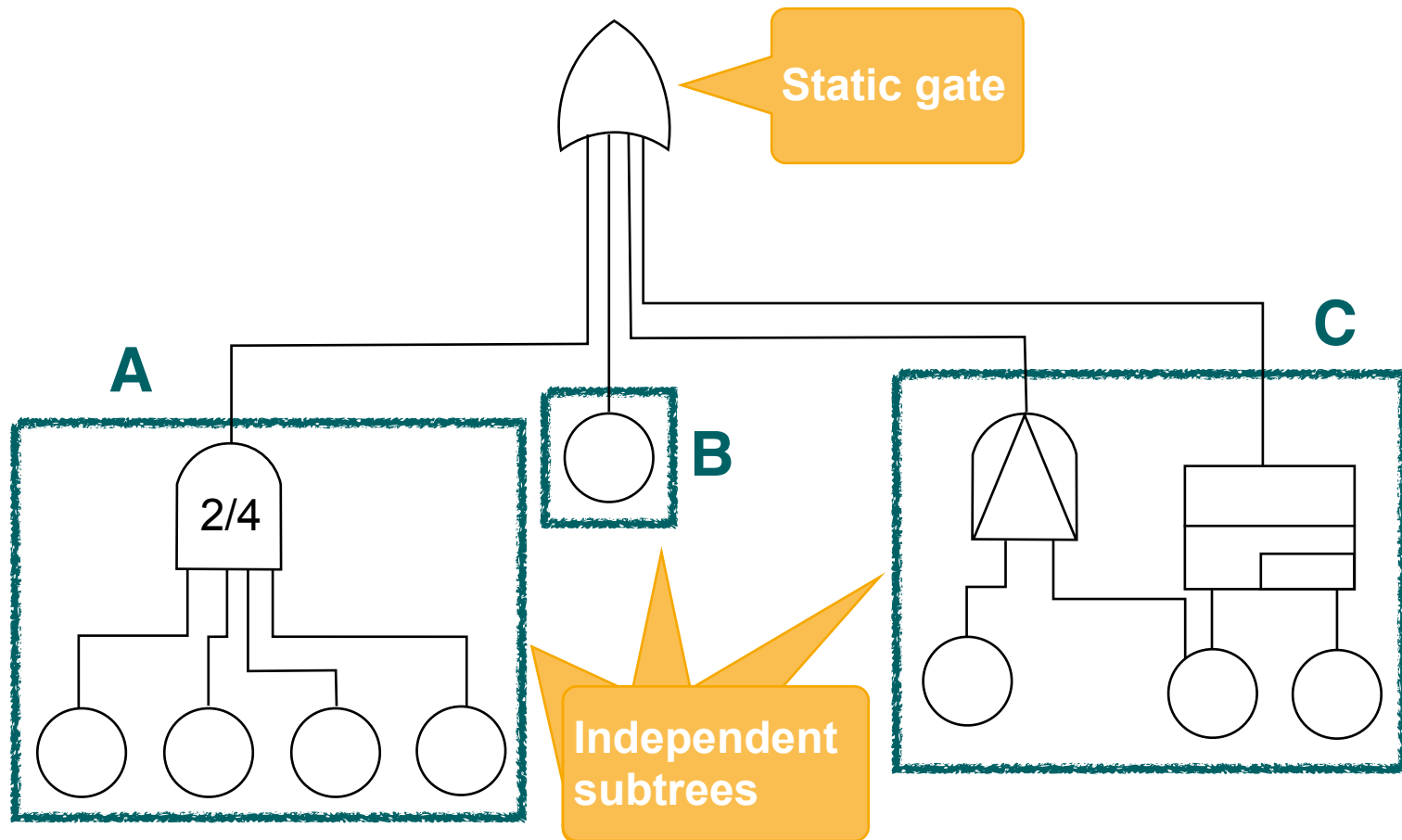


Symmetry reduction

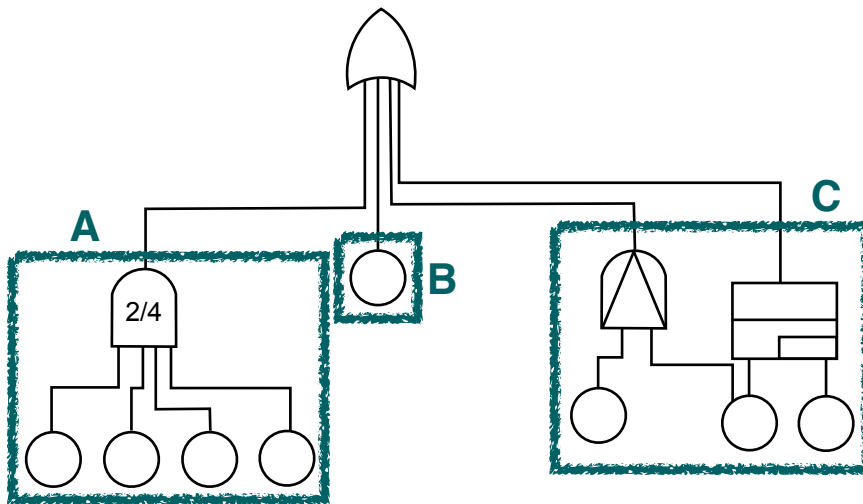
exploit symmetric structures



compositional analysis for reliability



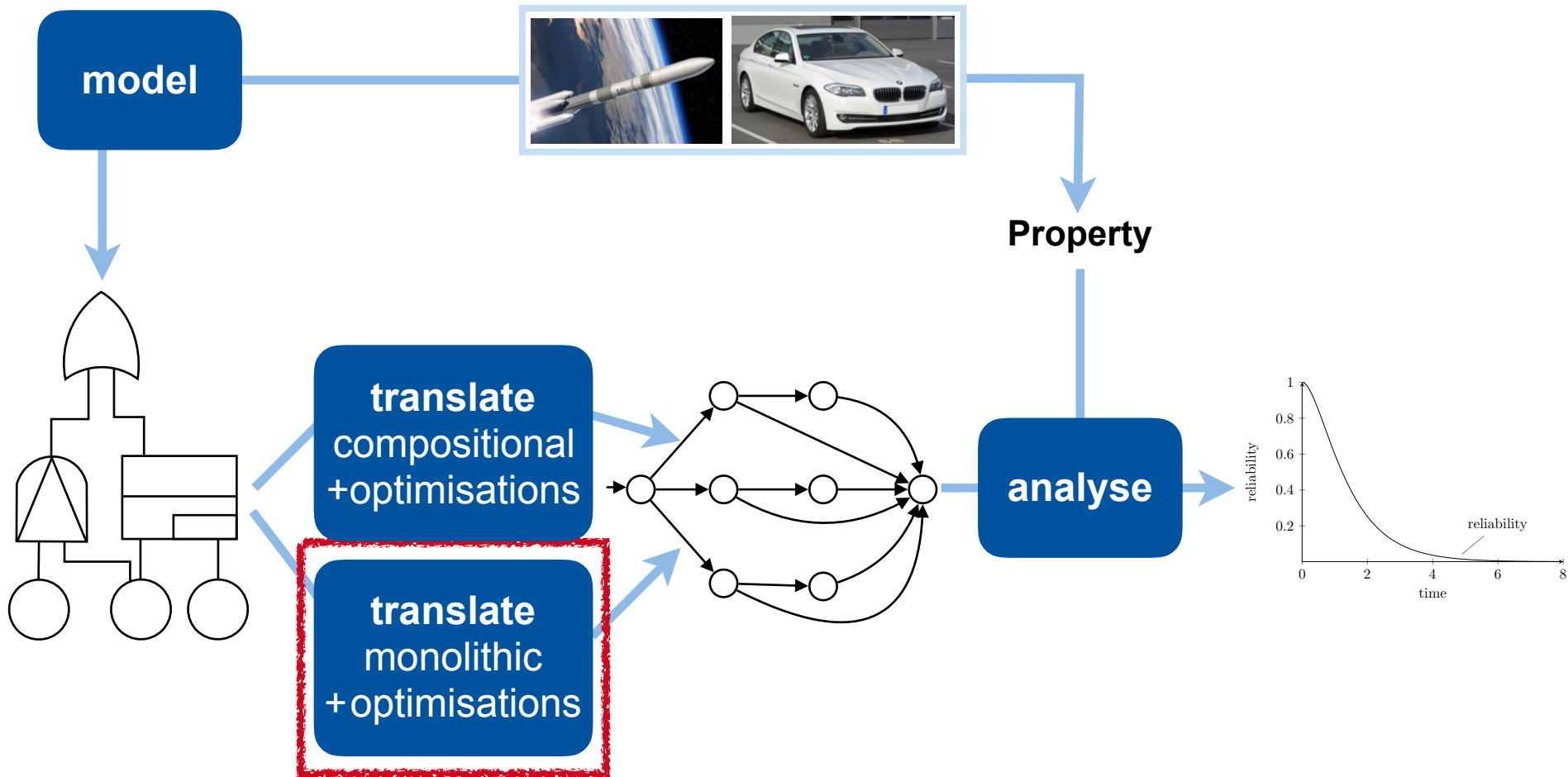
compositional analysis for reliability



1. Compute failure probability of A: p_A
2. Compute failure probability of B: p_B
3. Compute failure probability of C: p_C
4. Compute complete probability:

$$1 - (1-p_A)(1-p_B)(1-p_C)$$

Overview



Experimental evaluation



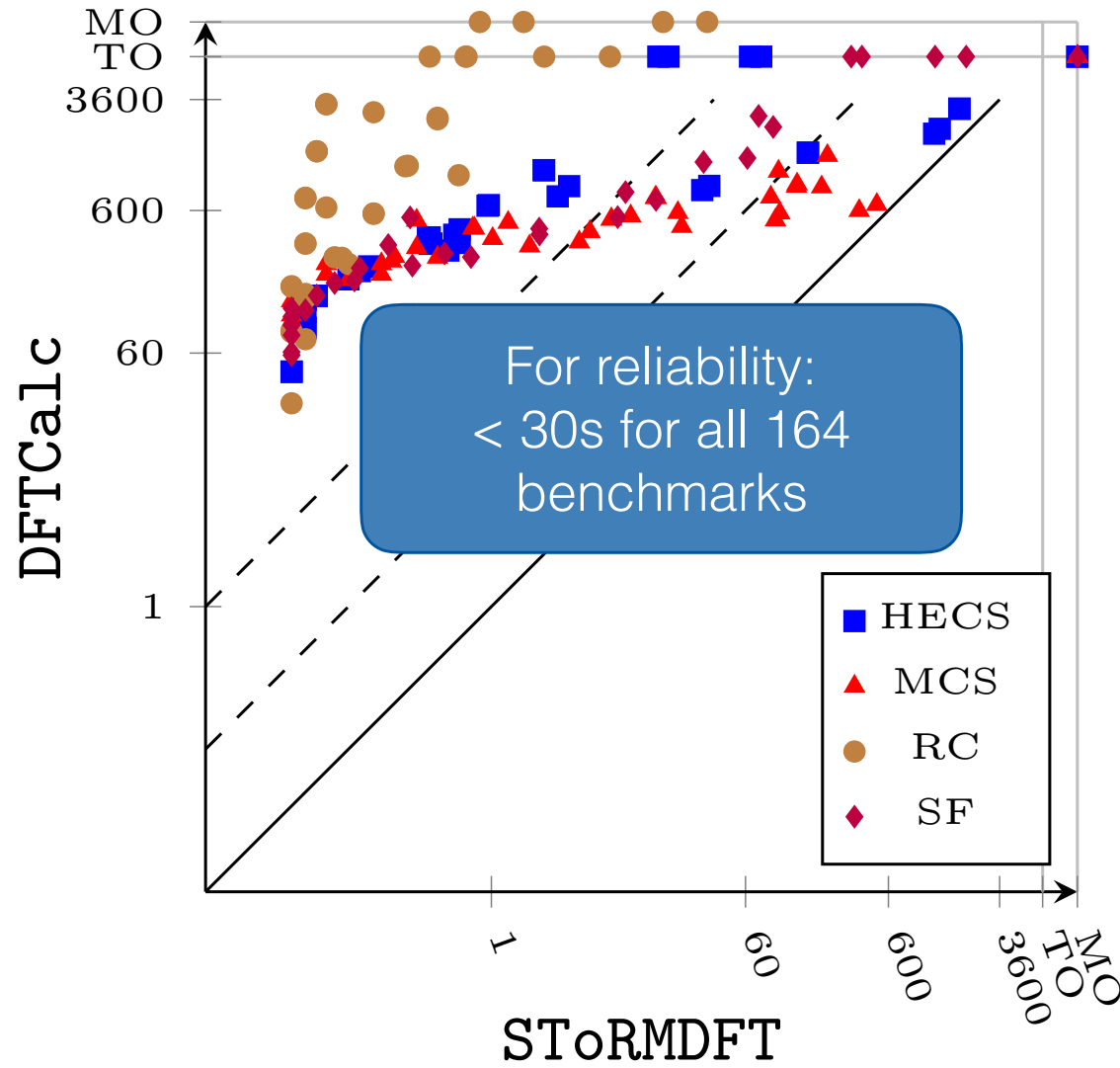
<http://www.stormchecker.org>

Experimental evaluation

- Comparison to compositional approach ([DFTCalc](#))
- 4 sets of benchmarks (164 DFTs in total):
 - [HECS](#) (Hypothetical Example Computer System)
 - [MCS](#) (Multiprocessor Computing System)
 - [RC](#) (Railway Crossing)
 - [SF](#) (Sensor Filter)
- largest DFT: over 120 BEs
- mostly: 50-60 BEs
- Machine: 2,0 GHz, 8 GB RAM, 1 hour

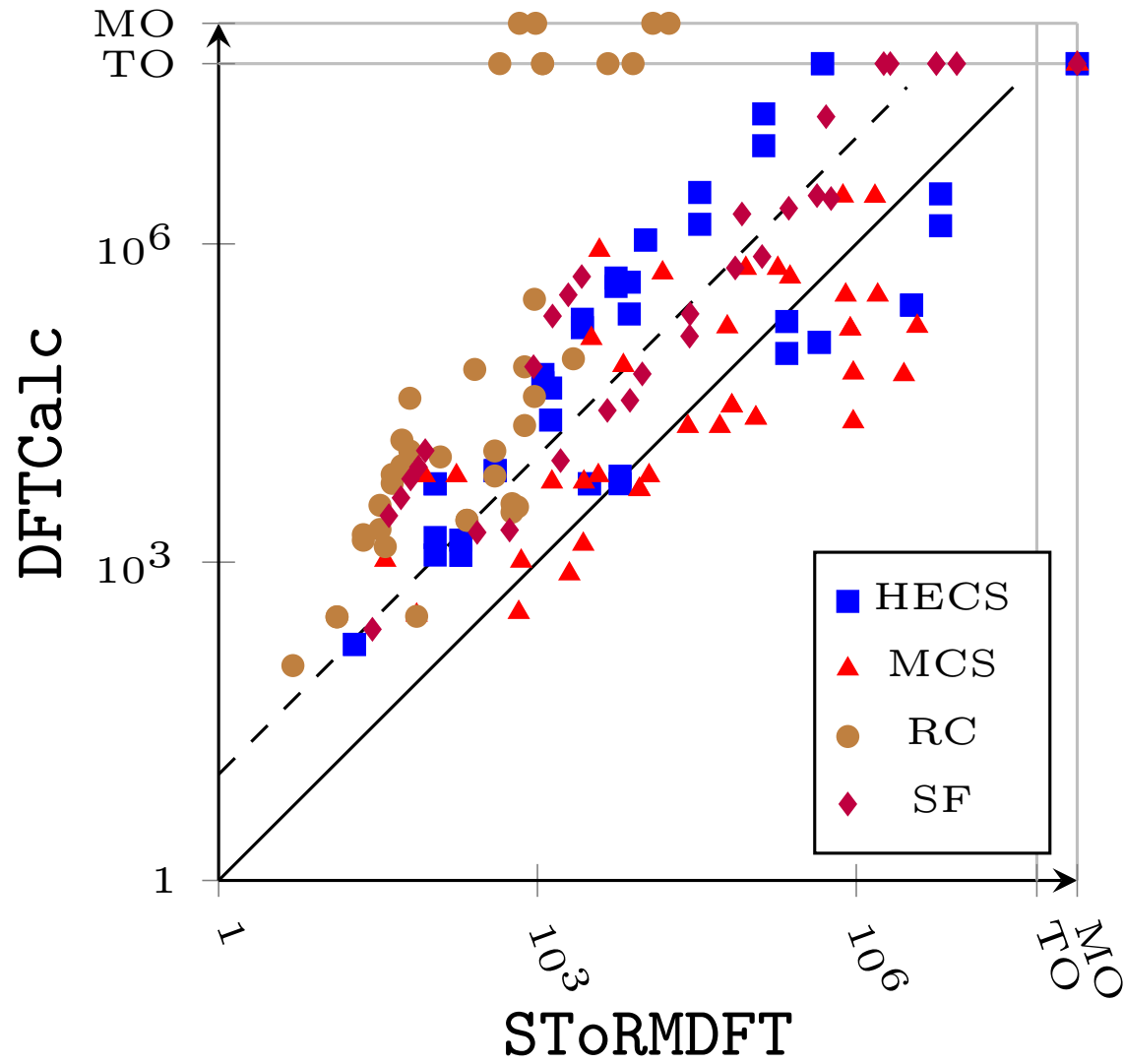
Analysis run times for MTTF

[Volk et al., SAFECOMP 2016]



Max. number of states during exploration

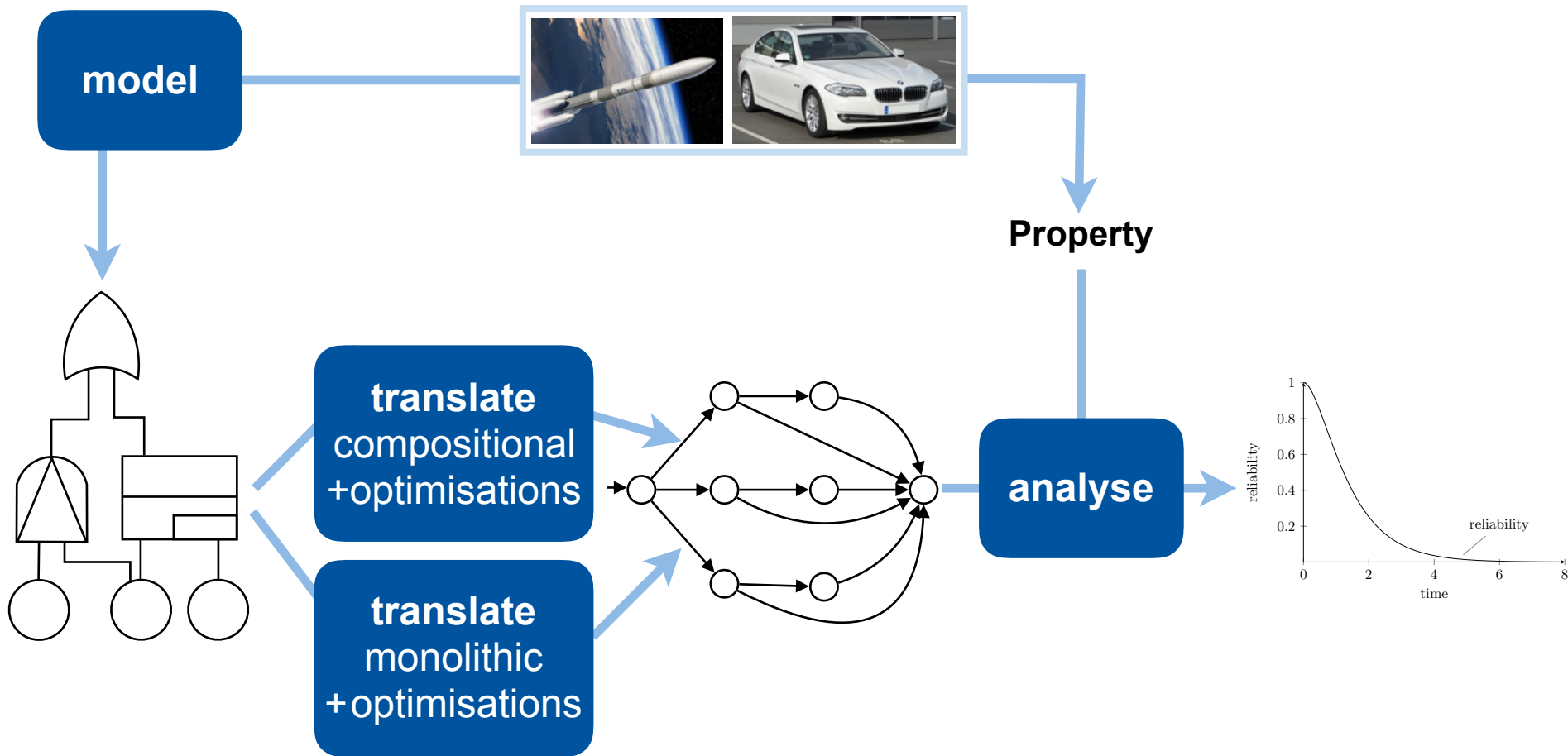
[Volk et al., SAFECOMP 2016]



		Reliability				MTTF			
		DFTCalc		SToRMDFT		DFTCalc		SToRMDFT	
		#	Time	#	Time	#	Time	#	Time
HECS	42	38	27517,06s	42	3,07s	36	25580,93s	40	6973,02s
MCS	42	40	21342,25s	42	20,80s	38	18671,74s	38	2079,08s
RC	38	29	27495,17s	38	2,09s	29	27386,01s	38	65,09s
SF	30	26	16137,67s	30	1,82s	25	13825,36s	29	4390,85s
CAS	8	8	1301,41s	8	0,36s	8	1299,89s	8	0,37s
SAP	4	4	357,64s	4	0,30s	4	316,02s	4	0,16s

		Reliability					MTTF
		no opti.	Sym. Red.	Don't Care	Modular.	all	all (SR+DC)
HECS₂	time	30,3s	15,6s	1,1s	0,05s	0,04s	0,61s
	max. states	864.001	432.073	11.881	4	4	5.995
MCS₂	time	337,8s	46,0s	1,1s	0,05s	0,05s	0,21s
	max. states	10.469.377	1.374.946	17.689	67	37	2.701
RC₁₀	time	53,6s	0,1s	53,5s	0,20s	0,05s	0,07s
	max. states	1.048.577	122	1.048.577	3	3	122
SF_{6,2}	time	22,1s	7,4s	0,3s	0,04s	0,04s	0,08s
	max. states	1.132.097	355.111	2.602	4	4	919

Overview



A Modern Perspective on Fault Tree Analysis

Joost-Pieter Katoen and Matthias Volk



*Joint work with: Majdi Ghadhab (BMW), Dennis Guck (TWT),
Sebastian Junges (RWTH), Matthias Kuntz (BMW),
Enno Ruijters (U. Twente) and Mariëlle Stoelinga (U. Twente)*

Tutorial MMB 2018, Erlangen, BY

Roadmap of This Tutorial

Part 1. What are Dynamic Fault Trees?

- DFT Elements, Benchmarks, Intricacies, DFTs as Stochastic Petri Nets

Part 2. From DFTs to Markov Models, Compositionally

- Compositional State-Space Minimisation, Non-Determinacy

Part 3. From DFTs to Markov Models, Monolithically

- Symmetry Reduction, Don't Care Propagation

Part 4. DFT Analysis by Model Checking

- Reliability Measures, Core Algorithms, Storm Tool

Part 5. Advanced Optimisations

- Graph Rewriting, Partial State-Space Generation

Part 6. Industrial Applications and Outlook

Focus is on conveying intuition and experimental results

Overview

Part 4: DFT Analysis by Model Checking

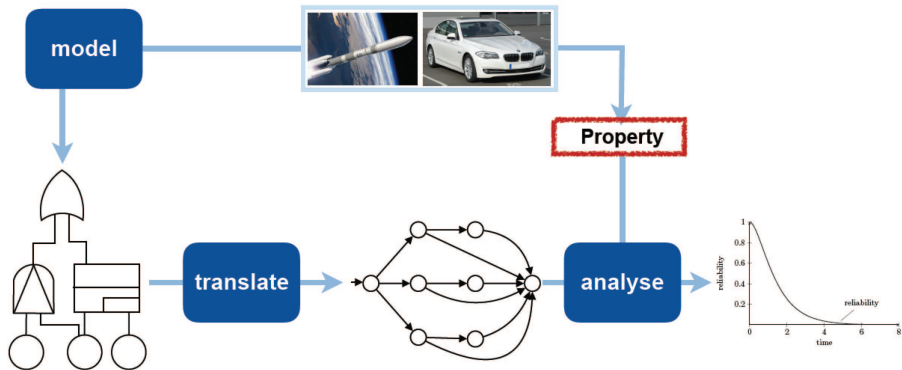
- Reliability Measures

- Probabilistic Model Checking

- Core PMC Algorithms

- PMC Tools

Graphical Overview

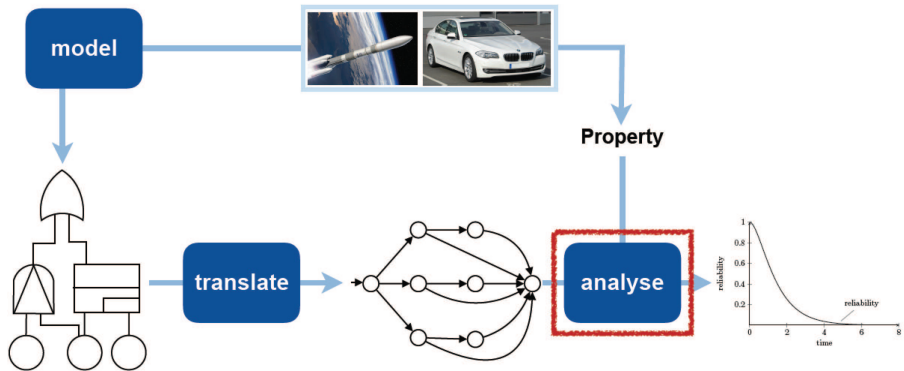


Reliability Measures

[Barlow and Proschan, 1985]

- ▶ The **reliability** of DFT F is the probability that the system it represents operates for a certain amount of time without failing.
- ▶ The **availability** at time t is the probability that the system is functioning at a given time.
 - ▶ Availability of **interval** $[t, t']$ is the fraction of $[t, t']$ in which the system is operational
 - ▶ For repairable DFTs, also the **long-run** availability is considered
- ▶ The **Mean Time To Failure (MTTF)** is the expected time from the moment the system becomes operational, to the moment the system subsequently fails.
- ▶ For repairable systems, the **Mean Time Between Failure (MTBF)** denotes the mean time between two successive failures

Graphical overview



Probabilistic Model Checking

“A promising new direction in formal methods research these days is **probabilistic model checking**, with associated tools for **quantitative evaluation of system performance along with correctness.**”

Theory in Practice for System Design and Verification



Rajeev Alur
Univ. of Pennsylvania



Thomas A. Henzinger
IST Austria



Moshe Y. Vardi
Rice University

ACM SIGLOG News 2015

Model Checking and ISO 26262

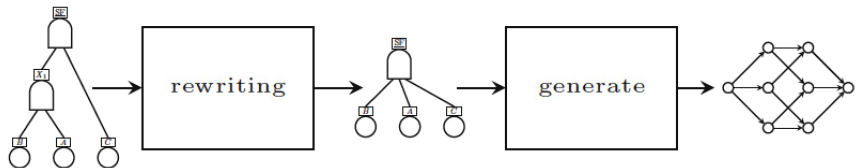
“Metrics are **verifiable** and **precise enough**
to differentiate between different architectures”

⇒ **PMC provides hard guarantees; no statistical ones**

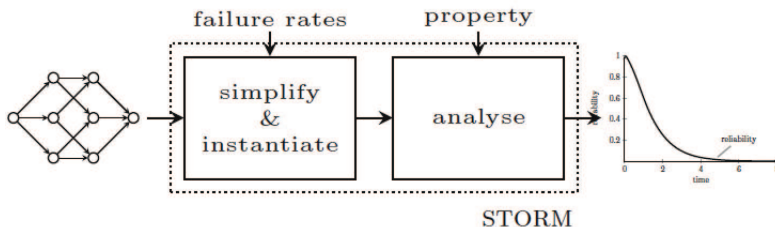
“[for systems where the] concept is based on redundant safety mechanisms,
multiple-point failures of a higher order than two are considered in the analysis”

⇒ **PMC naturally supports analysis of multiple-point of failures**

Model Checking DFTs



DFT simplification and state-space generation



DFT analysis using model checking

Properties in PMC

	Discrete	Continuous
Logic	probabilistic CTL	probabilistic timed CTL
Monitors	deterministic automata (safety and LTL)	deterministic timed automata (MITL fragments)

Others: e.g., conditional probs, multi-objective, rewards, quantiles, etc.

Core problem: computing (timed) reachability probabilities

Reachability Probabilities

Problem

Consider a finite MC with $s \in S$ and $G \subseteq S$.

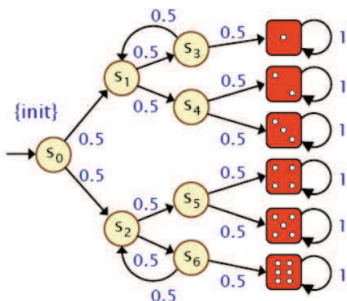
Aim: determine $\Pr(s \models \Diamond G) = \Pr_s\{\pi \in Paths(s) \mid \pi \models \Diamond G\}$

Characterisation of reachability probabilities

- ▶ Let variable $x_s = \Pr(s \models \Diamond G)$ for any state s
 - ▶ if G is not reachable from s , then $x_s = 0$
 - ▶ if $s \in G$ then $x_s = 1$
- ▶ For any state $s \in Pre^*(G) \setminus G$:

$$x_s = \underbrace{\sum_{t \in S \setminus G} P(s, t) \cdot x_t}_{\text{reach } G \text{ via } t \in S \setminus G} + \underbrace{\sum_{u \in G} P(s, u)}_{\text{reach } G \text{ in one step}}$$

Reachability Probabilities: Knuth-Yao's Die



- ▶ Consider the event $\diamond 4$

- ▶ We obtain:

$$x_1 = x_2 = x_3 = x_5 = x_6 = 0 \text{ and } x_4 = 1$$

$$x_{s_1} = x_{s_3} = x_{s_4} = 0$$

$$x_{s_0} = \frac{1}{2}x_{s_1} + \frac{1}{2}x_{s_2}$$

$$x_{s_2} = \frac{1}{2}x_{s_5} + \frac{1}{2}x_{s_6}$$

$$x_{s_5} = \frac{1}{2}x_5 + \frac{1}{2}x_4$$

$$x_{s_6} = \frac{1}{2}x_{s_2} + \frac{1}{2}x_6$$

- ▶ Gaussian elimination yields:

$$x_{s_5} = \frac{1}{2}, x_{s_2} = \frac{1}{3}, x_{s_6} = \frac{1}{6}, \text{ and } x_{s_0} = \frac{1}{6}$$

$$x_{s_0} = \frac{1}{6}$$

Reachability Probabilities are Pivotal

- ▶ **Repeated reachability** $\Pr(s \models \Box \Diamond G)$:

Determine probability to reach a **terminal SCCs** containing a **G**-state

- ▶ **Probabilistic CTL model checking**

Recursive descent on parse tree using reach-probabilities at nodes

- ▶ **LTL formulas** $\Pr(s \models \varphi)$:

1. Transform φ into a **deterministic** (Rabin) automaton
2. Take the **product** of the Markov chain and the automaton
3. Determine the probability to reach an **accepting** terminal SCC from s

This covers **(much) more** than the reliability measures on DFTs.

Probabilistic CTL

[Hansson & Jonsson, 1989]

- ▶ PCTL interpretation is Boolean, i.e., a formula is satisfied or not.
- ▶ For path-formula φ and threshold $>p$ with $> \in \{>, \geq\}$ and $p \in \mathbb{Q}$:

PCTL-formula $[\varphi]_{>p}$ denotes

all paths satisfying φ occur with probability $>p$

- ▶ $[\cdot]_{>p}$ is probabilistic counterpart of CTL path-quantifiers \exists and \forall .
- ▶ Examples: $[\Diamond a]_{>1/2}$, $[\Diamond[\Box a]_{=1}]_{>1/2}$ and $[\Box(\neg a \wedge [\Diamond a]_{>0})]_{>0}$.

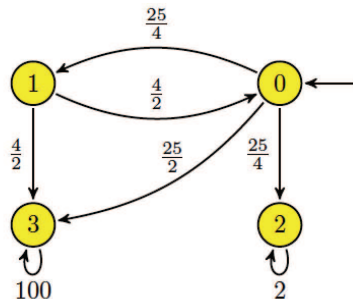
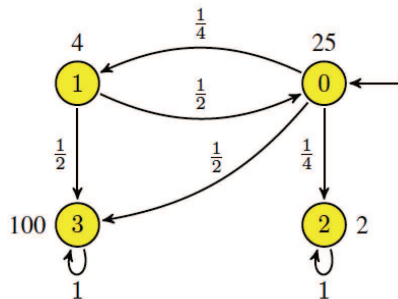
PCTL model checking is in P.

Random Timing



Continuous-Time Markov Chains

A CTMC is a DTMC with an *exit rate* function $r : S \rightarrow \mathbb{R}_{>0}$ where $r(s)$ is the rate of an exponential distribution.



Zenoness

Zeno theorem

In every CTMC, almost surely no Zeno runs occur.

In contrast to timed automata verification, Zeno runs thus pose **no** problem.

Timed Reachability Probabilities

[Baier *et al.*, 2003]

Problem

Consider a finite CTMC with $s \in S$, $t \in \mathbb{R}_{\geq 0}$ and $G \subseteq S$.

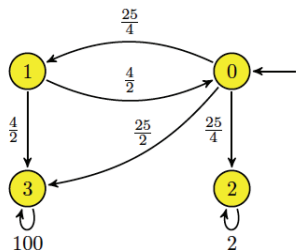
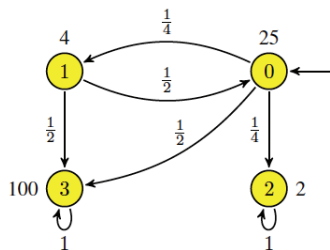
Aim: determine $\Pr(s \models \Diamond^{\leq t} G)$.

Characterisation of timed reachability probabilities

- Let function $x_s(t) = \Pr(s \models \Diamond^{\leq t} G)$ for any state s
 - if G is not reachable from s , then $x_s(t) = 0$ for all t
 - if $s \in G$ then $x_s(t) = 1$ for all t
- For any state $s \in \text{Pre}^*(G) \setminus G$:

$$x_s(t) = \int_0^t \sum_{s' \in S} \underbrace{R(s, s') \cdot e^{-r(s) \cdot x}}_{\text{probability to move to state } s' \text{ at time } x} \cdot \underbrace{x_{s'}(t-x)}_{\text{prob. to fulfill } \Diamond^{\leq t-x} G \text{ from } s'} dx$$

Timed Reachability Probabilities



Integral equations for $\diamond^{\leq 10} 2$:

- ▶ $x_3(d) = 0$ and $x_2(d) = 1$ for all d
- ▶ $x_0(d) = \int_0^d 25/4 \cdot e^{-25 \cdot x} \cdot x_1(d-x) + 25/4 \cdot e^{-25 \cdot x} \cdot x_2(d-x) dx$
- ▶ $x_1(d) = \int_0^d 4/2 \cdot e^{-4 \cdot x} \cdot x_0(d-x) + 4/2 \cdot e^{-4 \cdot x} \cdot x_3(d-x) dx$

Timed Reachability Probabilities

Reachability probabilities

Solve a system of linear equations for which many efficient techniques exist.

Timed reachability probabilities

Solve a system of **Volterra integral** equations.

Non-trivial, inefficient, and has several pitfalls such as numerical stability.

Solution

Reduce $\Pr(s \models \Diamond^{\leq t} G)$ to computing transient probabilities.

Timed Reachability Probabilities = Transient Probabilities

Aim

Compute $\Pr(s \models \Diamond^{\leq t} G)$ in CTMC \mathcal{C} . Observe that once a path π reaches G within t time, then the remaining behaviour along π is not important.
 \Rightarrow make all states in G absorbing.

$$\underbrace{\Pr(s \models \Diamond^{\leq t} G)}_{\text{timed reachability in } \mathcal{C}} = \underbrace{\Pr(s \models \Diamond^{=t} G)}_{\text{timed reachability in } \mathcal{C}[G]} = \underbrace{\vec{p}(t)}_{\text{transient prob. in } \mathcal{C}[G]} \text{ with } \vec{p}(0) = \mathbf{1}_s.$$

Transient probabilities can be efficiently computed as solutions of linear differential equations.

Computing Transient Probabilities

By solving a linear differential equation system

The **transient** probability vector $\underline{p}(t) = (p_{s_1}(t), \dots, p_{s_k}(t))$ satisfies:

$$\underline{p}'(t) = \underline{p}(t) \cdot (\mathbf{R} - \mathbf{r}) \quad \text{given} \quad \underline{p}(0)$$

where \mathbf{r} is the diagonal matrix of vector \underline{r} .

Solution using standard knowledge yields: $\underline{p}(t) = \underline{p}(0) \cdot e^{(\mathbf{R} - \mathbf{r}) \cdot t}$.

Computing the matrix exponential is a **challenging numerical** problem¹.

¹19 dubious ways to compute a matrix exponential [Moler & Van Loan, 1978/2003].

Uniformisation

CTMC \mathcal{C} is **uniform** if $r(s) = r$ for all $s \in S$ for some $r \in \mathbb{R}_{>0}$.

Uniformisation

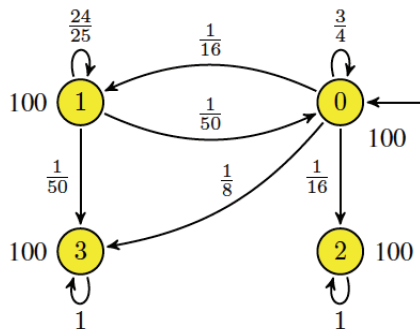
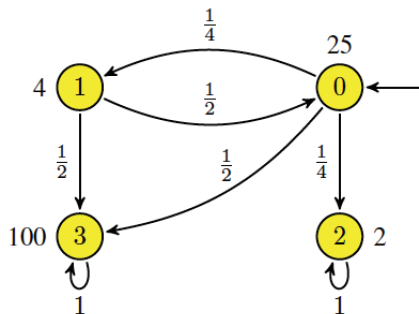
[Gross and Miller, 1984]

Let $r \in \mathbb{R}_{>0}$ such that $r \geq \max_{s \in S} r(s)$. Then $\bar{r}(\mathcal{C})$ is the CTMC \mathcal{C} with two changes: $\bar{r}(s) = r$ for all $s \in S$, and:

$$\bar{P}(s, s') = \frac{r(s)}{r} \cdot P(s, s') \text{ if } s' \neq s \quad \text{and} \quad \bar{P}(s, s) = \frac{r(s)}{r} \cdot P(s, s) + 1 - \frac{r(s)}{r}.$$

\bar{P} is a stochastic matrix and $\bar{r}(\mathcal{C})$ is **uniform**.

Uniformisation by Example



Uniformisation amounts to **normalise** the residence time in every CTMC state.

Benefits of Uniformisation

Transient probabilities of a CTMC and its uniformized CTMC coincide.

$$\text{Thus: } \underbrace{\underline{p}(t) = \underline{p}(0) \cdot e^{(\mathbf{R}-\mathbf{r}) \cdot t}}_{\text{transient probability in } \mathcal{C}} = \underbrace{\underline{p}(0) \cdot e^{(\bar{\mathbf{R}}-\bar{\mathbf{r}}) \cdot t}}_{\text{transient probability in } \bar{\mathcal{C}}} = \underline{p}(0) \cdot e^{-\mathbf{r} \cdot t} \cdot e^{\mathbf{r} \cdot t \cdot \bar{\mathbf{P}}}$$

Still a matrix exponential remains. Did we gain anything?
 Yes. Since $\bar{\mathbf{P}}$ is stochastic, Taylor-Maclaurin yields $\sum_i \dots \bar{\mathbf{P}}^i$.

Other Properties on CTMCs

- ▶ Expected time objectives

Can be characterised as solution of set of linear equations

- ▶ Long-run average objectives

1. Determine the limiting distribution in any terminal SCC
2. Take weighted sum with reachability probabilities terminal SCCs

- ▶ Probabilistic timed CTL model checking

recursive descent over parse tree

- ▶ Deterministic timed automata objectives

1. Take product of the MC and the Zone automaton of the DTA²
2. Determine the probability to reach an accepting zone

²This yields a piecewise deterministic Markov process.

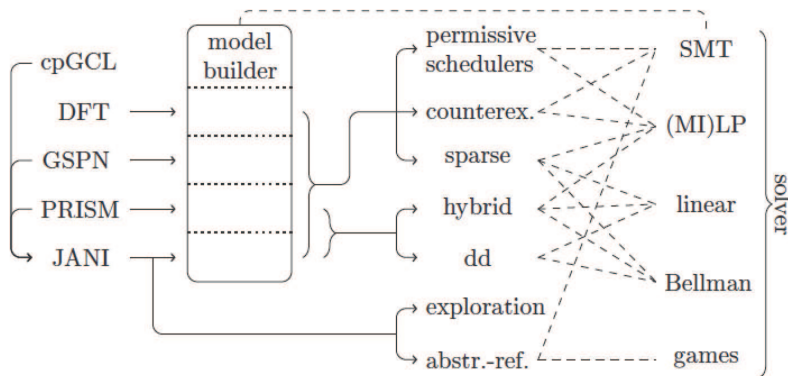
Probabilistic Model Checkers

- ▶ PRISM³ [Kwiatkowska, Parker *et al.*]
- ▶ MRMC [Katoen *et al.*]
- ▶ iscasMC [Zhang *et al.*]
- ▶ iBioSim [Myers *et al.*]
- ▶ GreatSPN [Franceschinis *et al.*]
- ▶ SMART [Ciardo *et al.*]
- ▶ MarCie [Heiner *et al.*]
- ▶ PAT [Song Dong *et al.*]
- ▶ **SToRM** [Dehnert, Katoen *et al.*]
- ▶

Statistical model checkers: Ymer, Vesta, UppAal-SMC, PlasmaLab,

³Recipient HVC Award 2016.

The Probabilistic Model Checker SToRM [Dehnert *et al.*, CAV 2017]

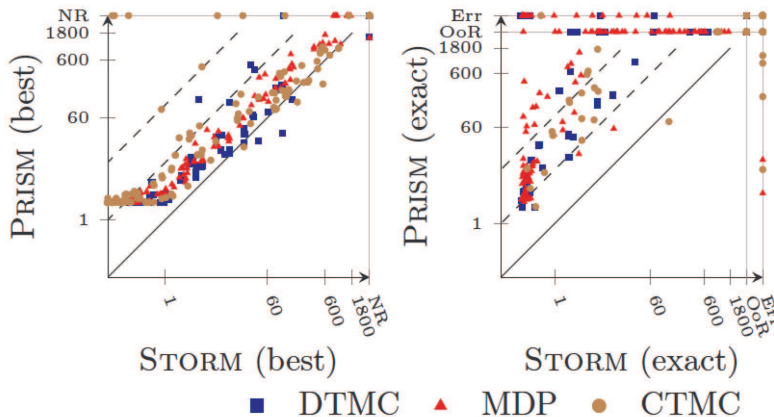


Native support for Dugan's dynamic fault trees

About 100,000 lines of C++ code

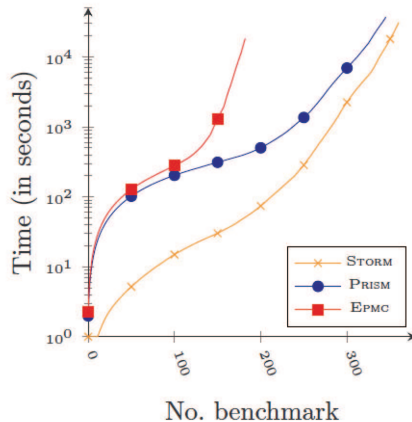
stormchecker.org

SToRM's Performance



Comparing the best engines of PRISM and STORM

SToRM's Performance



Comparing the best engines for all

Fault Tree Analysis by Model Checking

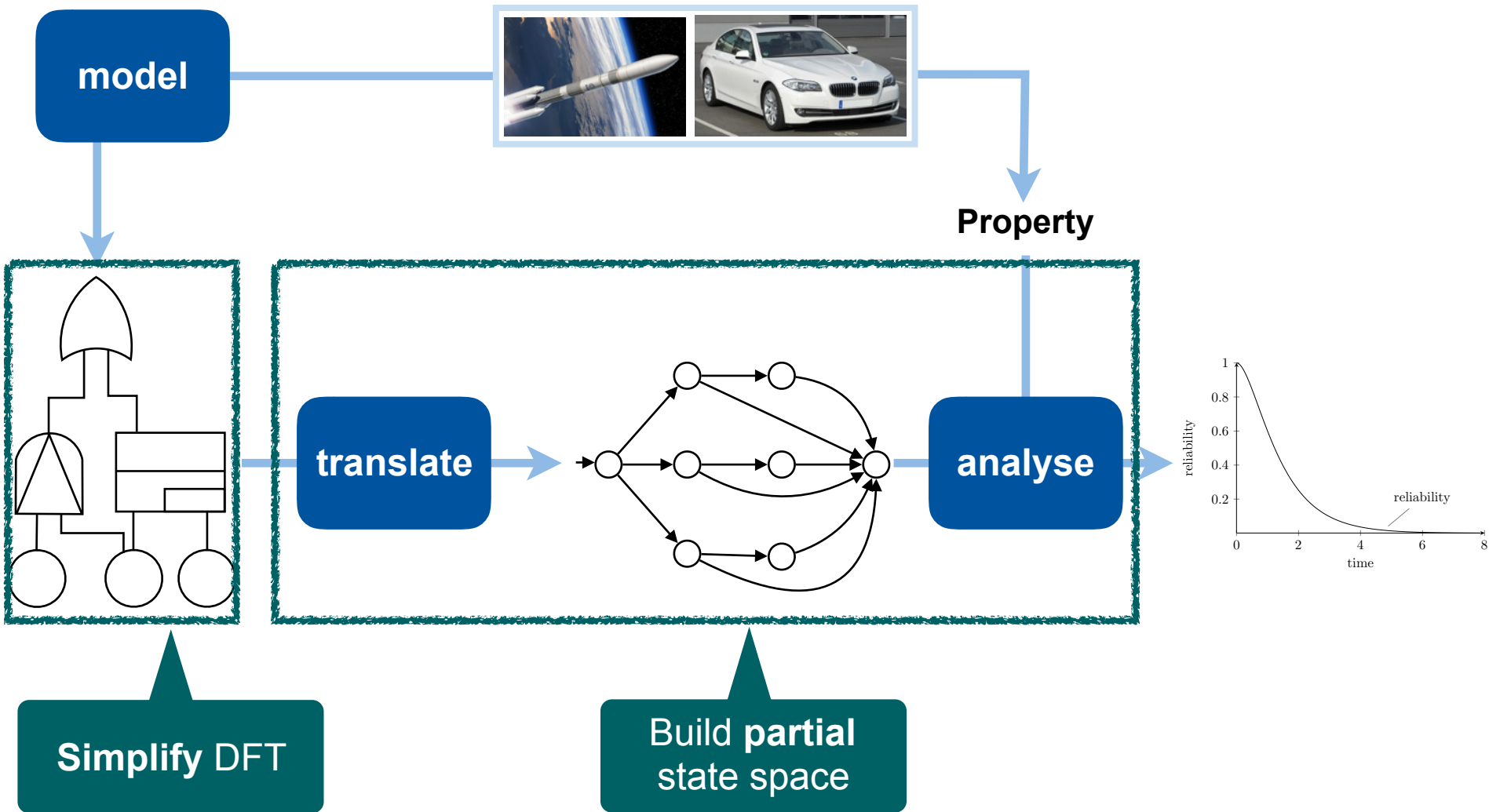
Probabilistic model checking \approx automated verification of models with randomness

Its Pros:

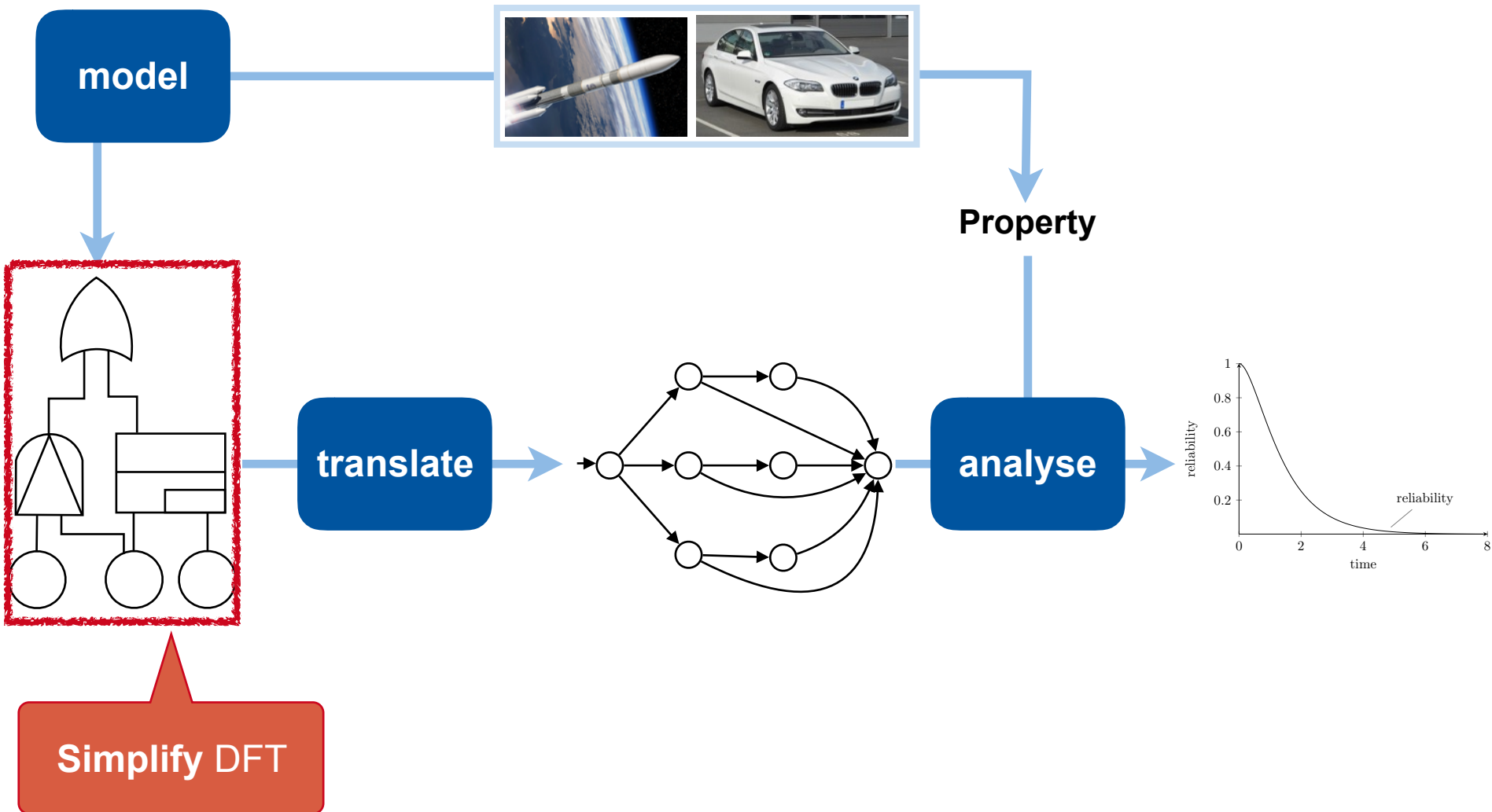
- ▶ Efficient and effective techniques for slim state-space generation
- ▶ Fully automated approach typically much faster than FT analysis
- ▶ Beyond MTTF, availability and reliability: many safety measures
- ▶ Supports checking functional correctness of FTs
- ▶ Supports non-determinacy as first-class citizen
- ▶ Tailored abstraction ... \implies ... scalability

Model-checking times are negligible compared to state-space generation times

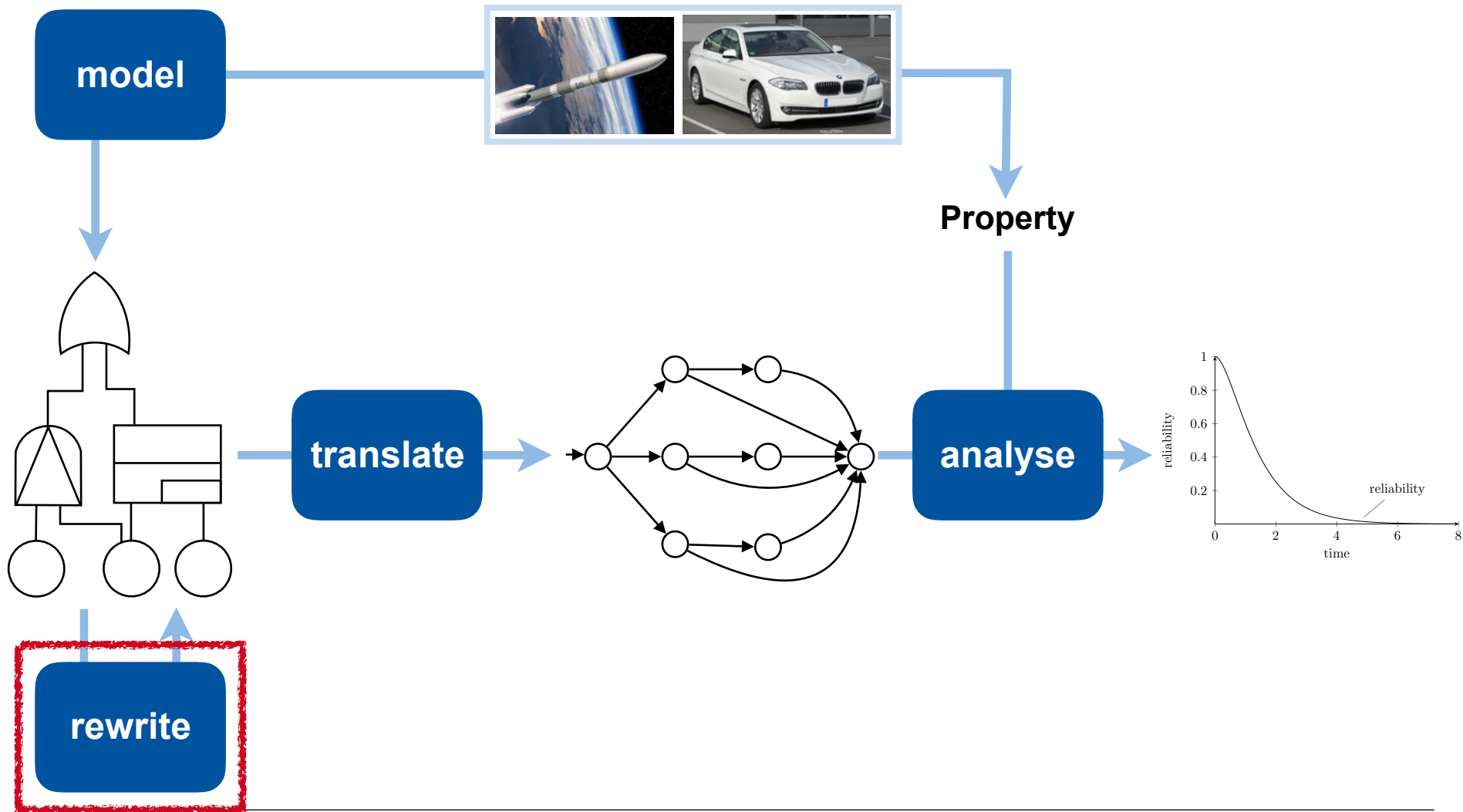
Overview



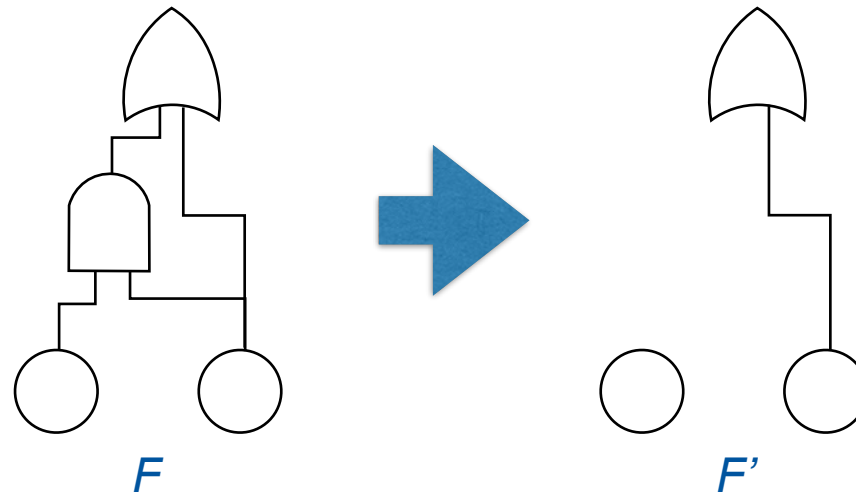
Overview



Overview

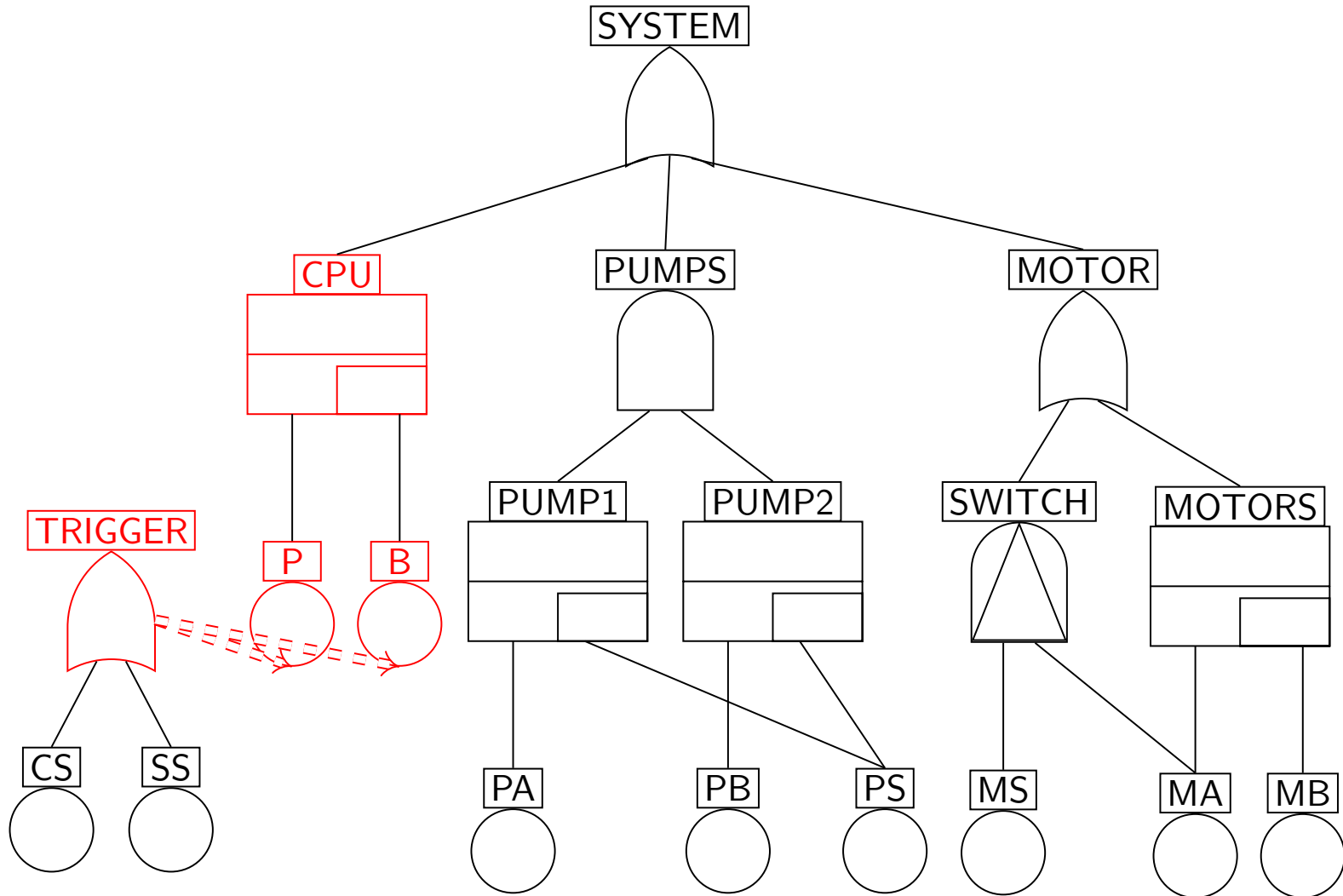


- Simplify DFTs before analysis
- Reduce DFT F via **graph rewriting** to smaller DFT F'

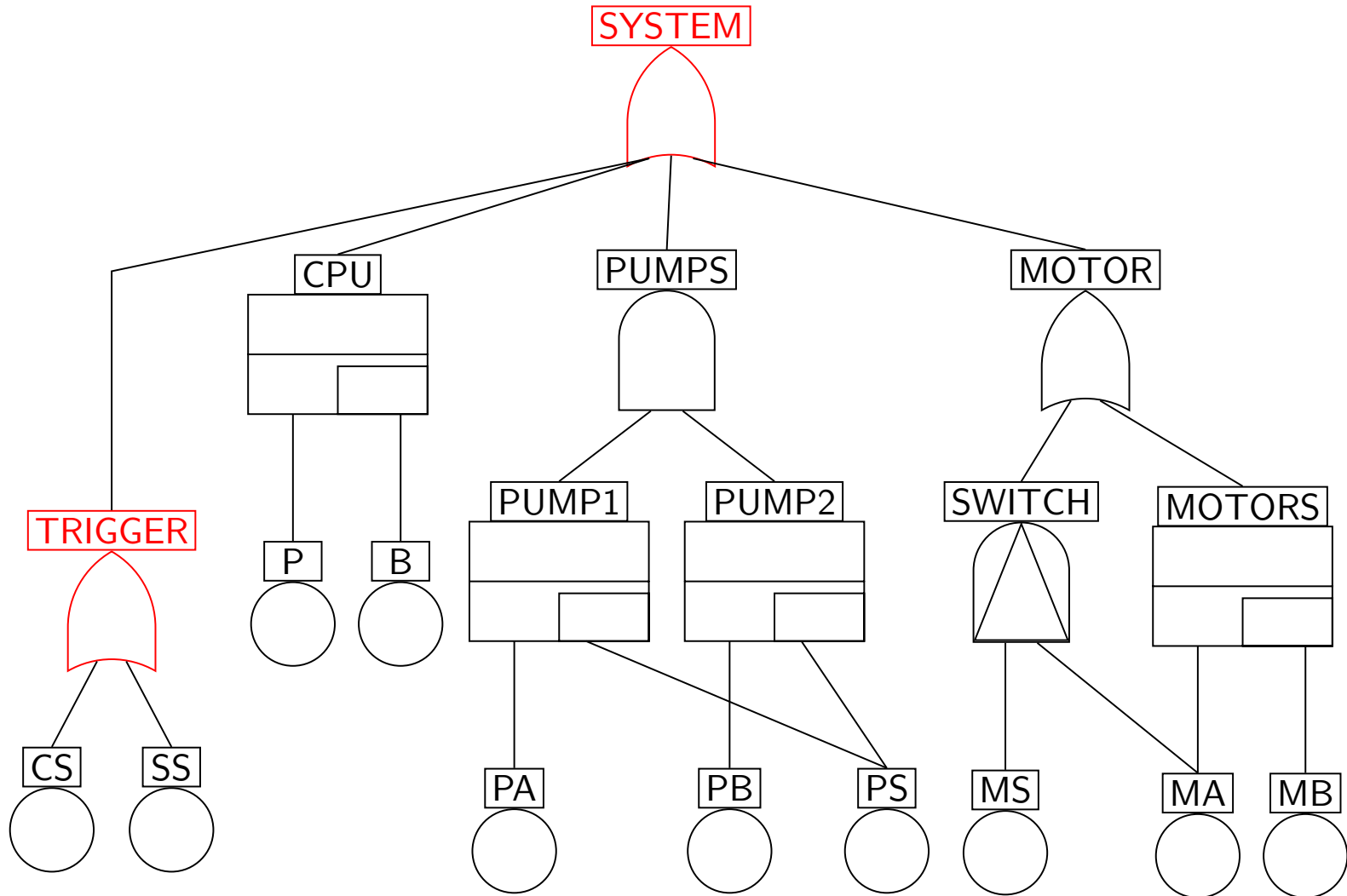


- Rewriting **preserves measures** of interest (reliability, MTTF, ...)
 - ➔ Suffices to **analyse F'**

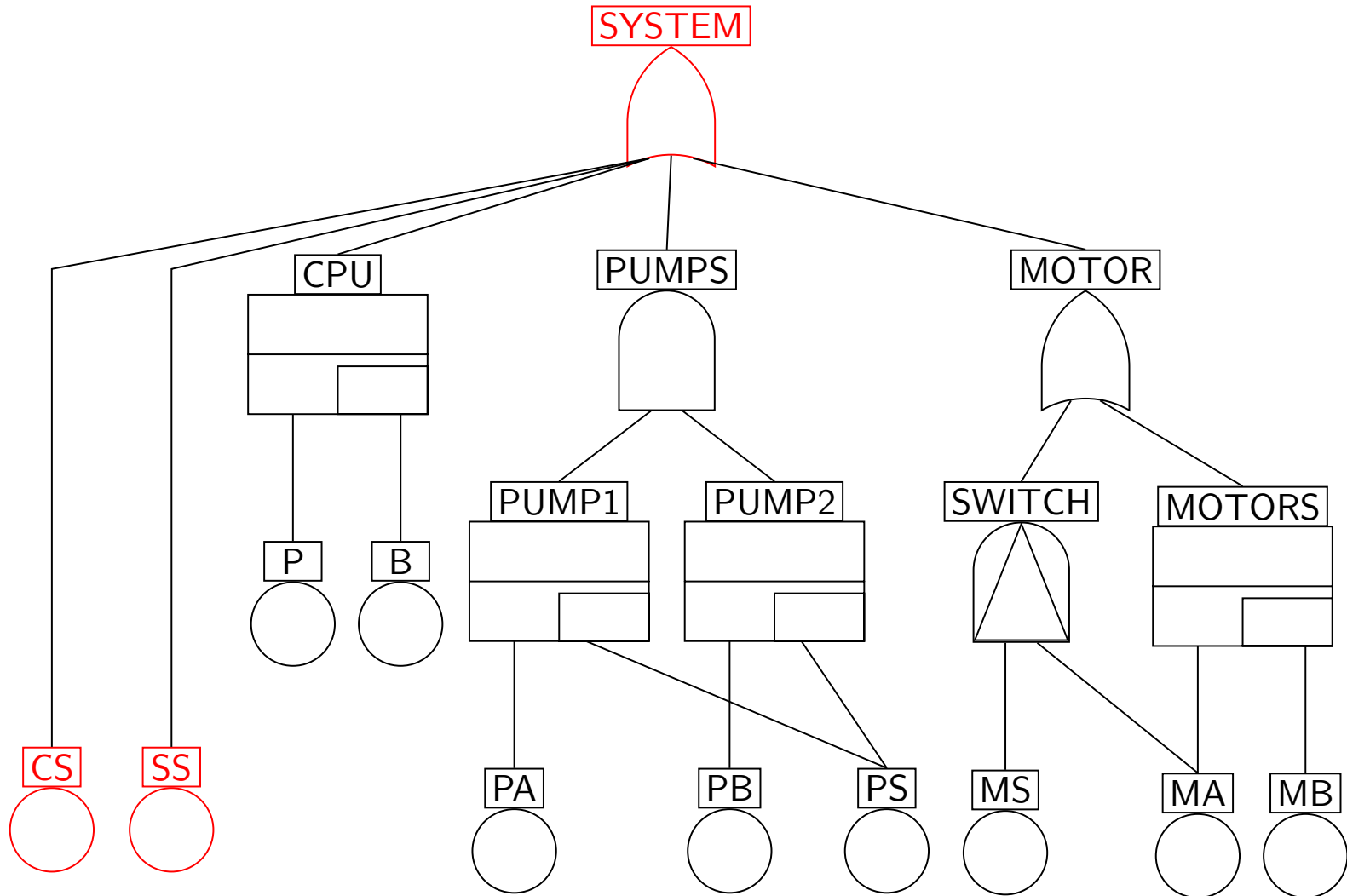
Example simplification



Example simplification

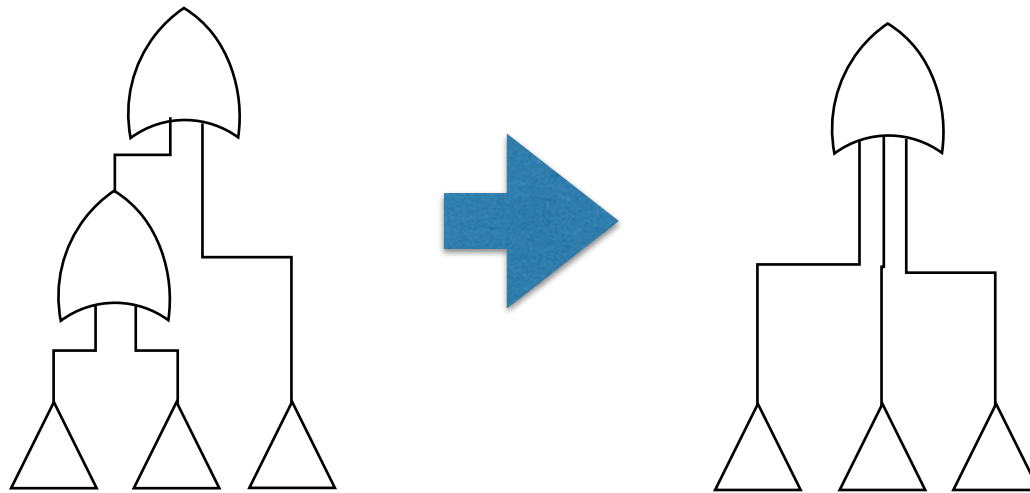


Example simplification



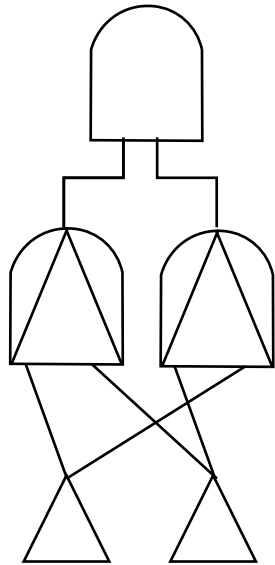
Reduction rule I

Flattening of static gates



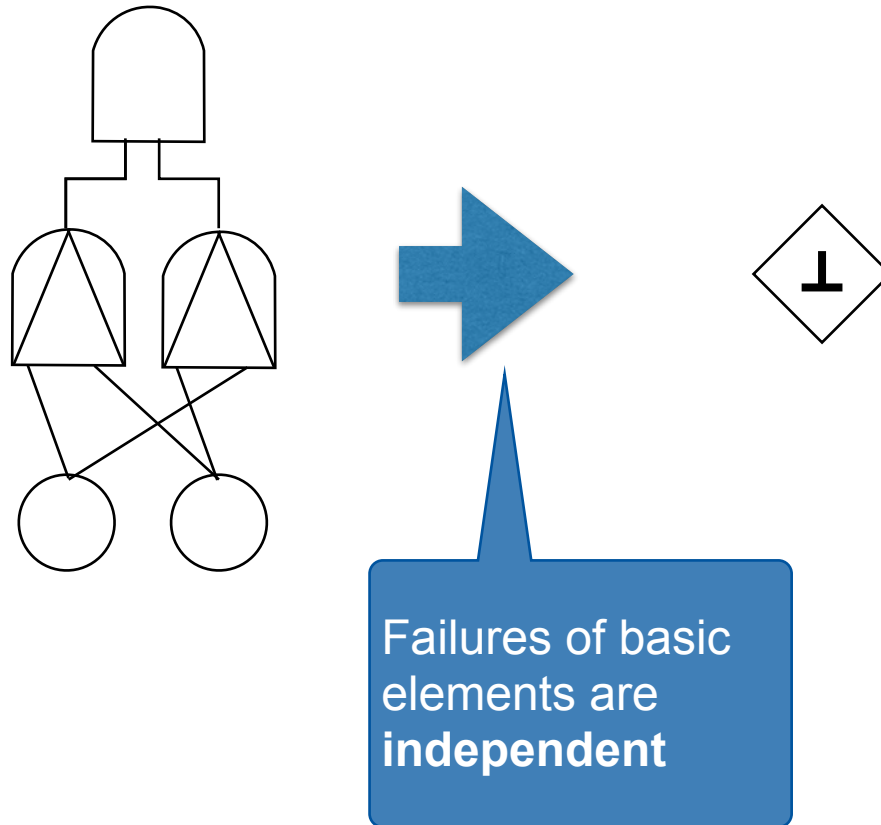
Reduction rule II

Simplification of conflicting PAND gates



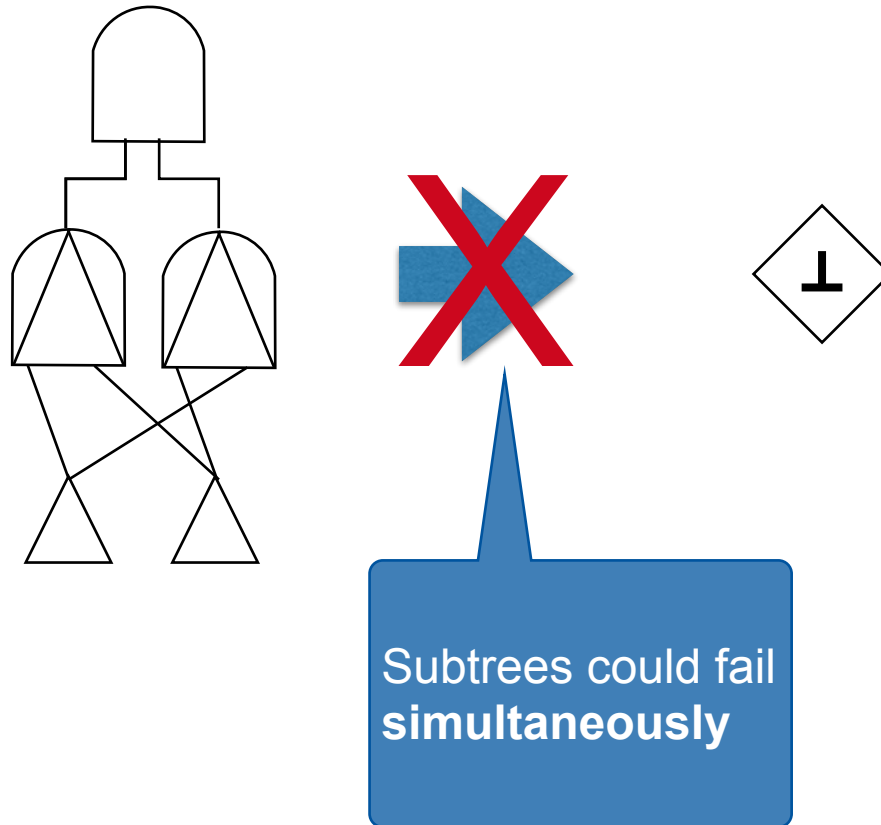
Reduction rule II

Simplification of conflicting PAND gates



Reduction rule II

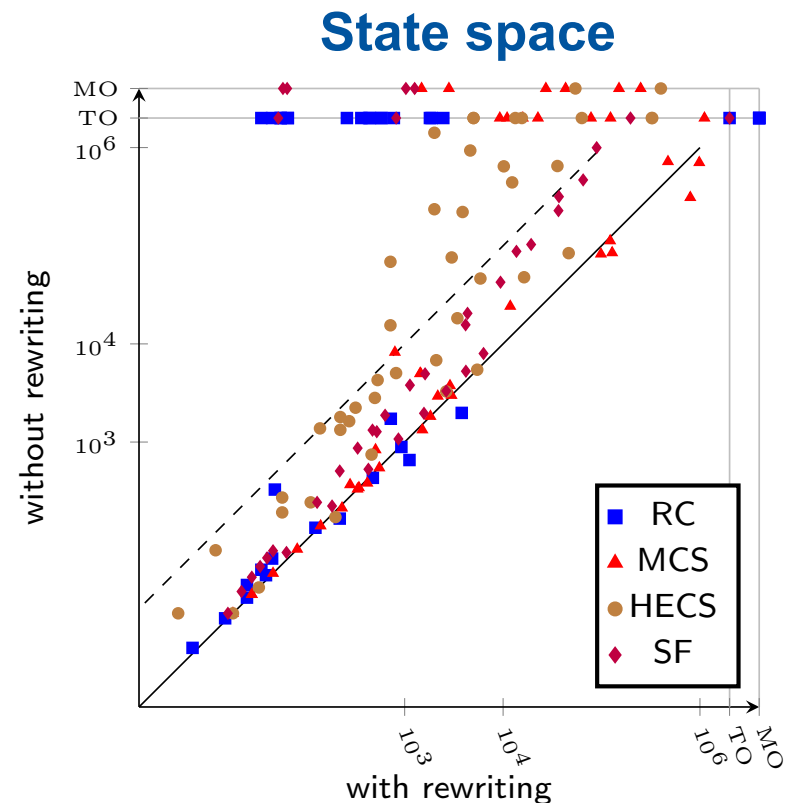
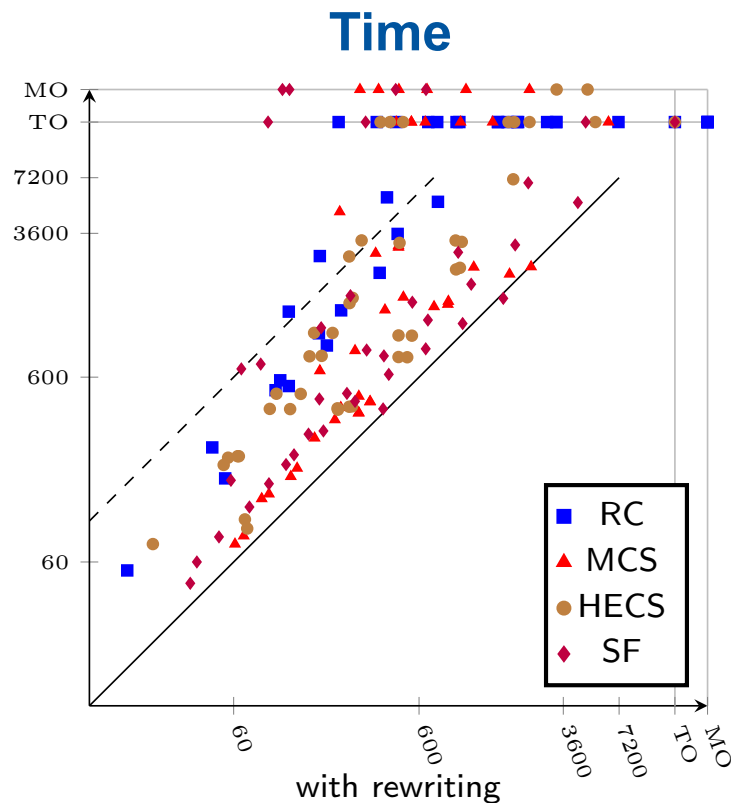
Simplification of conflicting PAND gates



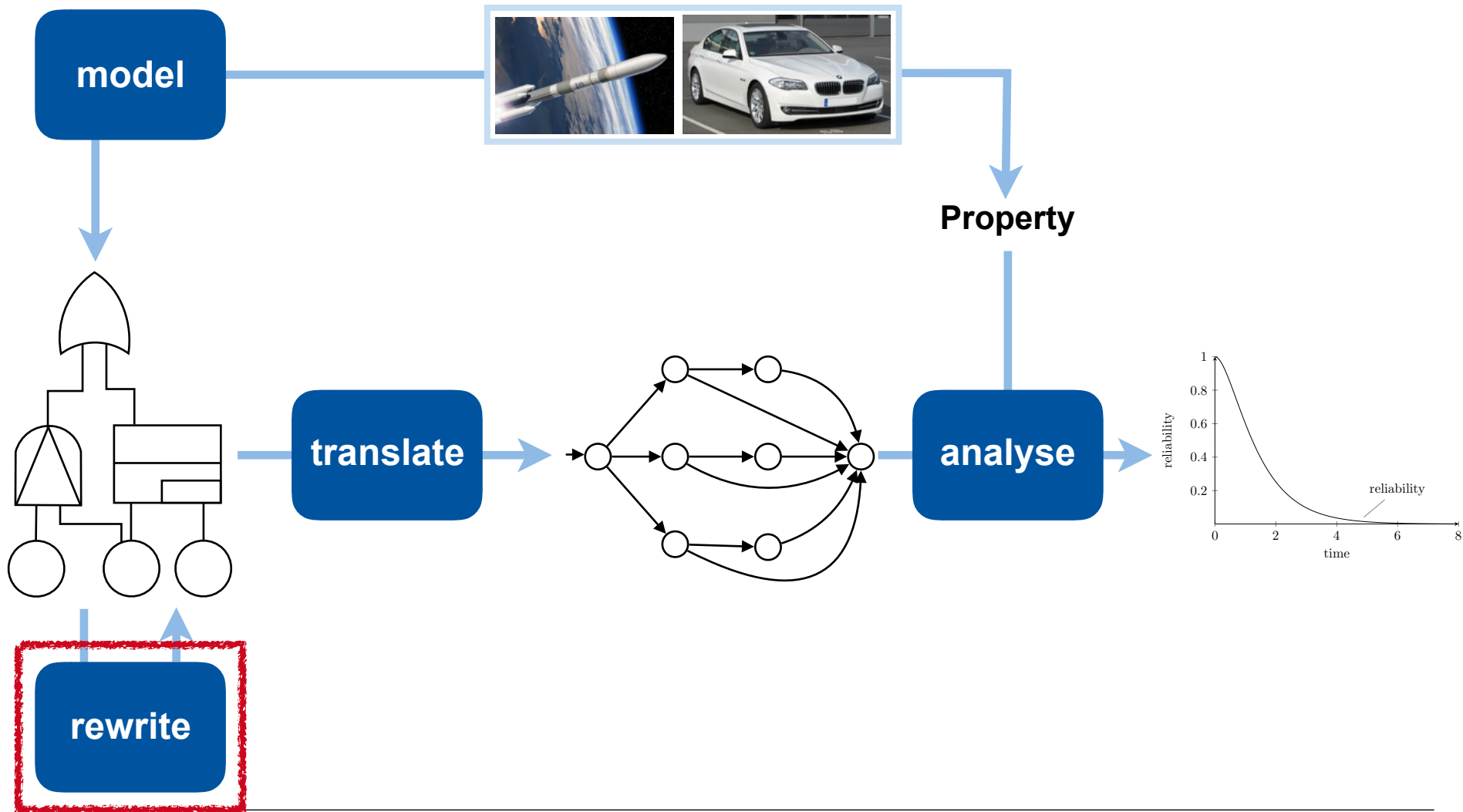
Rewriting DFTs

- Context-sensitive rewrite rules
- 29 rule families:
 - flattening of AND, OR, PAND
 - conflicting PAND gates
 - simplifying FDEP gates
 - ...
- Fully automated graph rewriting

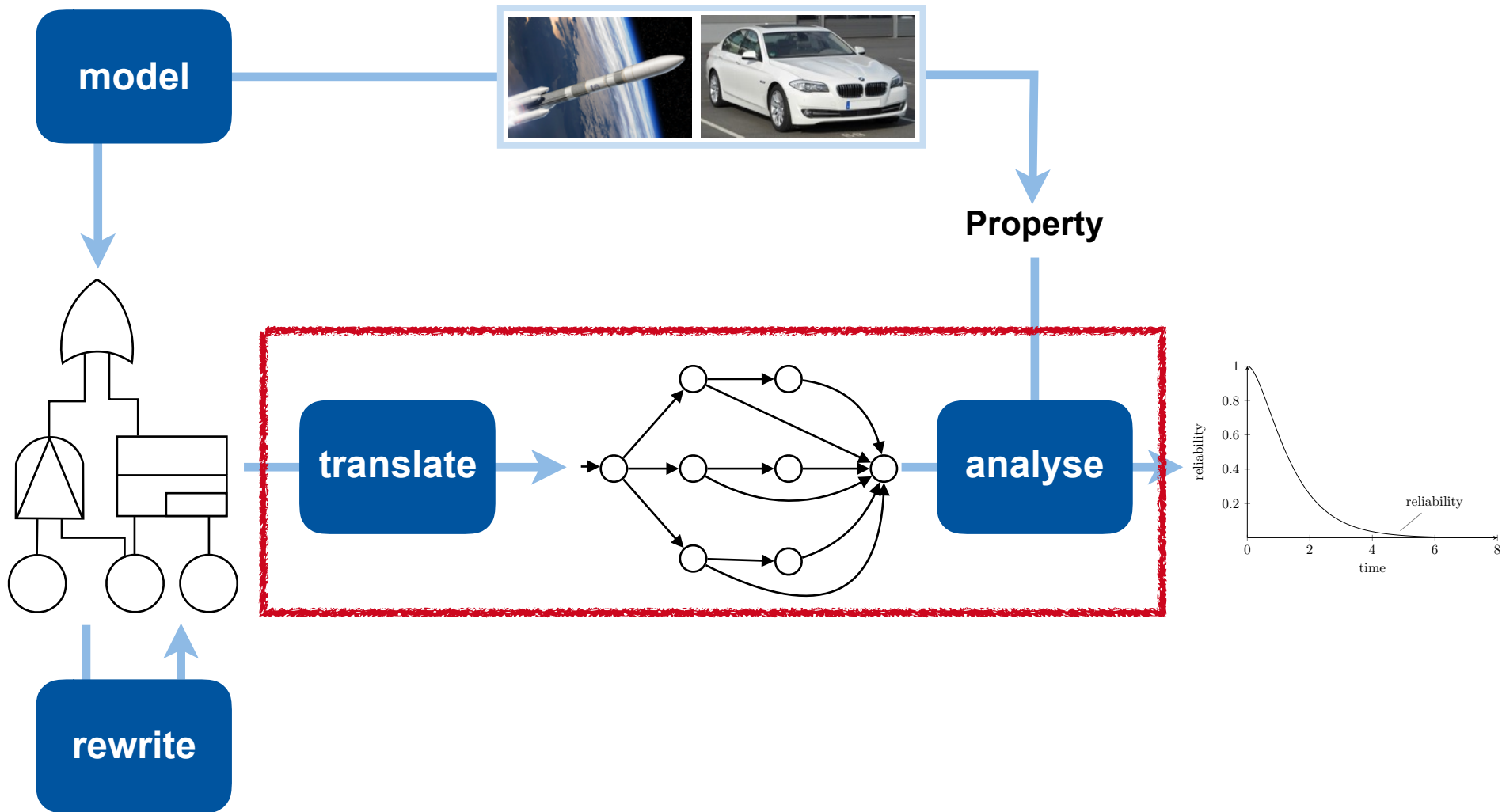
- Analysis with **DFTCalc**
- could solve **27% more** examples with rewriting



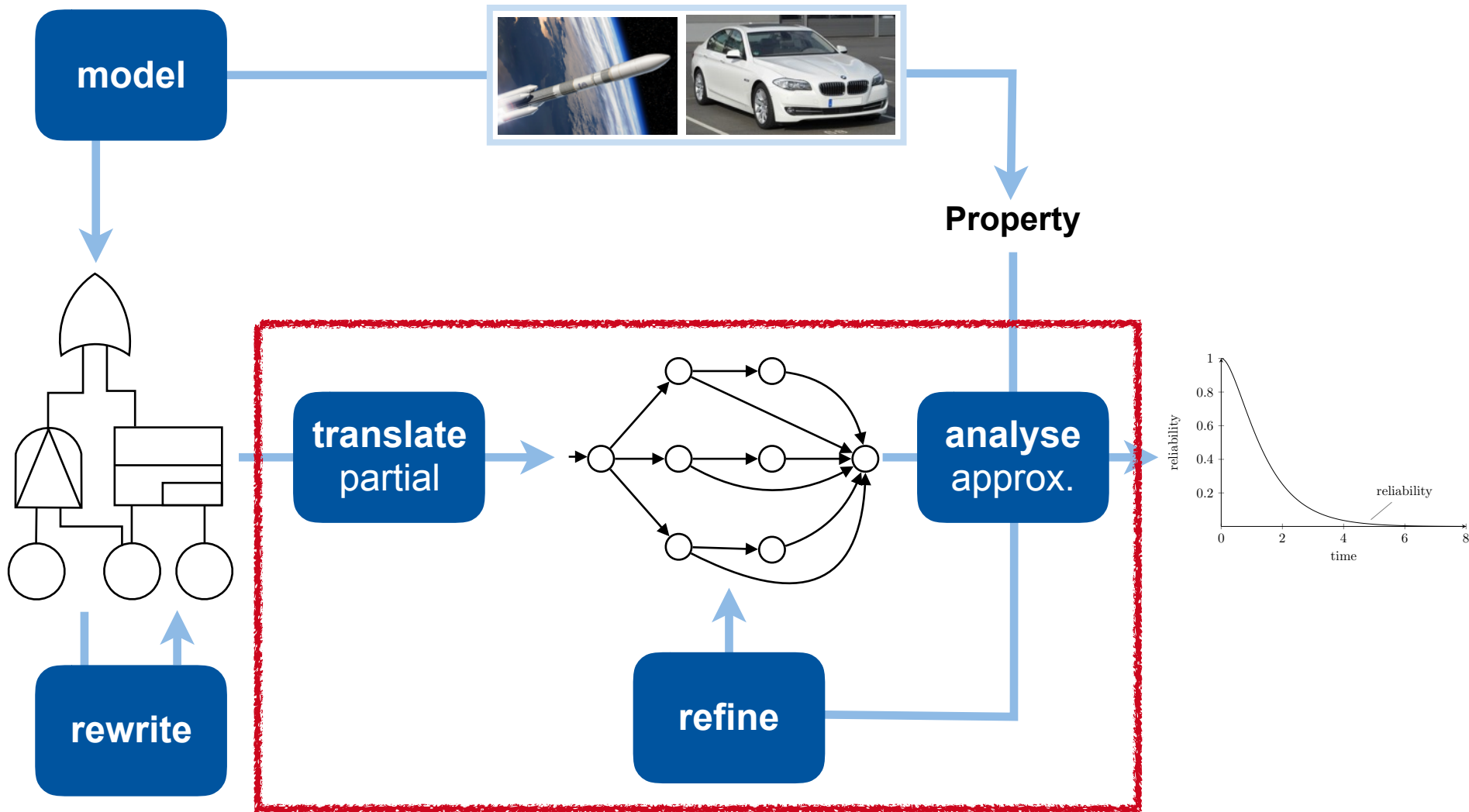
Overview



Overview



Overview



Problem:
state space might still be **large**

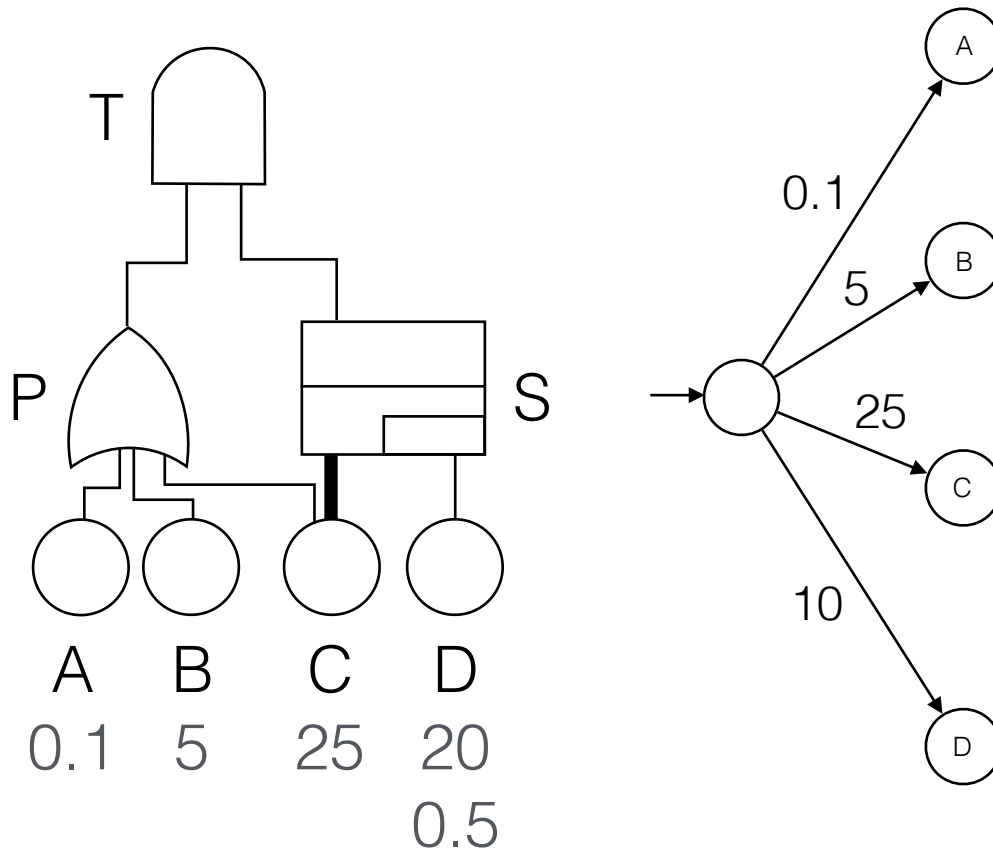
Observations:

1. **Exact** solution often not necessary:
e.g. ISO 26262 for automobiles requires analysis of 2 independent failures
 ➔ consider only **paths of length 2**
2. **Differences in rates** in orders of magnitude

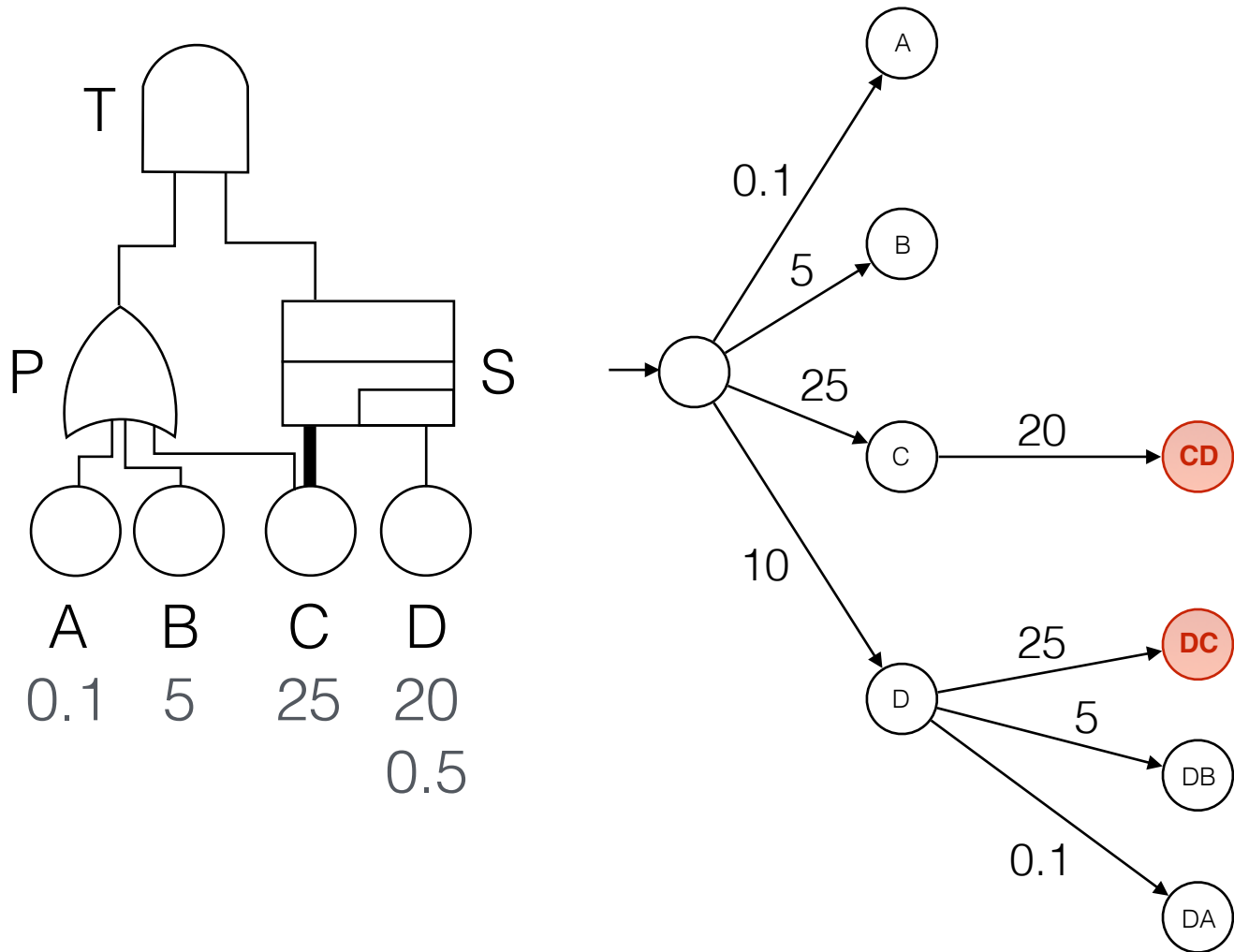
Solution:

- ➔ **Approximate result:**
- build only **parts of state space**
 - give **over-** and **under-approximation** of exact result

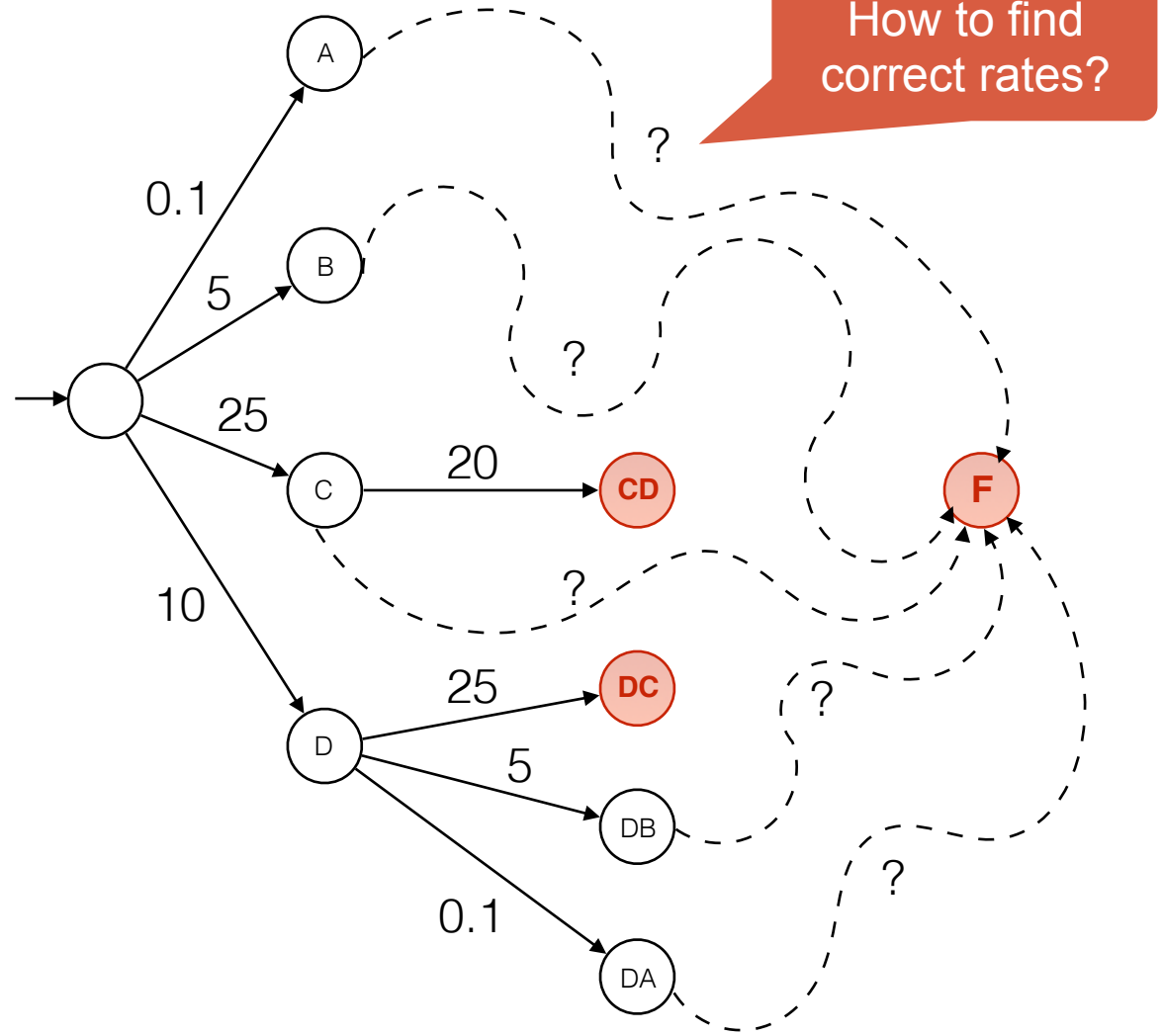
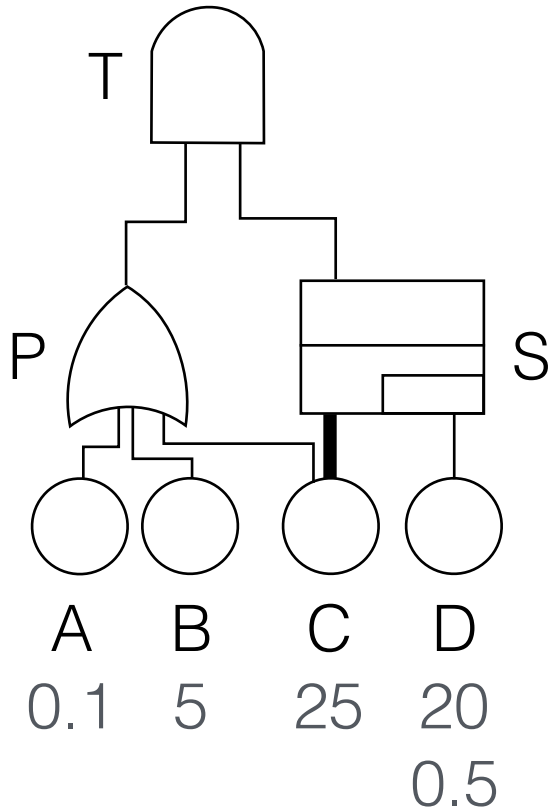
Approximation idea



Approximation idea



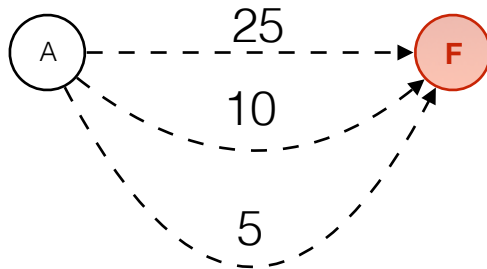
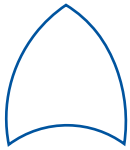
Approximation idea



Under and over approximation for MTTF

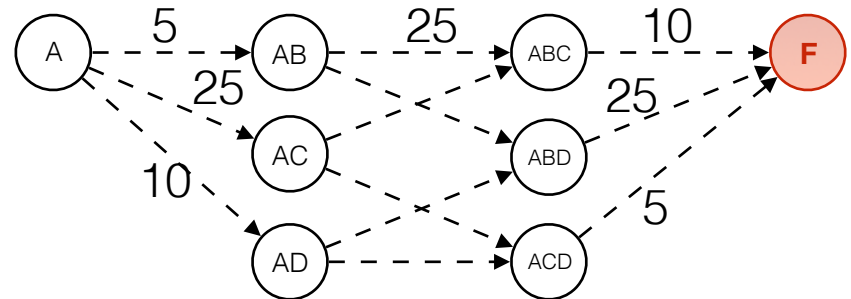
- **Under approximation:**

- next BE leads to complete failure

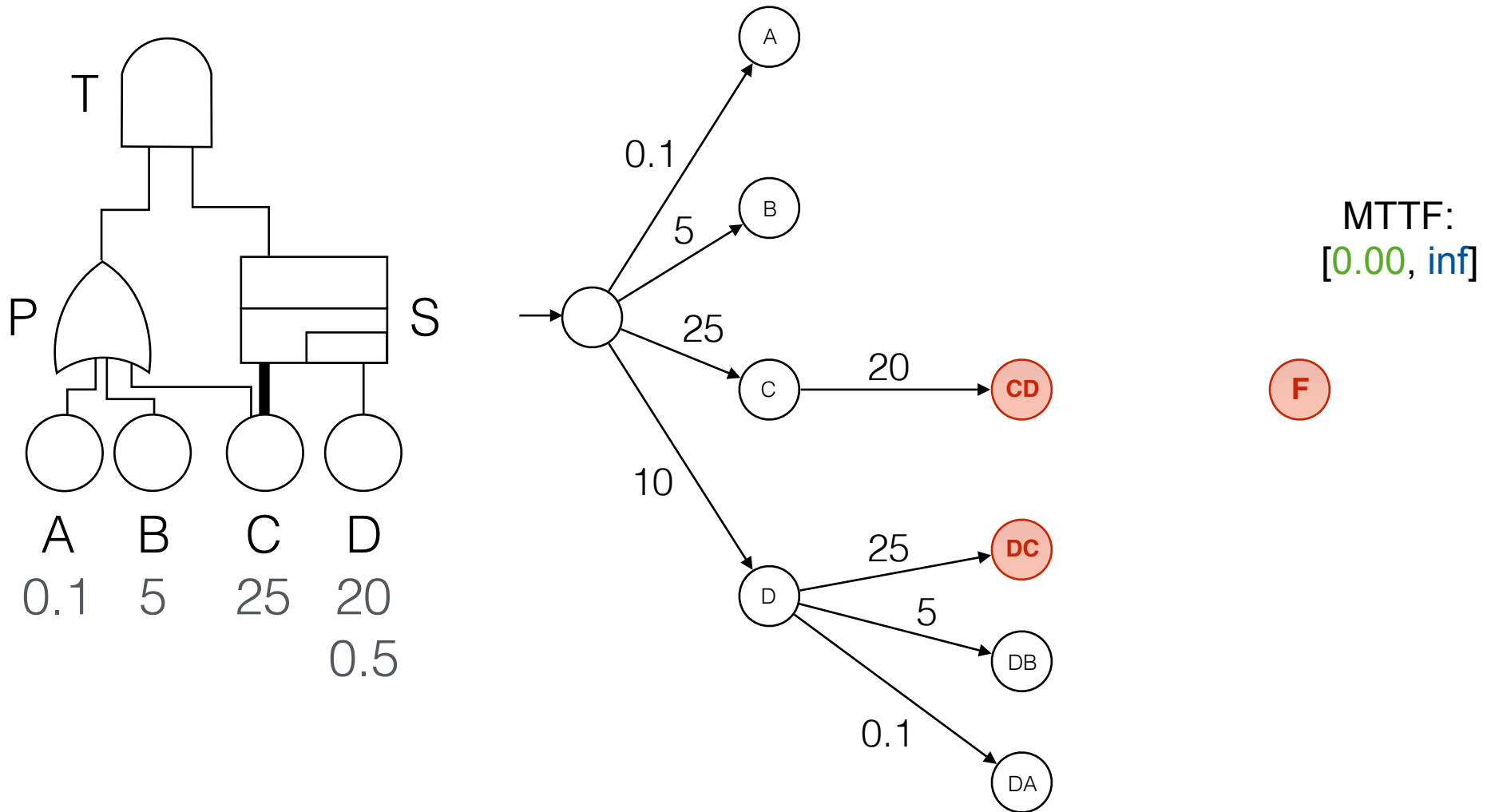


- **Over approximation:**

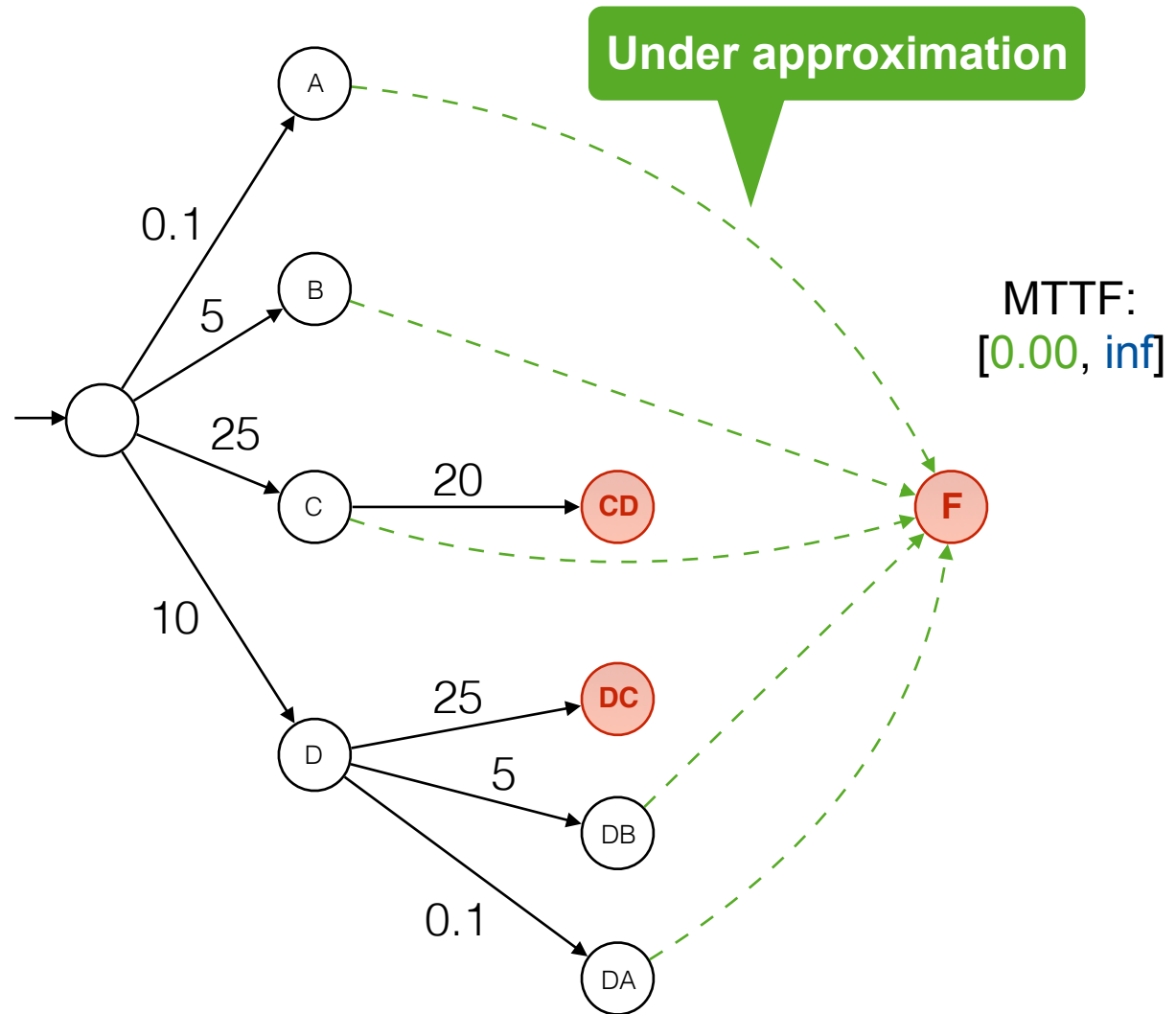
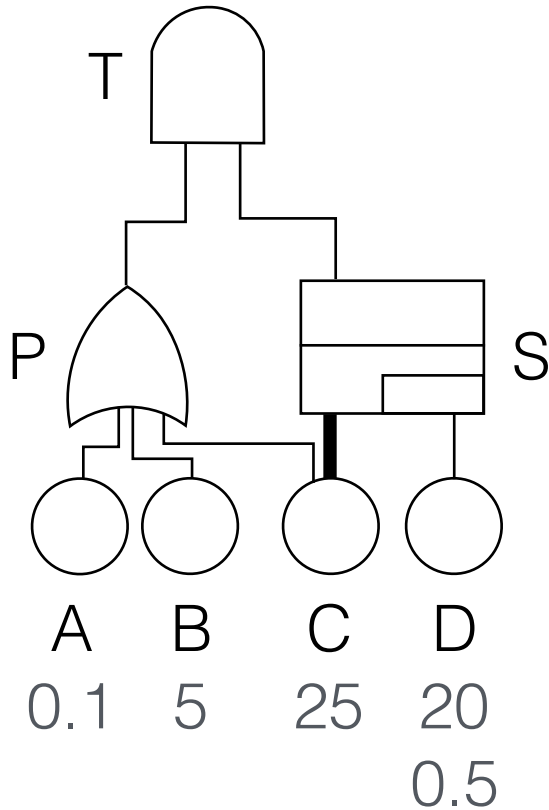
- complete failure only if **all** remaining BEs failed



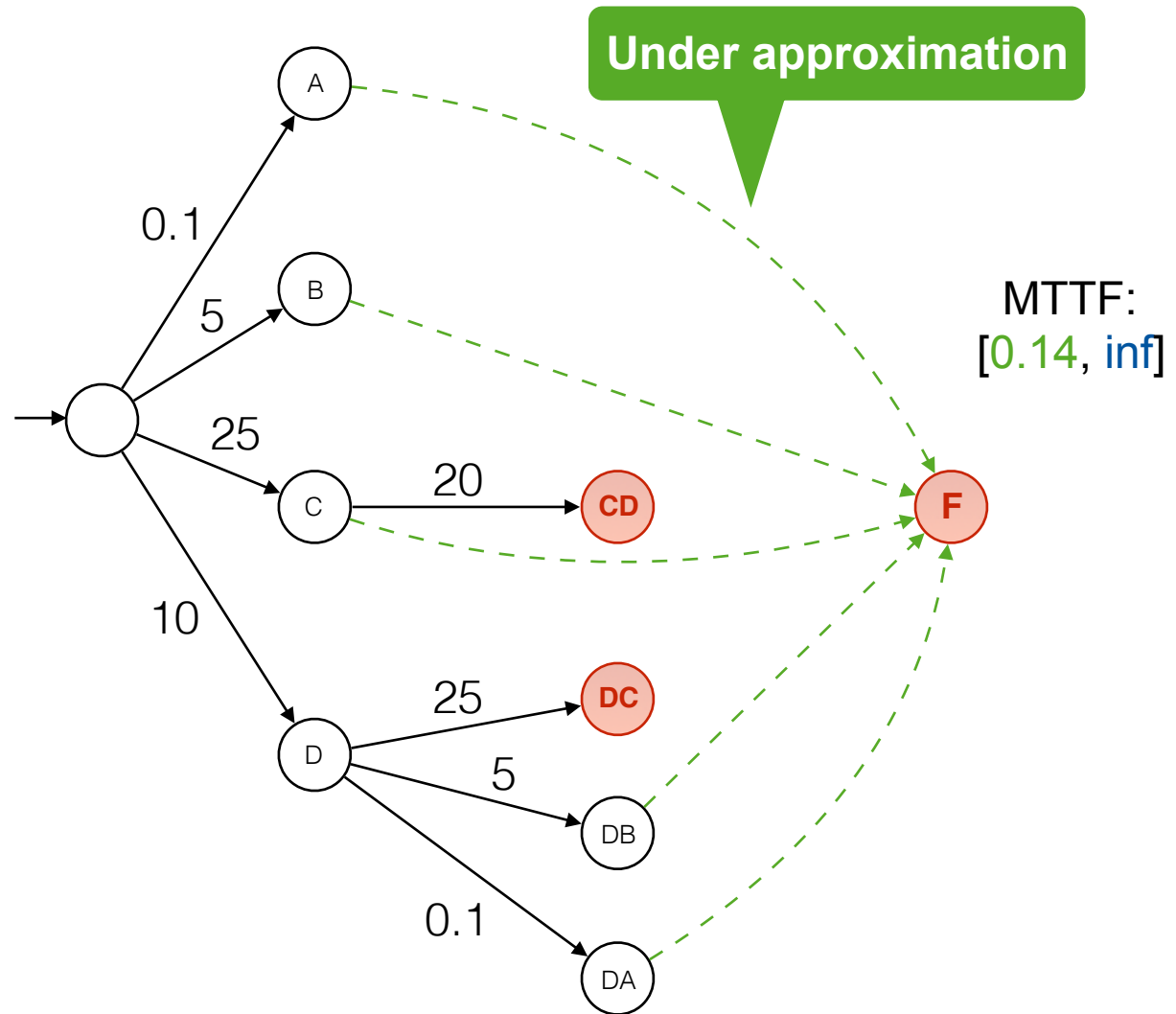
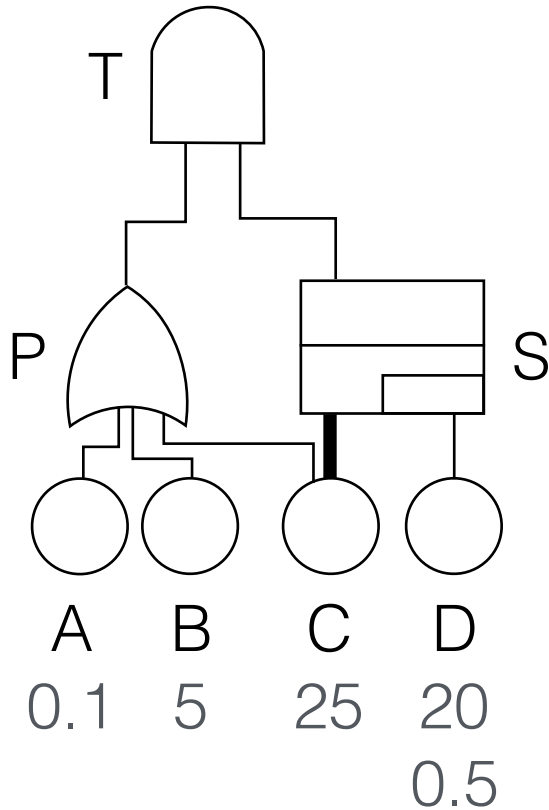
Approximation algorithm



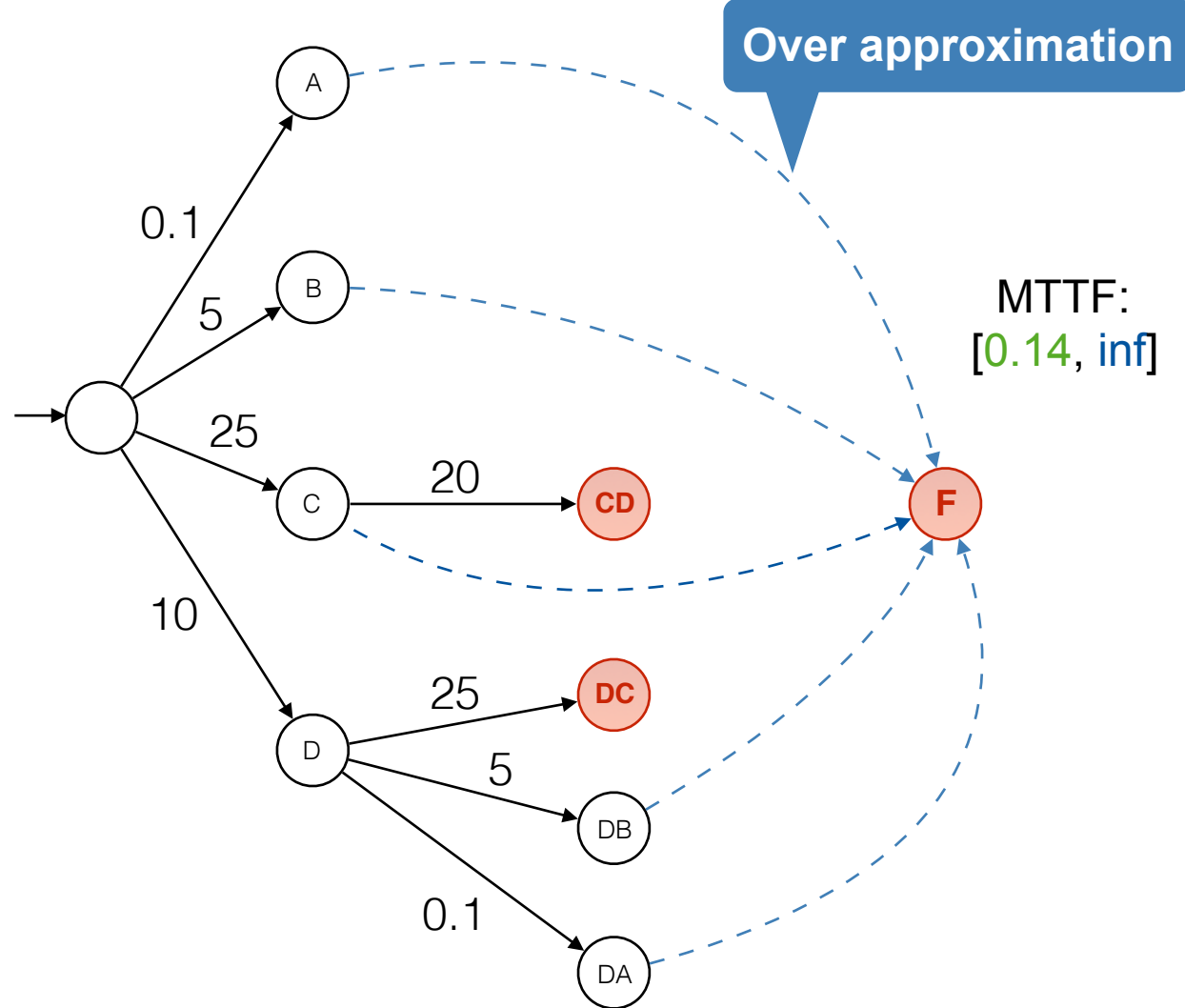
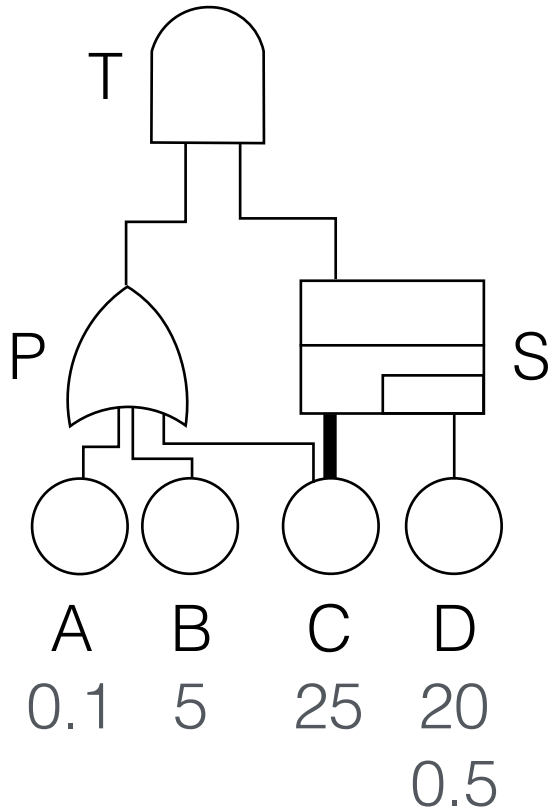
Approximation algorithm



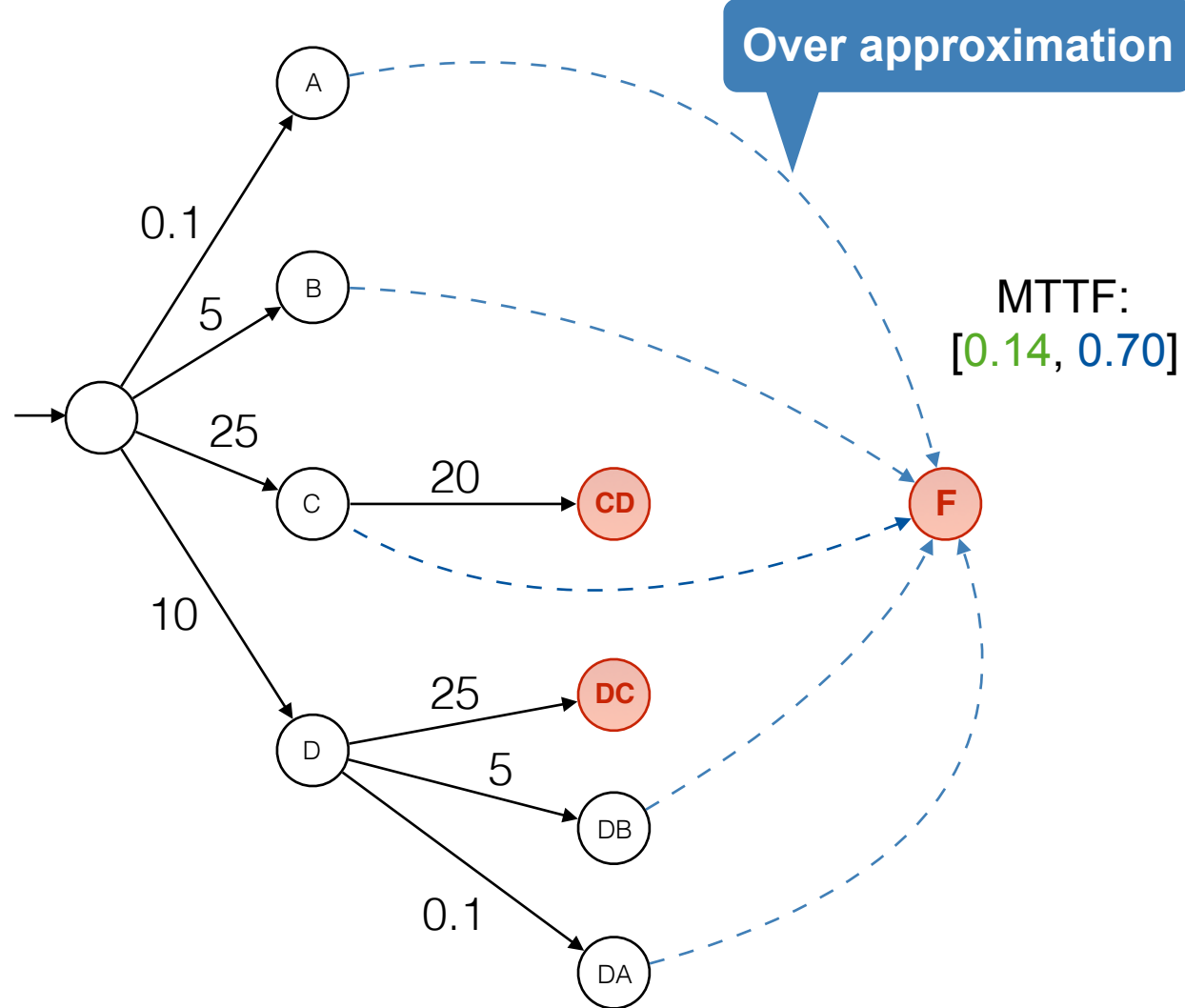
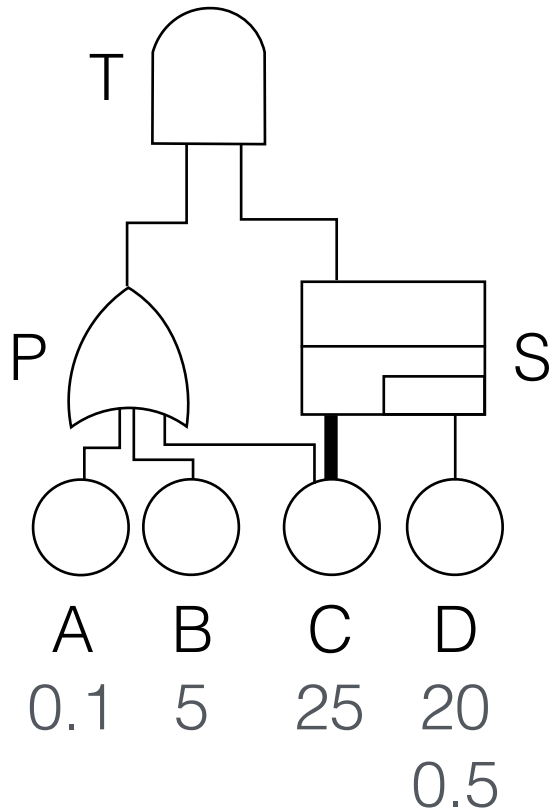
Approximation algorithm



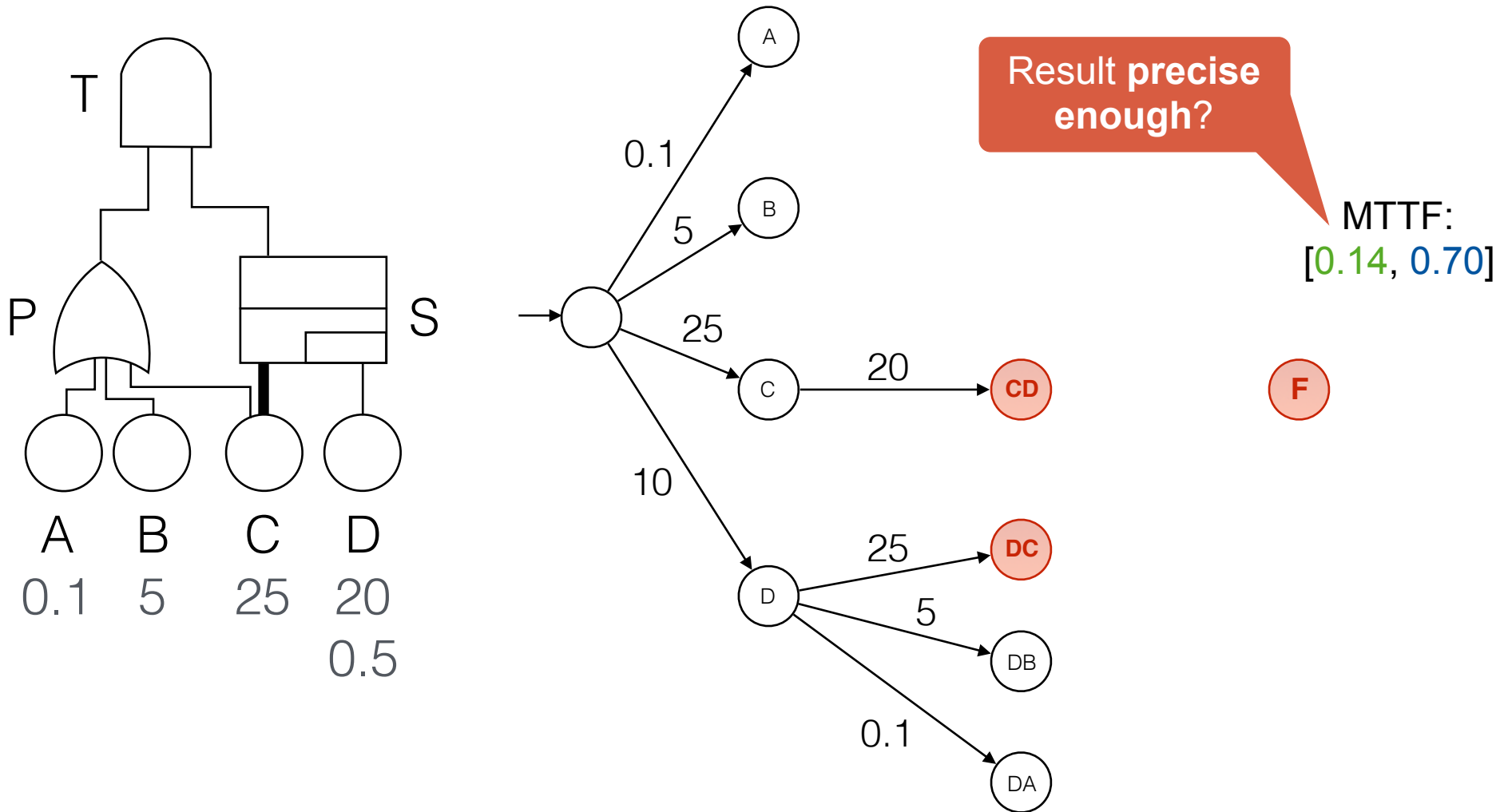
Approximation algorithm



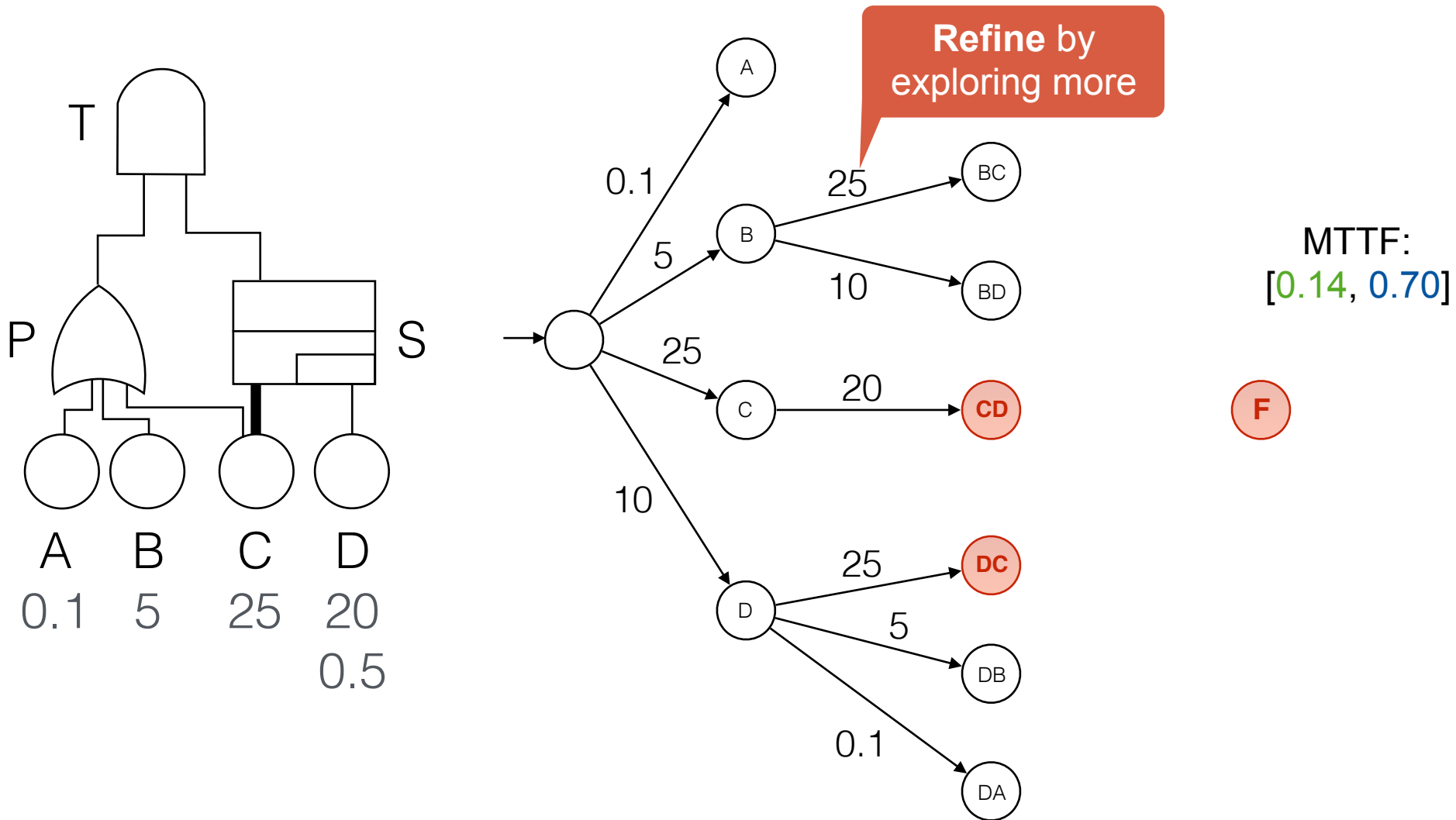
Approximation algorithm



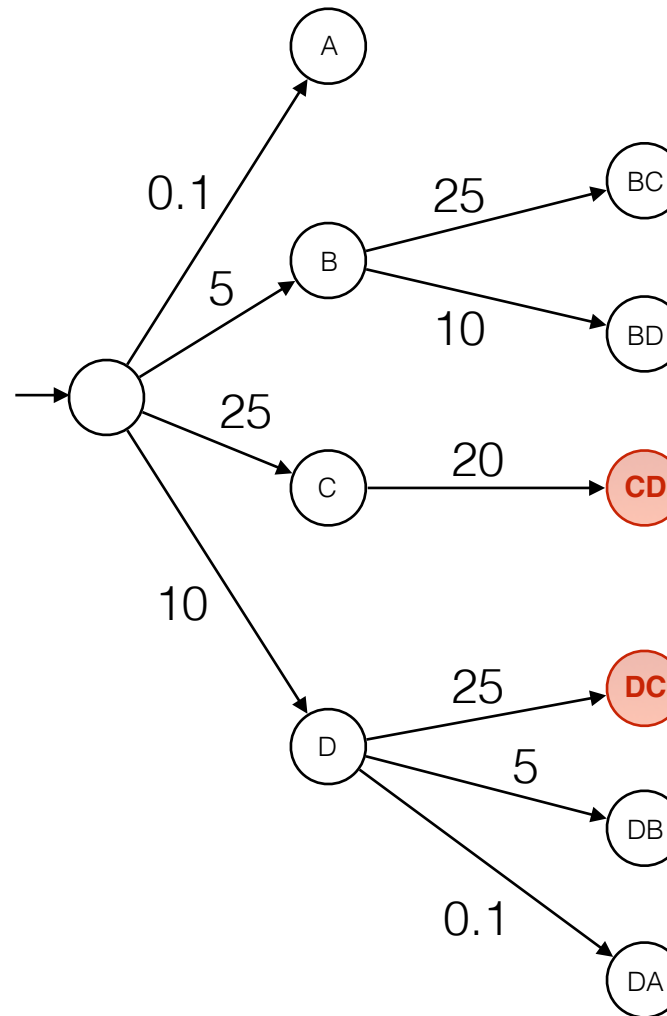
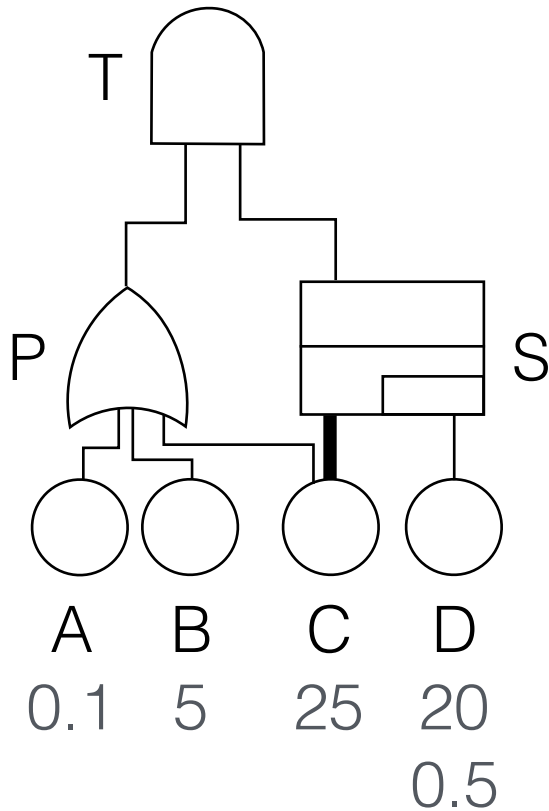
Approximation algorithm



Approximation algorithm



Approximation algorithm

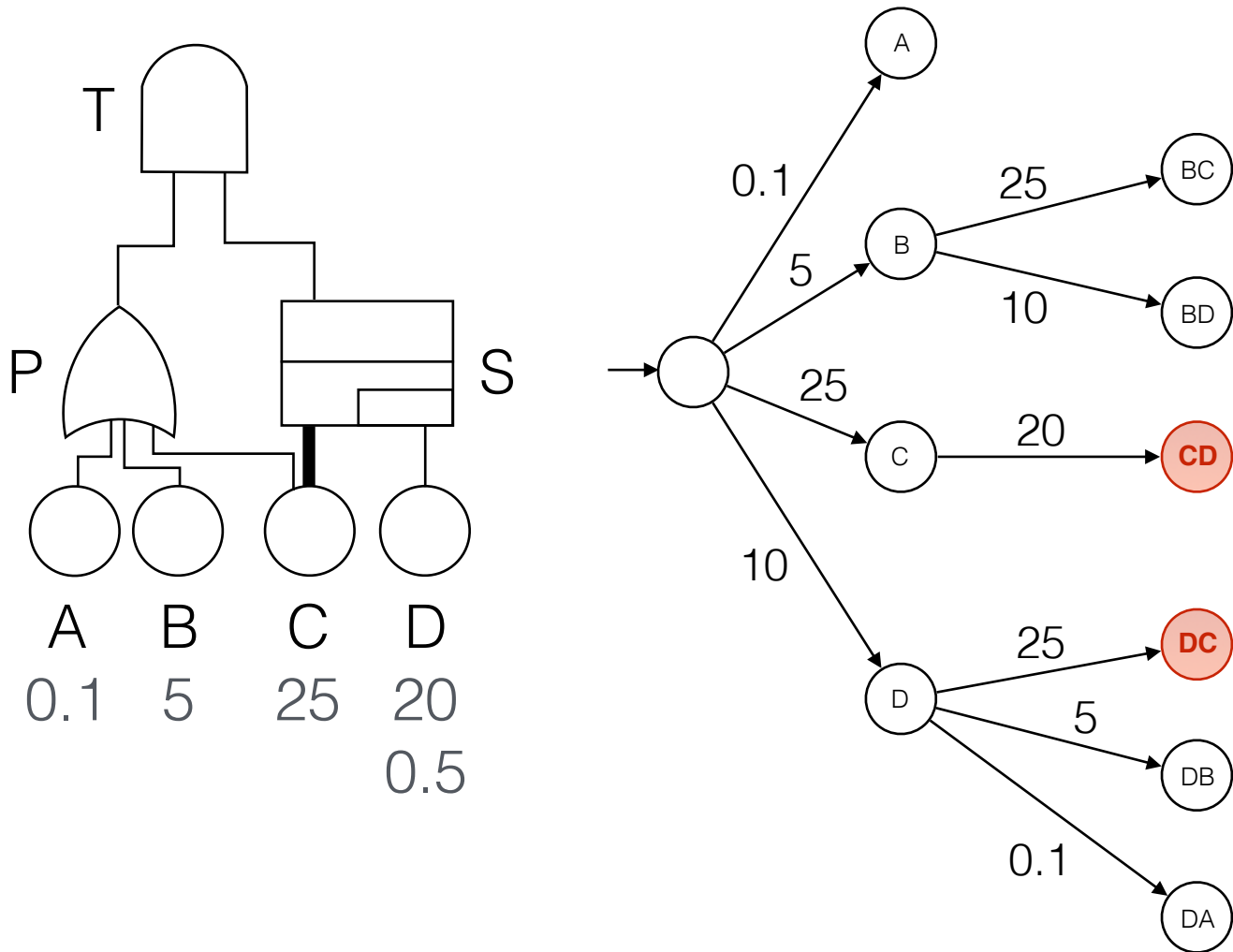


Compute approximation on refined state space

MTTF:
[0.20, 0.32]

F

Approximation algorithm



Stop if precision suffices

MTTF:
[0.27, 0.28]

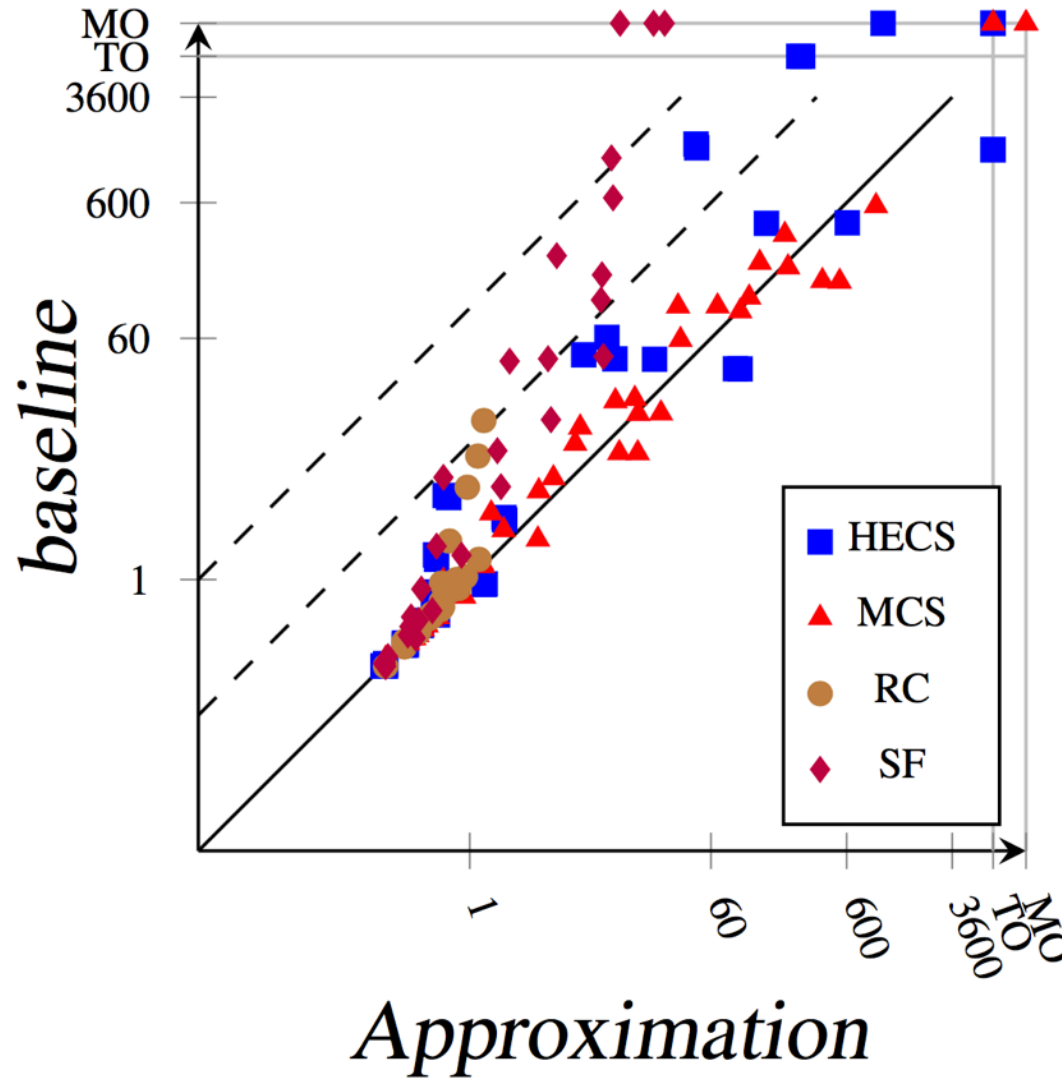
F

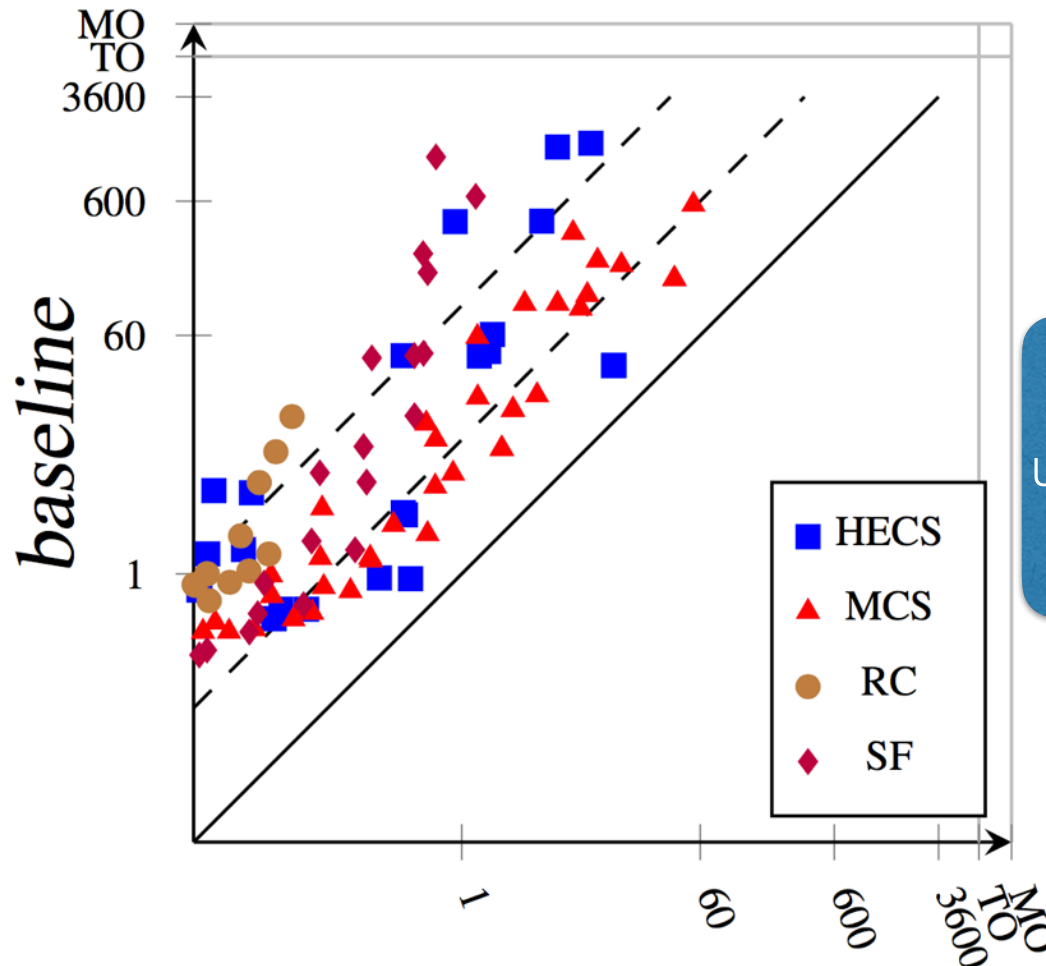
Approximation algorithm

- Approximation applicable for **reliability** and **MTTF**
- **Optimizations** still applicable
- Implemented in **Storm**
- **Fully automated** for given precision
but extendable to iterative computation with **user feedback**

Analysis run times: Approximation

[Volk et al., IEEE TII 2018]

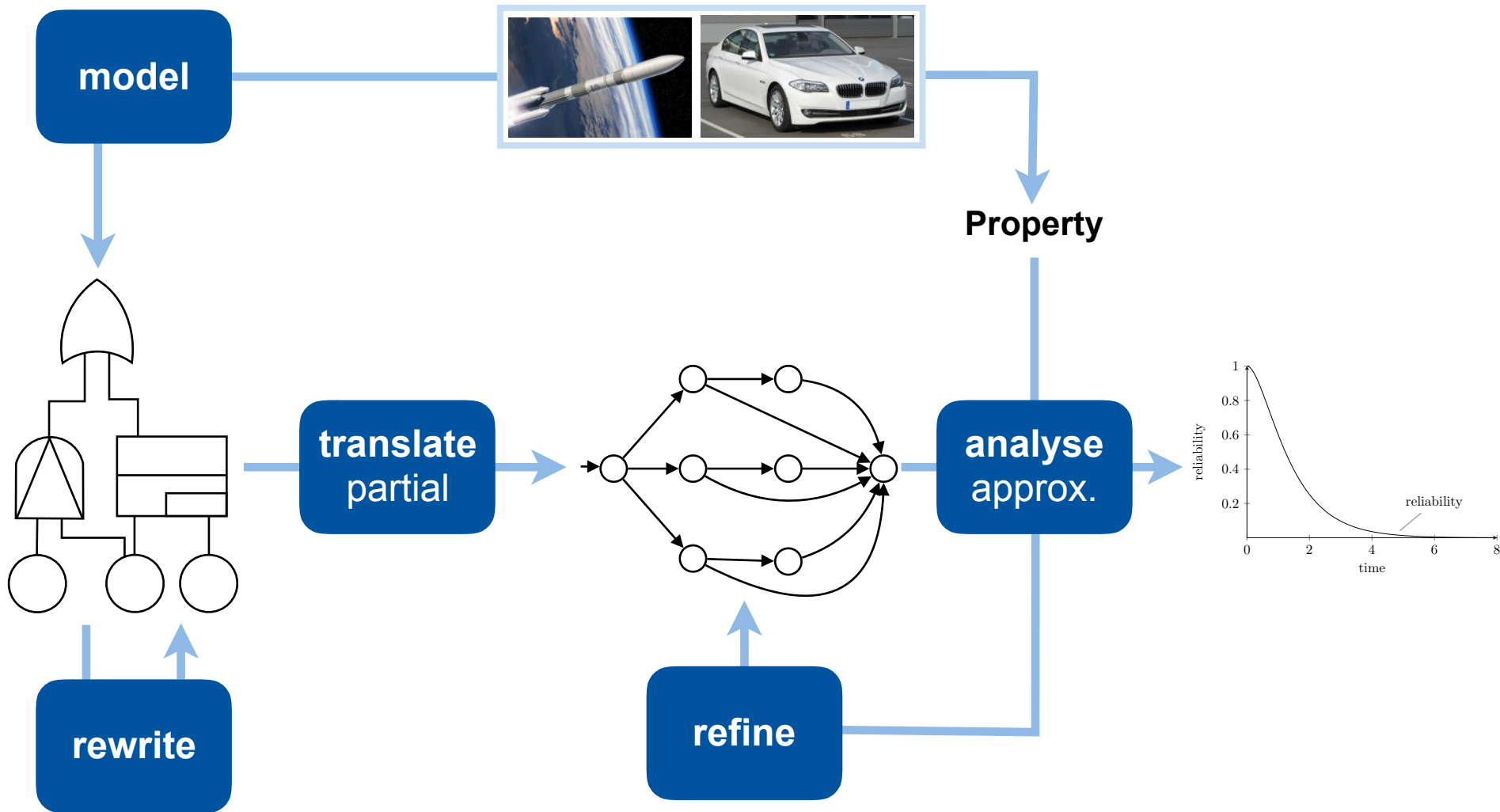




Time until
under approximation
was **95% of MTTF**

Approximation (lower bound)

Overview



A Modern Perspective on Fault Tree Analysis

Joost-Pieter Katoen and Matthias Volk



*Joint work with: Majdi Ghadhab (BMW), Dennis Guck (TWT),
Sebastian Junges (RWTH), Matthias Kuntz (BMW),
Enno Ruijters (U. Twente) and Mariëlle Stoelinga (U. Twente)*

Tutorial MMB 2018, Erlangen, BY

Roadmap of This Tutorial

Part 1. What are Dynamic Fault Trees?

- DFT Elements, Benchmarks, Intricacies, DFTs as Stochastic Petri Nets

Part 2. From DFTs to Markov Models, Compositionally

- Compositional State-Space Minimisation, Non-Determinacy

Part 3. From DFTs to Markov Models, Monolithically

- Symmetry Reduction, Don't Care Propagation

Part 4. DFT Analysis by Model Checking

- Reliability Measures, Core Algorithms, Storm Tool

Part 5. Advanced Optimisations

- Graph Rewriting, Partial State-Space Generation

Part 6. Industrial Applications and Outlook

Focus is on conveying intuition and experimental results

Overview

Part 6: Industrial Applications and Outlook

- Maintenance Analysis in Railway Engineering

- Safety Analysis of Autonomous Cars

- Outlook

- Some Literature

BMW case study

[Ghadhab *et al.*, 2017]

- ▶ **Topic:** Design-phase safety analysis of **autonomous vehicle guidance**
 - ▶ ASIL¹ D, i.e., 10^{-8} residual hardware failures per hour
 - ▶ **Fail-operational:** continue to operate a while after component failure
- ▶ **Inputs:**
 - ▶ Functional blocks: environment perception, trajectory planning, etc.
 - ▶ Safety concepts: TMR, nominal+safety path, main+fall-back path
 - ▶ Hardware architectures: for different safety concepts
- ▶ **Outputs:** which **function-2-hardware mapping yields optimal safety?**
- ▶ **Approach:**
 - ▶ Generate Dugan's **dynamic fault trees**
 - ▶ Analyse them using **probabilistic model checking**
- ▶ **Analysis outcomes**

¹Automotive Safety Integrity Level

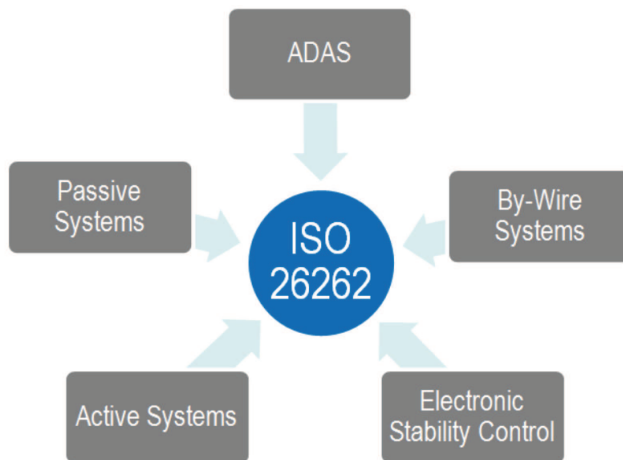
Autonomous Vehicle Guidance



Major safety goal: **avoid wrong vehicle guidance.**

Automotive Safety Integrity **Level D**, i.e., 10^{-8} residual hardware failures per hour

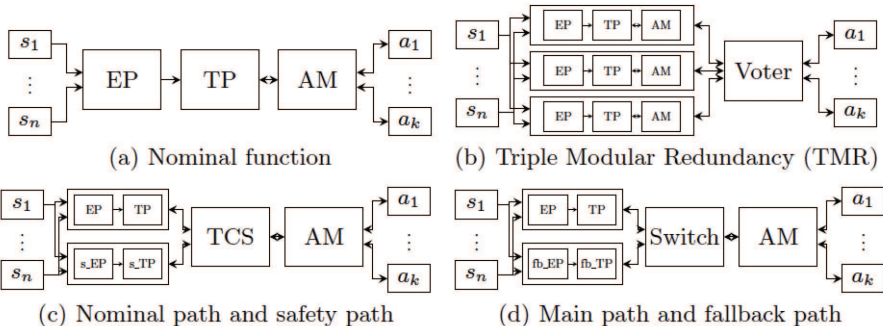
Fail Operational



Fail-operational: continue to operate a while after component failure



Functional Blocks+Safety Concepts

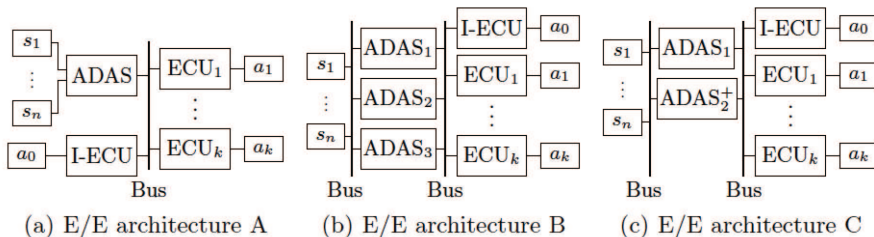


Fail-operational design patterns for autonomous driving.

EP = Environment Perception, TP = Trajectory Planning

AM = Actuator Mgt, TCS = Trajectory Checking and Selection

Sample Car Architectures



(a) **nominal**, (b) **"TMR"**, and (c) **ADAS+** architecture.

Assumption: during a transient fault, no other faults occur (conform ISO 26262)

ADAS = Advanced Driver Assistance System, I-ECU = Integration ECU

Sample Safety Metrics

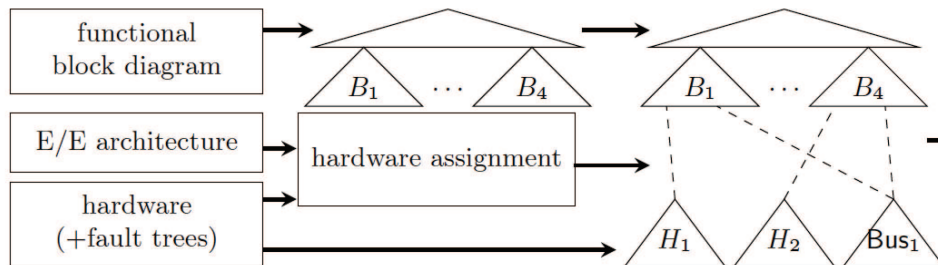
System integrity \approx probability of safe operation during operational lifetime

1. How probable is it that the system is fully functional at time t ?
2. What is the fraction of system failures w/o being degraded first?
3. The expected time to failure upon becoming degraded?
4. Criticality: how likely is it to fail within a drive cycle once degraded?
5. System integrity when limiting operational time after degradation?

Phrasing in Temporal Logic

	Measure	Model Checking Queries
System	integrity	$1 - P(\Diamond^{\leq t} \text{ failed})$
	FIT	$\frac{1}{\text{lifetime}} \cdot (1 - P(\Diamond^{\leq \text{lifetime}} \text{ failed}))$
	MTTF	$ET(\Diamond \text{ failed})$
Degradation	FFA	$1 - P(\Diamond^{\leq t} (\text{failed} \vee \text{degraded}))$
	FWD	$P((\neg \text{degraded}) \text{ U}^{\leq t} (\neg \text{degraded} \wedge \text{failed}))$
	MTDF	$\Sigma_{s \in \text{degraded}} (P(\neg \text{degraded} \text{ U } s) \cdot ET^s(\Diamond \text{ failed}))$
	MDR	$\text{argmin}_{s \in \text{degraded}} (1 - P^s(\Diamond^{\leq t} \text{ failed}))$
	SILFO	$1 - \left(FWD + \Sigma_{s \in \text{degraded}} (P(\neg \text{degraded} \text{ U}^{\leq t} s) \cdot P^s(\Diamond^{\leq \text{drivecycle}} \text{ failed})) \right)$

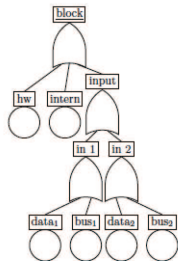
Fault Tree Generation



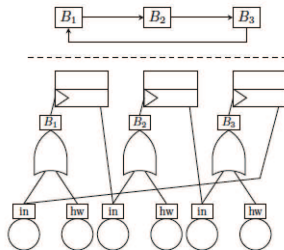
Three-level fault trees: (1) system, (2) block, and (3) HW level

- Why DFTs?
 - Warm+cold redundancies, spare components, state-dependent faults
 - Communication via **fallible buses**, depending on HW assignment

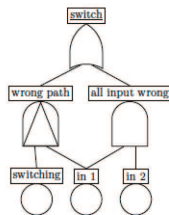
Sample DFTs for Case Study



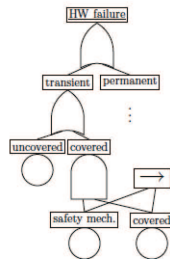
(a) Block FT



(b) Feedback loop and FT



(c) Switch FT



(d) Hardware FT

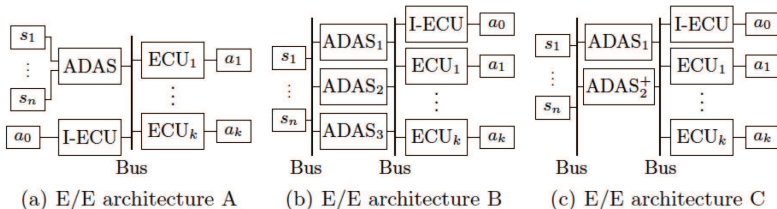
SPARE gates are used for modelling cold stand-by of fall-back paths



Case Study Characteristics

	Scenario					DFT			CTMC		Degrad.
	SC	Arch.	Adap.	Sens.	Act.	#BE	#Dyn.	#Elem.	#States	#Trans.	
I	SC1	B	—	2/4	4/4	76	25	233	5,377	42,753	—
II	SC2	B	—	2/4	4/4	70	23	211	5,953	50,049	19.35%
III	SC2	C	ADAS+	2/4	4/4	57	19	168	1,153	7,681	16.65%
IV	SC3	C	—	2/4	4/4	57	21	170	385	1,985	12.47%
V	SC2	A	—	2/4	4/4	58	19	185	193	897	0.00%
VI	SC2	B	w/o I-ECU	2/4	4/4	65	21	199	1,201	8,241	19.98%
VII	SC2	B	5 ADAS	2/8	7/7	96	30	266	$2 \cdot 10^5$	$2 \cdot 10^6$	19.35%
VIII	SC2	B	8 ADAS	6/8	7/7	114	36	305	$4 \cdot 10^6$	$66 \cdot 10^6$	10.90%

SC1 = TMR, SC2 = nominal and safety path, SC3 = main and fall-back path



(A) **nominal**, (B) **"TMR"**, and (C) **ADAS+** architecture.



Case Study Characteristics

	Scenario					DFT			CTMC		Degrad.
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VIII	SC2	B	8 ADAS	6/8	7/7	114	36	305	4 10^6	66 10^6	10.90%

#BE = the number of basic events (aka: leaves) in the DFT

#Dyn. = the number of dynamic gates in the DFT

#Elem. = the total number of elements in the DFT



Case Study Characteristics

	Scenario					DFT			CTMC		Degrad.
	SC	Arch.	Adap.	Sens.	Act.	#BE	#Dyn.	#Elem.	#States	#Trans.	
I	SC1	B	—	2/4	4/4	76	25	233	5,377	42,753	—
II	SC2	B	—	2/4	4/4	70	23	211	5,953	50,049	19.35%
III	SC2	C	ADAS+	2/4	4/4	57	19	168	1,153	7,681	16.65%
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VIII	SC2	B	8 ADAS	6/8	7/7	114	36	305	$4 \cdot 10^6$	$66 \cdot 10^6$	10.90%

Degrad. = fraction of degraded states in the DFT's Markov chain

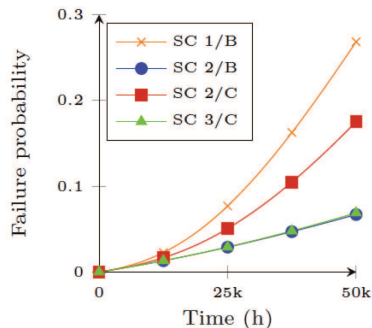
Timings

	I	II	III	IV	V	VI	VII	VIII
Model generation	1.02 s	1.02 s	0.38 s	0.33 s	0.34 s	0.40 s	25.13 s	632.89 s
System + FFA + FWD	0.02 s	0.02 s	0.00 s	0.00 s	0.00 s	0.00 s	1.46 s	46.67 s
MTDF	—	2.67 s	0.18 s	0.03 s	0.02 s	0.20 s	2892.42 s	>3600 s
MDR	—	0.60 s	0.11 s	0.02 s	0.02 s	0.11 s	26.07 s	781.93 s
SILFO	—	1.83 s	0.17 s	0.04 s	0.02 s	0.18 s	1694.91 s	>3600 s

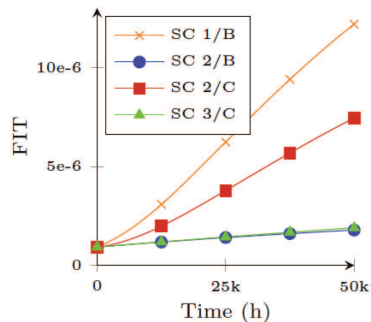
Computing MTDF and SILFO are computationally intensive

Partial state-space exploration for VIII of $\approx 10\%$ yields bounds of 3% error in 22s.

Analysis Results

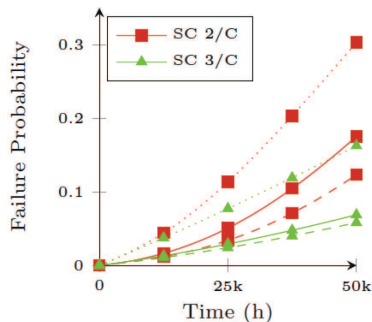


(a) Probability of failure

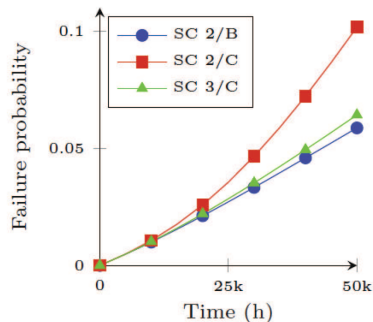


(b) FIT

Analysis Results



(c) Sensitivity analysis



(d) SILFO

Sensitivity is investigated by varying the failure rates
 SILFO = System Integrity under Limited Fail-Operation

Model Checking Boosts FT Analysis

- ▶ More safety measures
- ▶ Larger classes of DFTs can be analysed
- ▶ Typically substantially faster than classical FT analysis
- ▶ Abstraction aggravates this further:
 - ▶ tailored simplification for FTs + abstraction-refinement on FTs yields several orders of magnitude improvements.
- ▶ Full automation

Try it out yourself: stormchecker.org

No myths.

Railway case studies

- ▶ Series of case studies with stakeholders from railway engineering
 - ▶ asset manager [ProRail](#)
 - ▶ rolling stock maintenance company [NS/NedTrain](#), and
 - ▶ consultancy company [Movares](#)
- ▶ Focus: study of effect of [maintenance](#) strategies
- ▶ Property: trade-off between [reliability](#) and [maintenance costs](#)
- ▶ Based on [extension](#) of DFTs with [simple maintenance](#)
- ▶ Analysis using probabilistic and statistical [model checking](#)

Maintenance



Maintenance

Types:

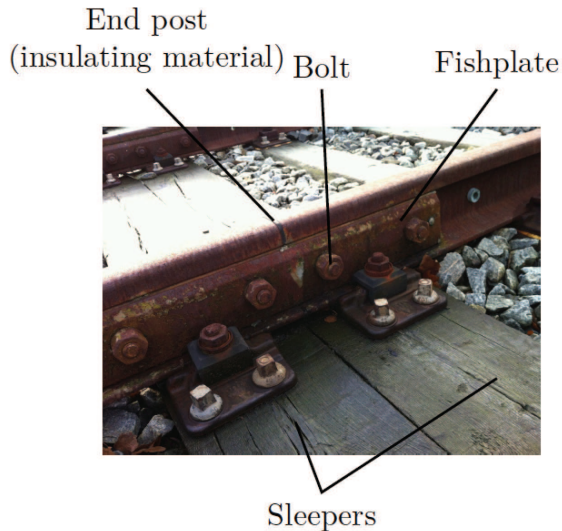
- Corrective maintenance
- Preventive maintenance

Strategies:

- Age-based
- Use-based
- Condition-based

Analysing Electrically Insulated Joint

[Ruijters *et al.*, 2016]

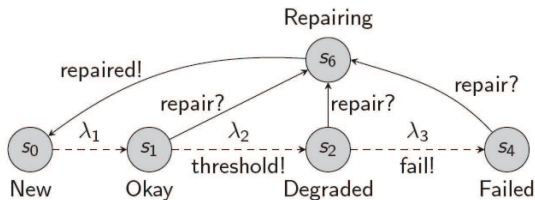


Maintenance in DFTs

- ▶ Many failures are not random events
 - ▶ Wear over time
 - ▶ Production faults
 - ▶ Caused by other failures
- ▶ Maintenance is essential for reliability
 - ▶ Reduce or prevent wear
 - ▶ Replace or repair worn components
 - ▶ Correct failures when they occur
- ▶ Maintenance is not a first-class citizen in DFTs

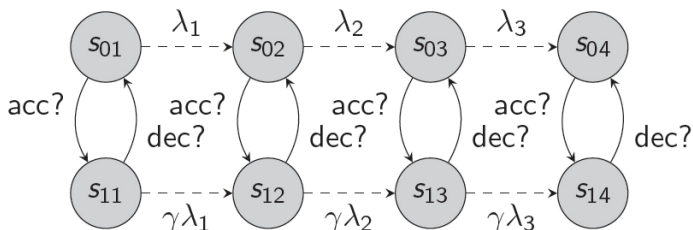
DFTs with Maintenance

- ▶ Idea: equip BEs with several degradation stages
- ▶ Maintenance := timed automaton with degradation stages
- ▶ Signals for composition:
 - ▶ Maintenance threshold, Repair, and Failure
- ▶ Other modules will send/receive these signals

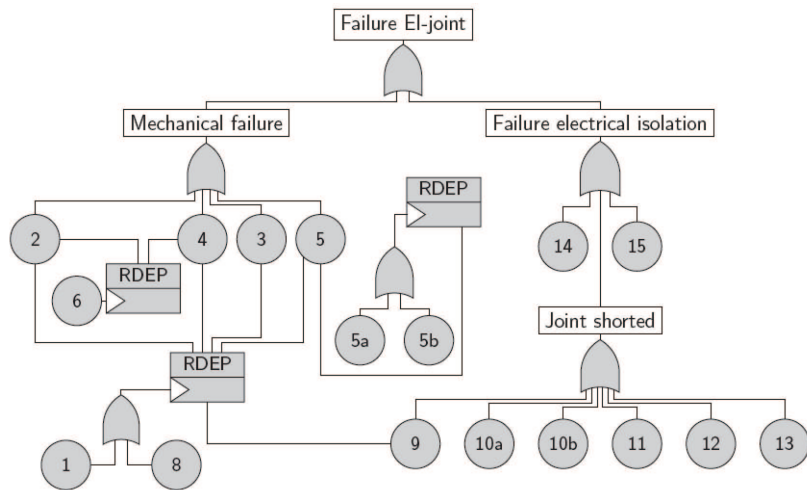


Rate-affecting failures

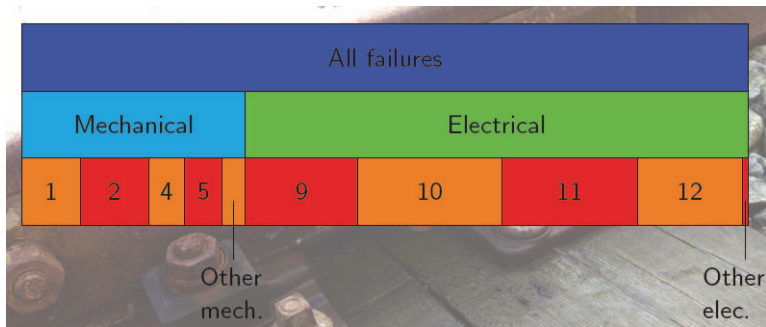
- Some failures accelerate wear of other components
- New variant on the FDEP gate: **rate dependency** (RDEP)
 - Failure of trigger BE accelerates degradation by factor γ
 - Repair of trigger BE does not repair triggered BE



DFT for the EI Joint



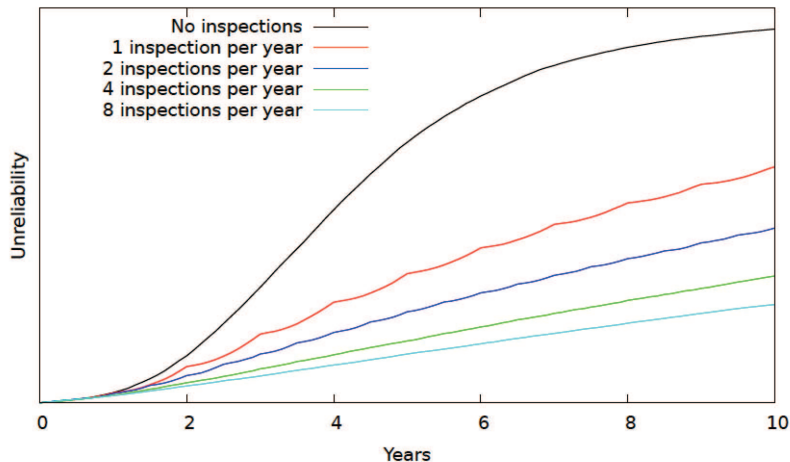
Failure Causes



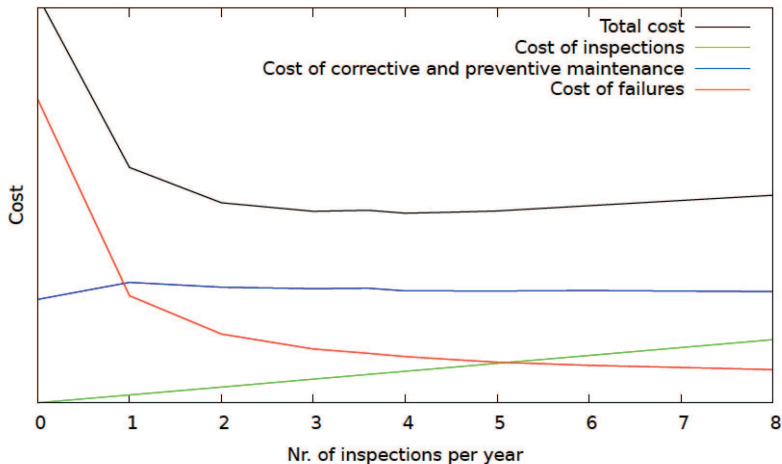
Parameters for the BEs for the EI-Joint

BE nr.	Failure mode	ETTF	ETTF		Prob. cnd.
			NRG	Phases	
1	Poor geometry	5	5	4	10%
2	Broken fishplate	8	12	4	33%
3	Broken bolts	15	20	4	33%
4	Rail head broken out	10	15	4	33%
5	Glue connection broken	10	15	4	33%
5a	Manufacturing defect	-	-	-	0.25%
5b	Installation error	-	-	-	0.25%
6	Battered head	20	22	4	5%
7	Arc damage	1	1	3	0.2%
8	End post broken out	7	8	3	33%
9	Joint bypassed: overhang	5	8	4	100%
10a	Joint shorted: shavings (normal)	1	1	4	12%
10b	Joint shorted: shavings (coated)	10	10	4	3%
11	Joint shorted: splinters	200	200	1	100%
12	Joint shorted: foreign object	250	250	1	100%
13	Joint shorted: shavings (grinding)	5000	5000	1	100%
14	Sleeper shifted	5000	5000	1	100%
15	Internal insulation failure	5000	5000	1	100%
16	End post jutting out	20	20	1	100%

Unreliability



Analysis results: inspection rate

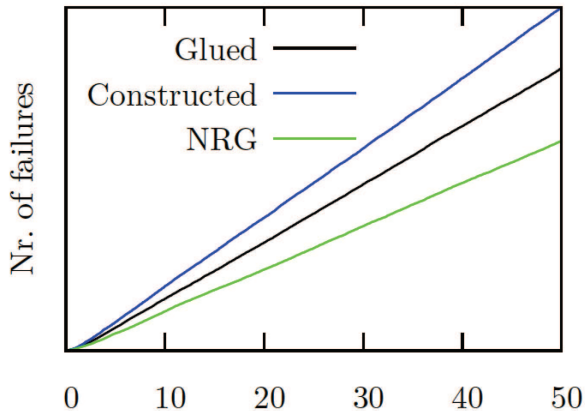


The new NRG joint



- ▶ Elongated fishplate to spread the stress on the plate
- ▶ Six bolts instead of four, to reduce flexing when a train drives over the joint
- ▶ Repositioned bolts to distribute stress over the bolts more evenly

Failure rates (over the years)



Conclusions

- ▶ The current maintenance policy is close to cost-optimal
- ▶ Increasing joint reliability by e.g., more inspections does not pay off
- ▶ Additional maintenance costs outweigh the reduced cost of failures
- ▶ Combination of exponential and deterministic timings
 - ▶ Analysed here by statistical model checking (Uppaal SMC)
 - ▶ Semantics and numerical algorithms would be of interest

The Need for Parameter Synthesis

Fact:

Probabilistic model checking is applicable to **various areas**, e.g.:

- ▶ reliability engineering
- ▶ randomised algorithms
- ▶ systems biology

Markov models of **hundreds of millions of states** can be handled.

Limitation:

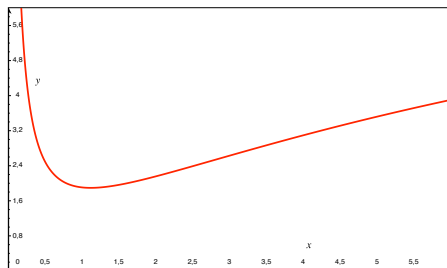
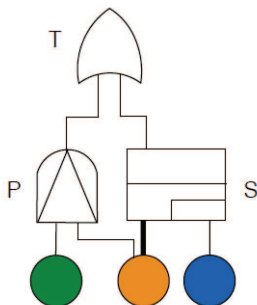
Probabilities need to be known **a priori**. Precisely.

How sensitive are results when transition probabilities fluctuate?

Goal:

Treat **parametric** models, **synthesise** “safe” parameter values

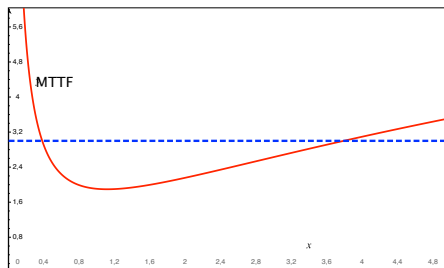
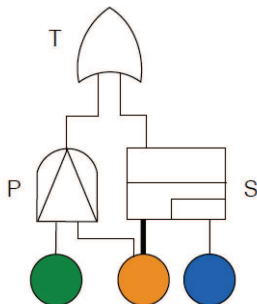
Parametric Fault Trees



Sample parametric DFT and its MTTF

$$\text{MTTF} = \frac{200x^2 + 20x + 201}{x \cdot (20x + 201)} \text{ for } (\alpha, \beta, \gamma, d) = (10, x, 0.1, 0.5)$$

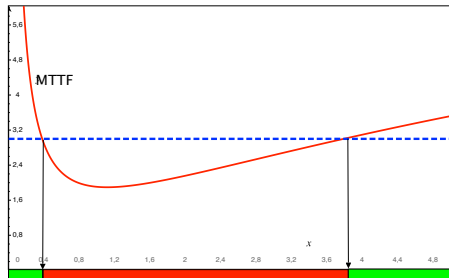
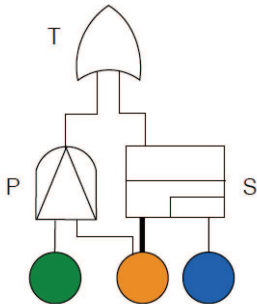
Parametric Fault Trees



Sample parametric DFT and its MTTF

For which $\frac{1}{10} \leq x \leq 10$ does **MTTF** ≥ 3 hold?

Parametric Fault Trees



Sample parametric DFT and its MTTF

For which $1/10 \leq x \leq 10$ does $\text{MTTF} \geq 3$ hold?

Further readings

- ▶ M. Volk, S. Junges, J-P. Katoen. *Fast dynamic fault tree analysis by model-checking techniques*. IEEE Transactions on Industrial Informatics, 2018.
- ▶ M. Volk, S. Junges, J-P. Katoen and M. Stoelinga. *One net fits all: A unifying semantics of DFTs using GSPNs*. 2018 (submitted).
- ▶ S. Junges et al. *Fault trees on a diet: automated reduction by graph rewriting*. Formal Aspects of Computing, 2017.
- ▶ M. Ghadhab et al. *Model-based safety analysis for vehicle guidance systems*. SafeComp 2017.
- ▶ E. Ruijters and M. Stoelinga. *Fault tree analysis: A survey of the state-of-the-art in modeling, analysis and tools*. Computer Science Review, 2015.
- ▶ S. Junges, D. Guck, J-P. Katoen and M. Stoelinga. *Uncovering DFTs*. DSN 2016.
- ▶ J-P. Katoen and M. Stoelinga. *Boosting fault tree analysis by formal methods*. Festschrift Ed Brinksma, 2017.

Tool support: www.stormchecker.org